# UNDERGRADUATE PROGRAMS IN THE MATHEMATICAL AND COMPUTER SCIENCES <br> The 1985-1986 Survey 

Donald J. Albers<br>Richard D. Anderson<br>Don O. Loftsgaarden

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This survey has been carried out under the auspices of the Conference Board of the Mathematical Sciences (CBMS). This Conference Board of organizations provides a means to address matters of common concern to the mathematical community in its broadest sense. The Conference Board is located at:

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## PREFACE

At five-year intervals, beginning in 1965, the Conference Board of the Mathematical Sciences (CBMS) has, with the financial support of The Ford Foundation in 1965 and later the National Science Foundation, conducted surveys of undergraduate programs in the mathematical and computer sciences as found in universities, four-year colleges, and two-year colleges. The surveys have obtained much information on undergraduate course enrollments, faculty, and teaching patterns in mathematical and computer science departments. The basic purpose of these surveys has been to provide information useful for decision-making in mathematical and computer science departments, professional organizations, and government agencies. The surveys have reflected the interests of the members of CBMS* and have drawn heavily on the expertise and experience of prominent individuals from the various areas of the mathematical and computer sciences represented by these organizations.

All five CBMS surveys have addressed two basic questions:

1. What are the national undergraduate course enrollments in mathematics, statistics, and computer science, how are those enrollments distributed among various types of institutions of higher education, and how do the enrollment patterns change over time?
2. What are the numbers, qualifications, personal characteristics, and teaching responsibilities of faculty in the mathematical and computer sciences, and how do these variables change over time?

* CBMS members are listed on the facing page and on the back cover.

In addition to establishing trend data on these basic questions, the present survey has initiated four special new thrusts deemed to be of importance in the mid-80's:

1. Much more detailed identification of faculty, course, and student phenomena in computer science.
2. Identification of faculty who are teaching computer science while they are members of mathematical science departments. This is especially important when examining questions related to organization of mathematical science departments and deployment of mathematical science faculty.
3. More detailed information on remediation.
4. Identification of various issues judged to be important by departments.

Questionnaire design and overall advice and guidance for the present Survey of Undergraduate Mathematical and Computer Science were provided by the CBMS Survey Committee. The members of that Committee are as follows:

Donald J. Albers, Menlo College, Chairman<br>Richard D. Anderson, Louisiana State University, Executive Director<br>Kim B. Bruce, Williams College<br>William G. Bulgren, University of Kansas<br>Wendell H. Fleming, Brown University<br>Barbara Gale, Prince George's Community College<br>Don 0. Loftsgaarden, University of Montana, Data Analyst<br>Donald Rung, Pennsylvania State University<br>Joseph Waksberg, WESTAT Research Corporation

We very much appreciate the help of Robert Aiken, Chair of the Education Board of the Association for Computing Machinery, in identifying computer scientists Kim Bruce and William Bulgren to serve on the Survey Committee and in reviewing a draft of the report.

The work of survey sample design, data analysis and report writing has been shared by three people. Data analysis and design of the sampling and estimation procedures was chiefly the work of Professor Don 0. Loftsgaarden, who also was a member of the 1980 CBMS survey project. In the early stages of sample design, Professor Loftsgaarden was assisted by Joseph Waksberg, an internationally known figure in this area of statistics.

The writing of the present report has been primarily the work of the undersigned. For several years in the 1970's Professor Anderson directed survey programs of the American Mathematical Society. Professor Alders, Chairman of the present Survey, largely authored the chapters on mathematical and computer sciences in two-year colleges in the 1975 and 1980 reports, as well as in the present one. In addition to designing the questionnaires for the present survey, the members of the Survey Committee reviewed the draft of the report making many helpful comments.

CBMS and its Survey Committee are indebted to Maureen Callanan of the Mathematical Association of America and to the other MAA staff members who administered and supported this project. Special thanks and appreciation for grant support are due the National Science Foundation, which also supported CBMS's 1970, 1975, and 1980 surveys.

Our special thanks to Cherie C. Wilks for preparation of the final manuscript.


Ejonald J. Alders
Chairman, Survey Committee


Richard D. Anderson
Executive Director of the Survey

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## INTRODUCTION

We present results from the 1985 CBMS Survey. In general, the data show for the period 1980-85 that undergraduate mathematics has recovered some ground lost in the seventies and that undergraduate computer science grew very rapidly in the first half of the eighties. There is an increasing quantification of many facets of society demanding more young people with knowledge of mathematical topics and with the ability to use computers to address increasingly complex problems of society. Thus people trained in mathematical thinking seem to be in increasing demand. The longer term enrollment data support this contention. The rather rapid development, over the past fifteen years, of computer science as an undergraduate academic discipline shows considerable adaptability of the educational system to powerful external forces. But the rather limited and slow changes observed within undergraduate mathematics itself show less impact of the forces of change.

We list Survey results in the university and four-year college sectors (Chapters 1-4) separate from those in the two-year college sector (Chapters 5-6). We include a special section on undergraduate programs in the computer sciences as Chapter 4, the result of a special questionnaire on computer science.

The Survey Committee feels, as its counterparts in the past have felt, that it should present data and findings without much policy interpretation. The factual background given here is for the use of those in education and science policy positions to use in making informed decisions. Thus we deliberately avoid making recommendations on policy issues, leaving such activities to people or groups responsible for making policy.

Our findings concern mathematical and computer science enrollment trends, faculty characteristics, instructional formats and administrative organization. The data given are estimates of national totals for fall 1985 in institutions of higher education. The estimates are based on
responses to questionnaires sent to a stratified random sample of schools from among 2,463 institutions with undergraduate programs in the mathematical or computer sciences. The stratification was by total student enrollments in universities, four-year colleges and two-year colleges. The sampling and estimation procedures are explained in Appendix A. The table given later in this introduction shows sampling and response rates in various categories of institutions and departments. The consistently high response rates in various strata give us confidence in the overall data reported although the lower response rates from computer science departments make the details of computer science data somewhat less reliable. See Appendix F for the list of all respondents. The lists and categories of universities, public four-year colleges, private four-year colleges and two-year colleges were obtained from NCES (National Center for Educational Statistics, now the Center for Education Statistics) lists of the most recent year (1982) available to us at the time of preparing the sample. Similar lists were used in the 1980 Survey. It should be noted that the list of universities is not the same as that used in the annual AMS Survey of doctoral producing departments. There is an overall $70-75 \%$ overlap with the AMS lists and a larger percentage overlap with AMS Groups I and II departments. Generally the four-year public college category is comparable to, but larger than, the AMS masters producing department category (M) and the private four-year college category is comparable to the AMS bachelors producing category (B) but they are not, in fact, identical and considerable variation from AMS data is to be expected. The Survey Committee felt that the advantages of using lists comparable to those of the 1980 Survey and of those used in other disciplines outweighed the advantages of using AMS lists. Indeed, we sampled institutions, not departments, in order to get national characteristics. For the institutions in the sample, questionnaires were sent to all mathematics departments or to the division in charge of mathematics courses. In addition, questionnaires were sent to all computer science, statistics or other mathematical science departments that were determined to exist at sampled institutions.

This Survey provides a valuable statistical data base concerning what was going on in the fall of 1985 in collegiate mathematics, statistics,
and computer science and what changes have occurred over the previous five to twenty-five years. It should be of continuing value to educational policy makers in and out of the mathematical and computer science communities. But the reader should keep in mind that it is not designed to give more than background information on important issues facing our community and our increasingly technological society. Among these issues not specifically addressed by the Survey are:

- What should our youth be learning to equip them (and us) to face the challenges of an ever-more rapidly changing technological world of tomorrow and how well equipped is our system and our faculty to address these developing student needs?
- What are the support levels and mechanisms necessary to effect a transition into education for the 21st century?

If anything, the data appear to suggest both rather slow adaptation to a rapidly changing society except in the development of computer science as an undergraduate discipline. Support levels in the mathematical sciences seriously lag even existing patterns of change.

SAMPLING AND RESPONSE RATES IN DEPARTMENTS OF MATHEMATICS, STATISTICS AND COMPUTER SCIENCE

|  | Population | Sample | Respondents | Response $\qquad$ |
| :---: | :---: | :---: | :---: | :---: |
| Universities |  |  |  |  |
| Mathematics | 157 | 72 | 56 | 78\% |
| Statistics | 40 | 21 | 19 | 90\% |
| Comp. Sci. | 105 | 51 | 32 | 63\% |
| Public 4-Yr. Colleges |  |  |  |  |
| Mathematics | 427 | 105 | 81 | 77\% |
| Statistics | 5 | 2 | 2 | 100\% |
| Comp. Sci. | 141 | 40 | 24 | 60\% |
| Private 4-Yr. Colleges 80 |  |  |  |  |
| Mathematics | 839 | 80 | 57 | 71\% |
| Comp. Sci. | 150 | 16 | 8 | 50\% |
| Two-Year Colleges | 1040 | 172 | 110 | 64\% |

The response rates generally were a bit higher than those for the 1975 Survey and a bit lower than those for the 1980 Survey. We believe the responses (compared for early and late respondents) are generally adequate to justify the numerical conclusions given.

There are two major periodic surveys in the mathematical community (1) the CBMS Survey conducted every five years (with Ford Foundation support in 1965 and with NSF support since 1970) published in a form such as this report, and (2) the annual American Mathematical Society (AMS) Survey, with reports published periodically in the AMS Notices. Both Surveys are directed by committees appointed by the sponsoring professional organizations. Over the years, the two committees have had considerable overlapping membership. The committees actively cooperate with each other and compare data.

The CBMS Survey is much lengthier and more detailed and is based on careful statistical sampling (with followups) and with projections to the total populations. It is concerned primarily with undergraduate education, is designed to cover both the mathematical and the computer sciences, and in both 1980 and 1985 has been based on lists of undergraduate institutions available from the Department of Education. It has a related but separate component on two-year colleges.

The AMS Survey is primarily a faculty and new doctorate survey, it concentrates now only on the mathematical sciences (since the response rates from computer science departments were getting progressively worse), and it gets limited information on course enrollments as a byproduct. However, since the AMS gets comparable data from both the current and past year, it monitors year-by-year changes very effectively.

The categories of institutions used by the CBMS Survey are Universities (Public and Private for sampling, but since 1980 reported in one "University" category), Four-Year Public Colleges, Four-Year Private Colleges and Two-Year Colleges. The AMS Survey currently classifies departments in the mathematical sciences by Groups I, II, and III (PhD producing mathematics departments), Group IV (Statistics departments), Group V (Applied mathematics, OR, etc., departments with doctoral programs), Group VI (Canadian departments) and Group M (Masters producing) and Group B (Bachelors producing) departments.

Both surveys collect and present data by their categories of institutions on numbers of full- and part-time faculty, on numbers of GTA's, and on enrollments in selected types of courses. Since the categories do not explicitly correspond, the numbers by categories can not be directly compared. However restricting the CBMS data to university mathematics departments, and after allowing for known differences in the specific institutions on the AMS and CBMS lists, the figures for numbers of full-time faculty and GTA's are in close agreement, with the AMS totals being expectedly about $10 \%$ higher than the CBMS totals.

Another relevant survey is the so-called Taulbee Survey of the Computer Science Board. Like the AMS Survey it is concerned primarily with PhD programs and their graduates and with the faculty of such programs. The 1985-86 Taulbee Survey had responses from 117 out of 118 PhD producing computer science departments (including 10 Canadian departments). The total faculty size in these 107 U.S. departments was almost half-again as large as that shown for the full-time faculty in the departments identified by CBMS in the university category (which included a number of computer science bachelors or masters producing departments). It is believed that this difference is largely explained by the known variations in the lists of departments in the categories used in the two surveys, by the fact that the Taulbee Survey figures apparently included some or all part-time faculty (presumably on a pro-rata basis), and different possible interpretations of whether to count visitors and/or faculty on leave.

## SUMMARY HIGHLIGHTS

We give some of the highlights of the Survey as a summary of the results. The reader is advised to note carefully the distinctions made at the beginning of Chapter 2 with respect to various components of the faculty. The reader is advised to read the relevant portions of Chapters 1 to 6 to better understand the limitations or qualifications of these highlights.

## HIGHLIGHTS

## FOUR-YEAR COLLEGES AND UNIVERSITIES

- While overall undergraduate enrollments in universities and four-year colleges were almost stable since 1980, mathematics course enrollments increased by $6 \%$ to $1,619,000$, statistics by $41 \%$ to 208,000, and computer science by $74 \%$ to 558,000 .
- The number of undergraduate degrees in mathematics and statistics (all types including mathematics education) was 20,096, up from 13,906 in 1980 but not up to the 24,181 level of 1975 . The number of degrees in computer science was 29,107, up from 8,917 in 1980 and from 3,636 in 1975.
- After a sharp rise from 1975 to 1980, the enrollments in remedial mathematics were 251,000, up from 242,000 five years earlier, a 4\% increase.
- The enrollments in upper division mathematics courses were up $52 \%$ over 1980 levels reversing a downward trend from the '70's.
- Undergraduate statistics enrollments have been increasing markedly since 1960.

1 The full-time faculty in the mathematical and computer sciences grew by $21 \%$ in the period 1980-1985 and now numbers 22,194 while the part-time faculty grew by $46 \%$ to 9,189 .

- Since 1970, the FTE (full-time equivalent) faculty of all those teaching in the mathematical sciences in four-year colleges and universities increased by $6 \%$ while the course enrollments in the mathematical sciences increased by $41 \%$. In the same period, the overall FTE faculty in the mathematical and computer sciences grew by $40 \%$ while course enrollments grew by $72 \%$.
- The total computer science faculty (i.e. teachers of computer science) is now 5,651 full-time ( 3,605 in computer science departments), 5,342 part-time (1,984 in computer science departments) for a total 7,432 FTE, up from an estimated 1,182 FTE in 1970. See page 37 for explanations of special faculty terminology.
- The percentage of doctorates among the full-time faculty has decreased from $82 \%$ in 1975 to $73 \%$ in 1985 in the mathematical and computer sciences.
- Teaching load assignments generally are similar to those in 1970. Typical computer science and statistics faculty teaching assignments are less than those for mathematics faculty.
- The creation of new computer science departments and the broadening of departmental duties and names to include computer science were frequent administrative changes.
- In five major introductory courses, $41 \%$ of university students are taught in large lecture-type sections (over 80 students) whereas in private colleges only $2 \%$ are. About one-fifth of all students in these five courses are taught in sections of 40 to 80 students.
\| There is little required use of computers in college algebra or calculus or in any mathematics course other than numerical analysis or other computing related courses.
- Since 1980 the number of graduate teaching assistants has been stable in university mathematics departments but has gone up markedly in statistics and computer science departments and in public college mathematics departments.
- About 95\% of all graduate teaching assistants in mathematics, statistics or computer science are students in the same or related subjects.
- Salary levels and departmental support practices are widely regarded as major problems in mathematics and statistics departments.
- Two-thirds of all universities, one-third of all public four-year colleges, and more than one-sixth of private four-year colleges have separate computer science departments. In the private four-year college category the number is 150 , more than triple that for 1980.

1 Of the 3,754 doctorates who teach computer science full-time, 1,291 have their degrees in computer science and 1,555 in mathematics. Of the 2,231 doctorates who teach computer science part-time, 181 have their degrees in computer science whereas 1,369 have their degrees in mathematics.

- Half of all part-time computer science faculty teach full-time in the same institution, almost a third are employed outside education and a tenth are not employed full-time anywhere.
- Half (49\%) of all computer science sections are taught in mathematics departments, the rest in computer science departments.
- In a substantial number of institutions, some computer science is taught outside mathematics and computer science departments, chiefly in business, engineering and education academic units.
- Total reported enrollments in computer science have climbed from 107,000 in 1975 to 321,000 in 1980 to 558,000 in 1985.
- There were 29,107 computer science undergraduate degrees in fiscal year 1984-85, with 8,646 of these in mathematics departments. In addition there were 3,084 joint majors with mathematics. The number of computer science degrees reported in the 1980 Survey for fiscal year 1979-80 was 8,917.
- About two-thirds of all institutions with computer science major programs require calculus for computer science majors, one-half require linear or matrix algebra and more than two-fifths require discrete mathematics.
\| The most common problems reported by computer science departments are salary levels and patterns, departmental support services, the need to use temporary faculty, and the upgrading and maintenance of computer facilities.

TWO YEAR COLLEGES

- Mathematical science enrollments remained essentially unchanged since 1980, decreasing by $1 \%$ whereas overall two-year college enrollments decreased by $2 \%$. Part-time students continued to account for nearly $2 / 3$ of all two-year college students. Nearly $2 / 3$ of all two-year college associate degrees are in occupational programs.
- Some specific mathematics course areas showing enrollment increases since 1980 in two-year colleges were statistics (29\%), calculus (13\%), remedial (9\%), other precalculus (4\%) and computing (3\%). Some showing decreases were technical mathematics (56\%), business mathematics (42\%) and mathematics for liberal arts (42\%). Remedial mathematics now accounts for almost $47 \%$ of all enrollments in the mathematical and computer sciences, up from $42 \%$ in 1980.
- The figures on course enrollments above are from mathematics programs per se. A substantial number of mathematics and computing courses are taught outside these mathematics programs. Estimates indicate that in 1985 more than $50 \%$ of business and technical mathematics was taught outside, about $20 \%$ of arithmetic, about $15 \%$ of statistics, about $80 \%$ of data processing and about $60 \%$ of computer science other than data processing. These courses were taught primarily in business and occupational programs.
- Access to computers as well as the impact of computers and calculators on mathematics teaching has increased. But even so, excluding computer science sections, less than $7 \%$ of all sections involve computer assignments for students.

1 Mathematics labs have been established in $82 \%$ of all two-year colleges, up from 68\% in 1980.

- Since 1980 there has been a marked decrease in the number of two-year colleges using any of the various alternative forms of instruction: TV, film, programmed, CAI, PSI, etc.
- Two-year college mathematical science faculty increased by $12 \%$ since 1980 in each of the full- and part-time categories. In 1985 there were 6,277 full-time and 7,433 part-time faculty. The percentage of doctorates among full-time faculty decreased to $13 \%$, the first decrease noted since 1970. Since 1975 the percentage of women on the full-time faculty increased from $21 \%$ to $31 \%$ and the percentage of
ethnic minorities increased from $8 \%$ to $12 \%$. About $43 \%$ of the full-time faculty reported teaching overloads but overall teaching loads decreased for the first time since 1970.
- Remediation was cited as the biggest problem facing faculties in the mid-1980's.


## CHAPTER 1

## UNDERGRADUATE STUDENTS

This chapter reports estimated national student enrollments in university and four-year college mathematical and computer science courses in fall 1985. Detailed course-by-course enrollments for universities, public four-year colleges and private four-year colleges are given in Appendix E. This chapter also contains analyses of undergraduate degrees granted in the mathematical and computer sciences. Extra computer science data is provided in Chapter 4. The current chapter provides some specially prepared data on undergraduate statistics. Where data is known and relevant, it also provides information on changes in undergraduate student phenomena over time.

## HIGHLIGHTS

- While overall undergraduate enrollments in universities and four-year colleges were almost stable since 1980, mathematics enrollments increased by $6 \%$, statistics by $41 \%$ and computer science by $74 \%$.
- The number of undergraduate degrees in mathematics and statistics (all types, including mathematics education) was 20,096, up from 13,906 in 1980 but not up to the 24,181 level of 1975 . The number of degrees in computer science was 29,107, up from 8,917 in 1980 and from 3,636 in 1975.
- After a sharp rise from 1975 to 1980, the enrollments in remedial mathematics were 251,000, up from 242,000 five years earlier, a $4 \%$ increase.
- The enrollments in upper division mathematics courses were up $52 \%$ over 1980 levels reversing a downward trend from the '70's.
- Undergraduate statistics enrollments have been increasing markedly since 1960.


## TRENDS IN UNDERGRADUATE EDUCATION

We begin with some data over time from Department of Education Publications "Projections of Educational Statistics", "Digest of Educational Statistics" and other national compilations of information about undergraduates or prospective undergraduates. With this data as background, we then look at mathematical and computer science student data from this Survey. For the reader's convenience, we have organized much special data about computer science as a separate and later Chapter 4.

Since 1970, full-time undergraduate enrollments in all higher education (including two-year colleges) have increased by $20 \%$ and part-time enrollments have more than doubled. Overall FTE (full-time equivalent) enrollments have increased by $30 \%$. Much of this increase has been at the two-year college level. Graph 1-A gives the full-time, part-time, and FTE enrollments over time.

GRAPH 1 - A

UNDERGRADUATE ENROLLMENTS IN HIGHER EDUCATION SINCE 1970
(In Thousands)


| FTE Equiv. | 6,035 | 7,433 | 7,843 | 7,860 |
| :--- | :--- | :--- | :--- | :--- |
| Full-time | 5,280 | 6,169 | 6,362 | 6,320 |
| Part-time | 2,096 | 3,510 | 4,113 | 4,277 |

Based on reports from various institutions, Department of Education sources use a part-time student enrollment as equivalent to $36 \%$ of a full-time enrollment. Over the period 1970-1985, the total increase in overall FTE undergraduate enrollments was 30\%. By comparison undergraduate student course enrollments in the mathematical and computer sciences in all of higher education increased by $76 \%$ from 1970 to 1985. Even with all computer science enrollments deleted, the increase in undergraduate enrollments in mathematical sciences from 1970 to 1985 was over 50\%. And 1970, the base year, was at the end of a boom period in science in the 1960's. These figures clearly show a rapidly increasing
role for both the mathematical and computer sciences in higher education.
Looking only at the four-year college and university sector, overall FTE enrollments increased about 16\% in the period from 1970 to 1985 and mathematical sciences enrollments (not counting computer science enrollments) increased $40 \%$, (From Tables 1-2 and 1-10). This occurred over a period when almost the entire growth of the combined mathematics and computer science faculty since 1970 has been concentrated in computer science (Table 2-5).

## PROBABLE MAJORS OF ENTERING FRESHMEN IN HIGHER EDUCATION

Table 1-1 below shows the trend over time of the choices of academic majors in a number of disciplines. The data comes from The American Freshman: National Norms for Fall 1985 by Astin, A. W., King, M. R. and Richardson, G.T. and earlier editions of this report. The trends in the various disciplines shown seem to conform to conventional wisdom. It is encouraging that the "mathematics and statistics" category appears to have "bottomed out". Among the "hard" sciences and engineering, only the mathematical sciences show an upswing, albeit mild, since 1980.

TABLE 1-1

## PERCENTAGES OF ENTERING FRESHMEN PLANNING MAJORS IN SELECTED DISCIPLINES

|  | 1965 | 1970 | 1975 | 1980 | 1985 |
| :--- | ---: | ---: | ---: | ---: | ---: |
| Business | 14.3 | 16.2 | 18.9 | 23.9 | 26.8 |
| Education | 10.6 | 11.6 | 9.9 | 7.7 | 7.1 |
| Engineering | 9.8 | 8.6 | 7.9 | 11.8 | 10.7 |
| Humanities \& Arts | 24.3 | 21.1 | 12.8 | 8.9 | 8.3 |
| Mathematics \& Statistics | 4.5 | 3.2 | 1.1 | 0.6 | 0.8 |
| Physical Science | 3.3 | 2.3 | 2.7 | 2.0 | 1.6 |
| Social Sciences | 8.2 | 8.9 | 6.2 | 6.7 | 7.6 |
| Computer Science | - | - | - | 2.5 | 2.3 |
| Data Proc. and Comp. Prog. | - | - | - | 2.4 | 2.1 |

The 1986 figures for computer science and for data processing and computer programming were $1.9 \%$ and $1.6 \%$. The profiles on "first choices of intended specific fields of study of college bound seniors" prepared annually for the College Board and involving responses from some million high school seniors show somewhat similar patterns and trends. In mathematics and statistics, the figures from 1975, 1980 and 1985 are 2.4, 1.1 and 1.1 respectively. However, the overall computer science and systems analysis figures for the same years were 2.8, 4.2 and 7.2.

TOTAL MATHEMATICAL AND COMPUTER SCIENCE ENROLLMENTS SINCE 1970

Graph 1-B gives total undergraduate enrollments in the mathematical and computer sciences in two-year colleges and in the four-year colleges and universities. The growth can be compared to that of all undergraduate enrollments shown in Graph 1-A and to that of faculty growth shown in Table 2-2.

TOTAL MATHEMATICAL AND COMPUTER SCIENCE ENROLLMENTS IN HIGHER EDUCATION (In Thousands)

$197019751980 \quad 1985$
All Higher Educ. 1,970 2,371 3,043 3,421
4-Yr. Col./Univ. 1,386 1,497 1,995 2,387
2-Yr. College $584 \quad 874$ 1,048 1,034

## UNDERGRADUATE MATHEMATICS ENROLLMENTS OVER TIME

From the earlier Surveys and a Department of Education Report of 1960 authored by Clarence Lindquist (who also did the basic statistical work for the 1965 to 1980 Surveys) we see some interesting changes over time in undergraduate enrollments. We look first at mathematics course enrollments by levels of courses and separately at statistics and computer science. In Table 1-2 we give course enrollments by four categories A: Remedial (courses 1-4); B: Other pre-calculus (courses 5-14); C: Calculus level (courses 15-19); and D: Advanced (courses 20-44). The comparable long term trend data for statistics is in Table 1-11 and for computer science is in Table 4-10. See Appendix B or E for the course numbers and titles. We use the course designations and numbers from the
present Survey and adapt the course lists from the earlier Surveys to fit the present list. We used the lists on page 28 of the 1975 Survey report for the 1960-1970 data. It is necessary to make some arbitrary decisions, e.g. general mathematics (basic skills, operations) is regarded as a remedial course, $A$, even though it was not previously listed that way; mathematics for elementary school teachers is regarded as B even though it was sometimes listed as an upper division course; linear algebra (now listed in $C$ as 19) and in $D(a s 34)$ earlier was listed only once and thus enrollments had to be arbitrarily apportioned. Computer science courses have changed in name and level rather dramatically, thus forcing some arbitrary decisions. But the general trends are rather clearcut.

TABLE 1-2

ENROLLMENTS IN VARIOUS LEVELS OF MATHEMATICS COURSES
(in Thousands)

|  | 1960 | 1965 | 1970 | 1975 | 1980 | 1985 |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: |
| A: Remedial | 96 | 89 | 101 | 141 | 242 | 251 |
| B: Other pre-calc. | 349 | 468 | 538 | 555 | 602 | 593 |
| C: Calculus level | 180 | 315 | 414 | 450 | 590 | 637 |
| D: Advanced | $\underline{92}$ | $\underline{133}$ | $\underline{162}$ | $\frac{106}{1215}$ | $\frac{91}{1525}$ | $\frac{138}{1619}$ |

Roughly speaking, A represents high school mathematics taught in college, $B$ represents other freshmen level mathematics at a level below calculus, $C$ represents the first two years of mathematics for those able to start with calculus, and $D$ represents upper division mathematics. It should be noted that a great deal of elementary statistics and computer science is also taught in mathematics departments. Thus figures in Table 1-2 and in Table 1-3 below do not represent departmental teaching loads but levels of mathematics courses taken. Below we give the percentages of mathematics courses taken at various levels over time obtained from Table 1-2 above.

TABLE 1-3

PERCENTAGES OF ENROLLMENTS IN VARIOUS LEVELS OF MATHEMATICS
$\begin{array}{llllll}1960 & 1965 & 1970 & 1975 & 1980 & 1985\end{array}$

| A: | Remedial | $13 \%$ | $9 \%$ | $9 \%$ | $11 \%$ | $16 \%$ |
| :--- | :--- | ---: | ---: | ---: | ---: | ---: |
| B: | Other pre-calc. | $49 \%$ | $46 \%$ | $45 \%$ | $44 \%$ | $39 \%$ |
| C: Calculus level | $24 \%$ | $29 \%$ | $34 \%$ | $36 \%$ | $39 \%$ | $39 \%$ |
| D: Advanced | $14 \%$ | $16 \%$ | $12 \%$ | $9 \%$ | $6 \%$ | $9 \%$ |

There has been a small but encouraging increase $i n$ the sum of $C$ and $D$ from $45 \%$ in 1965 to $48 \%$ in 1985. The big jump in remedial enrollments for 1975-80 occurred at a time of the development of specially funded federal programs designed to get colleges and universities to address remediation issues and was accompanied by an equally large reduction in the percentage of enrollments in other pre-calculus mathematics. In that light, this change was merely a shift downward from other pre-calculus courses to remedial--perhaps a reflection of both falling student entrance test scores at the lower levels and more faculty attention to that problem.

Since most undergraduate statistics courses taught in mathematical science departments are taught in the (primary) mathematics department, it is reasonable to look at the total mathematics and statistics undergraduate load over time. The detailed (and explosive) growth in statistics enrollments, per se, is given in Table 1-11. Combining mathematics and statistics enrollments in the two categories of (1) pre-calculus and (2) calculus-and-beyond we have the following phenomena.

## TABLE 1 - 4

COMBINED MATHEMATICS AND STATISTICS ENROLLMENTS BY LEVEL
$19651970 \quad 1975 \quad 1980 \quad 1985$

## Pre-Calculus Courses

1-14, 45, 46
54\%
54\%
57\%
$57 \%$
54\%
Calculus and Beyond
15-44, 47-54
46\%
46\%
43\%
43\%
46\%

The 1960 figures were $61 \%$ and $39 \%$ making the detailed data from that original study somewhat suspect in light of this almost constant distribution of course load by level.

Since computer science as a subject has developed only within the past 25 years, there has, of course, been phenomenal growth in computer science enrollments over that period. The time trends for computer science are given in Table 4-10.

In Table 1-5, we give the enrollments in four-year colleges and universities over time in several specific mathematics courses.

TABLE 1 - 5

## ENROLLMENTS OVER TIME IN SOME SPECIFIC MATHEMATICS COURSES (in Thousands)

| Subject | 1960 | 1965 | 1970 | 1975 | 1980 | 1985 |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: |
|  |  |  |  |  |  |  |
| Arith./Gen. Math. | 48 | 29 | 23 | 32 | 63 | 45 |
| H.S. Alg. \& Geo. | 48 | 60 | 78 | 109 | 179 | 202 |
| Lib. Arts Math. | 36 | 87 | 74 | 103 | 63 | 59 |
| Math for Elem. Teachers | 23 | 61 | 89 | 68 | 44 | 54 |
| Coll. Alg., Trig. | 235 | 262 | 301 | 259 | 345 | 352 |
| Finite Math. | 1 | 7 | 47 | 74 | 95 | 88 |
| Anal. Geo. \& Calc. | 184 | 295 | 345 | 397 | 517 | 534 |
| Diff. Equations | 29 | 31 | 31 | 29 | 45 | 45 |
| Linear/Matrix Alg. | 4 | 19 | 47 | 28 | 37 | 47 |
| Adv. Calc. | 17 | 20 | 20 | 14 | 11 | 14 |
| Other Undergrad. Math. | $(94)$ | $(134)$ | $(160)$ | $(139)$ | $(126)$ | $(179)$ |
| $\quad$ Total Math. |  |  |  |  |  |  |
| $\quad$ Enrollment | 717 | 1005 | 1215 | 1252 | 1525 | 1619 |
| $\quad$ (Stat. \& C.S. |  |  |  |  |  |  |

UNDERGRADUATE ENROLLMENTS IN THE MATHEMATICAL AND COMPUTER SCIENCES FOR 1980 AND 1985

In Table 1-6A, we give 1980 and 1985 enrollments for various course levels in mathematics, statistics, and computer science and in Table 1-6B we give the separate totals for all undergraduate mathematics, statistics and computer science in these years.

TABLE $1-6 \mathrm{~A}$

1980 AND 1985 MATHEMATICS, STATISTICS AND COMPUTER SCIENCE ENROLLMENTS BY LEVELS IN UNIVERSITIES \& PUBLIC \& PRIVATE FOUR-YEAR COLLEGES* (In Thousands)**

19801985

|  | Univ. | Pu. | Pr. | Total | Univ. | Pu. | Pr. | Total | Ch. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Remedial math. | 63 | 151 | 28 | 242 | 56 | 155 | 40 | 251 | +4\% |
| Other pre-calc. | 214 | 261 | 127 | 602 | 200 | 280 | 113 | 593 | -1\% |
| Calc. level | 282 | 175 | 133 | 590 | 281 | 258 | 101 | 637 | +8\% |
| Adv. level math. | 28 | 29 | 32 | 91 | 47 | 66 | 25 | 138 | +52\% |
| Elem. stat./prob. | 33 | 48 | 23 | 104 | 52 | 54 | 39 | 144 | +38\% |
| Adv. stat. | 25 | 13 | 6 | 43 | 37 | 18 | 10 | 66 | +53\% |
| Lower level C.S. | 69 | 77 | 60 | 206 | 94 | 155 | 101 | 350 | +70\% |
| Middle level C.S. | 12 | 14 | 8 | 35 | 18 | 34 | 13 | 66 | +89\% |
| Upper level C.S. | 30 | 35 | 19 | 80 | 54 | 61 | 28 | 142 | +78\% |
| Total | 756 | 803 | 434 | 1993 | 839 | 1081 | 470 | 2387 | 20\% |

The enrollment figures above show that remediation is still a major but not a significantly growing problem. The increase in advanced level math enrollments was fairly evenly spread over all types of courses: core math, math for secondary school teachers and applied math.

The statistics figures are for enrollment in the mathematical and computer sciences type departments not in psychology, education, business, etc.

The list of computer science courses did not include data processing per se (at an elementary level) but a small number of data processing enrollments might have appeared in an "other" category.

[^0]TABLE 1 - 6B

TOTAL 1980 AND 1985 UNDERGRADUATE ENROLLMENTS IN MATHEMATICS, STATISTICS AND COMPUTER SCIENCE*
(In Thousands)**

|  | 1980 |  |  |  | 1985 |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Univ. | Pu. | Pr. | Total | Univ. | Pu. | Pr. | Total |
| Mathematics | 587 | 616 | 320 | 1525 | 584 | 759 | 279 | 1619 |
| Statistics | 58 | 61 | 29 | 148 | 89 | 72 | 49 | 208 |
| Computer Science | 111 | 126 | 85 | 322 | 166 | $\underline{250}$ | 142 | 558 |
| Total | 756 | 803 | 434 | (1993) | 839 | 1081 | 470 | (2387) |

* It should be noted, as remarked in the Introduction to this report, that enrollments as well as faculty data in the university, public college and private college categories are not directly comparable to the AMS Survey Groups I, II, \& III; M; and B categories. The Dept. of Education lists of institutions for the three categories from which the Survey samples were drawn have considerable but not total overlap with the AMS lists of departments. A comparison of the Survey and AMS lists suggest that total mathematics enrollments in the Survey "university" category should be marginally lower than enrollments in Groups I, II, \& III departments.
** The course-by-course enrollments are given in Appendix E. To maximize the accuracy of primary published data, they were individually rounded to the nearest thousand. This process led to some total enrollments being different from the sum of the addends, e.g. $1.3+2.3+$ $3.3=6.9$ rounds to $1+2+3$ which is not 7 . Consequently, the numbers in Tables $1-6 \mathrm{~A}$ and $1-6 \mathrm{~B}$ do not always sum correctly to the last digit.


## AVAILABILITY OF SELECTED UPPER LEVEL MATHEMATICAL COURSES IN UNIVERSITIES AND FOUR-YEAR COLLEGES IN 1985

In the 1985 questionnaire, departments were asked to report on whether particular courses were being offered in the academic year 1985-86 or had been offered in the academic year 1984-85. In previous surveys, the question did not contain the reference to the preceding year. The Survey Committee felt that because many advanced courses are only offered on a two-year cycle, particularly in smaller institutions, the proper reference frame on availability should cover a two-year cycle. It turned out that with this revised wording asking for the availability of courses over two years, there were much higher percentages of institutions offering various upper level courses. The Survey committee believes that this year's data more accurately represents the status of course availability. Twenty-one out of the thirty percentages below are about half again as high as those reported in 1980.

TABLE 1-7

## PERCENTAGE OF INSTITUTIONS OFFERING SELECTED COURSES <br> IN 1984-85 OR 1985-86

|  | Course | Univ. | Pu.4-Yr. | Pr.4-Yr. |
| :---: | :---: | :---: | :---: | :---: |
| 1) | Theory of Numbers | 65\% | 56\% | 20\% |
| 2) | Combinatorics | 63\% | 22\% | 5\% |
| 3) | Foundations of Mathematics | 27\% | 30\% | 17\% |
| 4) | Set Theory | 33\% | 24\% | 3\% |
| 5) | History of Mathematics | 42\% | 39\% | 9\% |
| 6) | Geometry | 79\% | 77\% | 47\% |
| 7) | Math. for Sec. Sch. Teachers | 45\% | 55\% | 40\% |
| 8) | Mathematical Logic | 35\% | 19\% | 12\% |
| 9) | Applied Math./Math. Model. | 51\% | 37\% | 26\% |
| 10) | Operations Research | 44\% | 33\% | 26\% |

## AVERAGE SECTION SIZE AT VARIOUS COURSE LEVELS

From the main questionnaire on course enrollments and numbers of sections, we are able to get the following information:

- The average section size in remedial mathematics is about 32 with intermediate algebra sections a bit larger and arithmetic and general mathematics sections a bit smaller.
- The average section size in other pre-calculus mathematics is 35 with each course having an average section size within 3 of that number except for business mathematics with 43, finite mathematics with 39 , and mathematics for elementary school teachers with 29.
- The average section size in calculus-level courses is 34 with calculus for biological, social and management sciences at 40 and discrete mathematics and linear/matrix algebra just under 30.
- The average section size for advanced level courses in mathematics is 19.
- In statistics, at the elementary (freshman) level the average section size is 37 and at the advanced level is 30.
- For the lower, middle and upper level courses in computer science the average section sizes are 31,26 , and 22 respectively.


## BACHELORS DEGREES IN THE MATHEMATICAL AND COMPUTER SCIENCES

Three different types of data are given in the tables below: in Table 1-8, the overall numbers of bachelors degrees in various specialties for the twelve months ending on June 30 of 1975, 1980 and 1985; in Table 1-9, the 1984-1985 numbers of bachelors degrees by type of departinent; and in Table 1-10, the 1984-1985 bachelors degrees reported by mathematics departments and tabulated by category of institution. Together these tables and accompanying comments give an interesting picture of undergraduate major programs. The reader is also referred to Table 1-13 and Table 4-11 for separate data relevant to statistics and computer science degree programs.

The numbers given below include only the given institution's majors in mathematics, computer science or statistics departments (by whatever name it is called). There were eight other mathematical science departments of various special descriptions whose data were submitted in the Survey. But the total number (eight) of such departments divided among various strata for sampling was too small to make meaningful projections to national totals of undergraduate degrees for such types of departments. Those eight departments reported a total of 320 degrees. Thus the counts of degrees given in this Survey may be a bit low, particularly in some of the specialty areas.

The numbers of bachelors degrees in the mathematical and computer sciences took a major leap in the five year period from 1980 to 1985, with computer science degrees more than tripling and, when joint majors are included, overall mathematics degrees increasing toward the 1974-75 levels. The current Survey asked for counts of joint majors as well as for individual majors for the period July 1984 to June 1985. In earlier Surveys, such joint majors would presumably have been counted as degrees only in the field of the department in which they studied.

The recent 1985-86 Taulbee Survey of the Computer Science Board indicates a cessation of growth in the number of computer science undergraduate degrees. Recent AMS Surveys indicate a modest reduction in computer science enrollments.

TABLE 1 - 8

## NUMBERS OF BACHELORS DEGREES

| Special Area | 1974-75 | 1979-80 | 1984-85 |
| :---: | :---: | :---: | :---: |
| Mathematics (General) | 17,713 | 10,160 | 12,102 |
| Applied Mathematics | 1,120* | 1,527* | 1,215 |
| Math. Education | 4,778 | 1,752 | 2,567 |
| Computer Science | 3,636 | 8,917 | 29,107 |
| Statistics | 570 | 467 | 538 |
| Operations Res. | --- | --- | 312* |
| Joint C.S. \& Mathematics | --- | --- | 3,084 |
| Joint Math. \& Statistics | --- | --- | 121 |
| Joint C.S. \& Statistics | --- | -- | 157 |
| Total | 27,817 | 22,823 | 49,203 |

* The applied mathematics categories in 1974-75 and 1979-80 include figures from the small categories "actuarial science" and "other" not included in this year's questionnaire. However, the additional "operations research" category this year presumably would have been included under "other" or "applied mathematics" in earlier years. The counts of joint majors are in addition to the separate individual listings for mathematics, computer science or statistics majors since the total number of "bachelors degrees awarded by your department" was specifically asked for.

The $50 \%$ increase in the number of bachelors degrees in mathematics education since 1980 is encouraging. It should be noted that the questionnaire was sent to mathematics departments, per se, and in many universities and some public colleges, mathematics education students are handled separately by colleges or departments of education rather than by mathematics departments. Thus the figures cited are understood to be incomplete as counts of the total number of secondary education graduates
in mathematics. However, the trend data should be meaningful since the counts over time are comparable.

The actual number of degrees in the mathematical sciences including joint majors but not including computer science or mathematics education as such has gone from 19,403 in 1974-75 to 12,154 in 1979-80 to 17,529 in 1984-85. The increase since 1979-80 was about $44 \%$.

The totals of mathematics, statistics and computer science degrees may be compared with Department of Education figures for the July 1984 to June 1985 period which show 15,146 mathematics degrees (including 371 statistics majors) and 38,878 computer and information science majors. With some uncertainties as to how to classify some applied mathematics degrees and whether (all?) information science degrees would have been counted in the CBMS Survey, the figures appear to be generally consistent with Survey data.

Recent data from the 1986 AMS Survey which counts majors in school for the junior-senior years show a slight decrease in such majors in the mathematical sciences over the past year and a larger decrease in computer science majors over that period.

## THE DISTRIBUTION OF BACHELORS DEGREES GRANTED IN 1984-85 AMONG VARIOUS TYPES OF DEPARTMENTS

Table 1-9 below gives the distribution of majors by type of department. It should be noted that "Mathematics Departments" is the catch-all category for universities or colleges which do not have separate statistics or computer science departments; such mathematics departments normally perform (part of) the functions of departments in those disciplines.

## TABLE 1 - 9

NUMBERS OF BACHELORS DEGREES BY TYPE OF DEPARTMENT, JULY 1984-JUNE 1985

|  | Math Dept. | C.S. Dept. | Stat. Dept. | Total |  |
| :--- | ---: | ---: | ---: | ---: | ---: |
|  |  |  |  |  |  |
| Mathematics (general) | 11,956 | 146 | 0 | 12,102 |  |
| Applied Mathematics | 1,215 | 0 | 0 | 1,215 |  |
| Math. Education | 2,567 | 0 | 0 | 2,567 |  |
| Computer Science | 8,646 | 20,416 | 45 | 29,107 |  |
| Statistics | 212 | 0 | 326 | 538 |  |
| Operations Res. | 302 | 0 | 10 | 312 |  |
| Joint Mathematics \& C.S. | 2,519 | 565 | 0 | 3,084 |  |
| Joint Math. \& Statistics | 102 | 0 | 19 | 121 |  |
| Joint C.S. \& Statistics | 2 | 148 | 7 | 157 |  |
|  |  |  |  |  |  |
| Total | 27,521 | 21,275 | 407 | 49,203 |  |

There are several items in the table worthy of note. As expected, all mathematics education degrees are from mathematics departments. About $82 \%$ of joint mathematical and computer science majors are reported by mathematics departments. The development of computer science major programs within mathematics departments must be preceded by extensive course programs in computer science. Thus although the number of computer science sections taught in mathematics departments is almost the same as in computer science departments, we should not expect mathematics departments to produce as many computer science degrees as do computer science departments.

In Table 1-10, numbers of bachelors degrees in mathematics departments are shown by type of institution. For comparison purposes, the total FTE Faculty Size (Full-time plus $1 / 3$ Part-time) is given in the bottom line. It gives partial support to the common belief that private colleges, with their attention to undergraduates, do turn out
proportionately somewhat more bachelors degrees in the mathematical sciences. It is not clear whether the computer science category should be included in such comparisons. In any event, the non-existence of competing engineering and various specialty degree programs in private colleges presumably contributes to the observed differences. Note how applied mathematics degrees are concentrated in universities and public colleges and mathematics education degrees in the colleges. However as noted above, in some universities and public colleges, mathematics education degrees are the province of colleges or schools of education and thus are not included in the counts given. The higher incidence of separate computer science departments in universities presumably accounts for the smaller number of computer science degrees in university mathematics departments.

TABLE 1 - 10

1984-85 BACHELORS DEGREES FROM MATHEMATICS DEPARTMENTS BY CATEGORY OF SCHOOL FOR VARIOUS DEGREE TYPES

|  | Univ. | Pu. 4-Yr. | Pr. 4-Yr. | Total |
| :---: | :---: | :---: | :---: | :---: |
| Mathematics (general) | 3,467 | 4,277 | 4,212 | 11,956 |
| Applied Mathematics | 624 | 537 | 54 | 1,215 |
| Mathematics Educ. | 324 | 1,376 | 867 | 2,567 |
| Computer Science | 1,865 | 3,175 | 3,606 | 8,646 |
| Statistics | 115 | 97 | 0 | 212 |
| Operations Research | 259 | 43 | 0 | 302 |
| Joint C.S. \& Math | 605 | 1,102 | 811 | 2,519 |
| Joint Math. \& Stat. | 25 | 77 | 0 | 102 |
| Joint C.S. \& Stat. | 0 | 2 | 0 | 2 |
| Total | 7,284 | 10,686 | 9,551 | 27,521 |
| FTE Faculty Total Size (for comparison purposes) | 5,681 | 8,866 | 5,664 |  |

See Table 4-11 for a separate breakdown of degrees from computer science departments by category of institution. See the Introduction for a discussion indicating that the categories are not directly comparable to AMS Survey Group I, II \& III; Group M; and Group B.

## STATISTICS AS AN UNDERGRADUATE SUBJECT

The data generally cited elsewhere but organized below gives much information about undergraduate statistics. Enrollments in statistics in departments of the mathematical and computer sciences has grown rapidly over the past twenty-five years, at both elementary and advanced levels. We classify probability as a part of statistics for this purpose. Total enrollments in probability courses themselves are quite small and some include a probability and statistics designation. See Appendix $B$ or $E$ for Course titles.

TABLE 1 - 11

UNDERGRADUATE ENROLLMENTS IN STATISTICS OVER TIME (in Thousands)
$1960 \quad 1965 \quad 1970 \quad 1975 \quad 1980 \quad 1985$

Elem. Stat./Prob.
Courses 45, 46
4
11
57
99
104
144
Adv. Stat./Prob.
Courses 47-54
Total
16
20
32
35
42
43
64
43
92
141
147
208

We may conjecture on various reasons for the continuing impressive growth of undergraduate statistics enrollments:
(1) The increasing quantification of society, causing numerical data, its collection, use, analysis and interpretation to be much more widespread.
(2) The developing computer age which underlies much of (1) above.
(3) The increasing student choice of business as a major subject and the computerization and quantification of the whole business community resulting in statistics and probability and their applications becoming an integral part of the business curriculum.

The distribution of types of statistics courses among universities, public colleges and private colleges is revealed in Table 1-12. (See Appendix $E$ for individual course enrollments).

TABLE 1 - 12

## 1985 STATISTICS COURSE ENROLLMENTS BY CATEGORY OF INSTITUTION (in Thousands)

Univ. Pu. 4-Yr. Pr. 4-Yr. Total

| Elem. Stat./Prob. <br> (No Calc. prereq. 45, 46) | 52 | 54 | 39 | 144 |
| :--- | :---: | :---: | :---: | :---: |
| Math. Stat./Prob. <br> (Calculus prereq. 47, 48) | 17 | 14 | 9 | 39* |
| Other Stat. Courses <br> (49-54) | 20 | 4 | 1 | 25 |

[^1]The distribution of elementary courses is roughly proportional to the distribution of pre-calculus non-remedial courses in mathematics departments except that the public four-year college figure above is too low. But as the courses get more specialized, the colleges show relatively low course enrollments. With the courses 47-54 lumped together the enrollments are roughly proportional to the numbers of statisticians on the three faculties (see Table 2-12).

The numbers of degrees in statistics has been reported by the Survey only for 1974-75, 1979-80, and 1984-85.

TABLE 1 - 13

NUMBERS OF STATISTICS UNDERGRADUATE DEGREES OVER TIME

$$
\begin{array}{ccc}
1974-75 & 1979-80 & 1984-85 \\
570 & 467 & 816
\end{array}
$$

The figure 816 is from 538 reported as statistics majors, 121 as joint mathematics and statistics majors and 157 as joint computer science and statistics majors. Of these 278 joint majors only 26 were from statistics departments. Thus, since in previous Surveys there was no place to list joint majors, it seems very likely that in earlier years almost all joint majors in statistics would have been listed only as mathematics or computer science majors. Of the 538 statistics degrees, 326 were from statistics departments and 212 from mathematics departments. In addition, mathematics departments produced 302 operations research degrees and statistics departments produced 10. Statistics departments also produced 45 computer science majors. The total number of degrees reported by statistics departments was 407 with mathematics departments reporting another 514 in statistics or operations research. Thus with other joint statistics majors, there were 1,173 majors with a very large dose of statistics. Unfortunately, the available data from the earlier surveys does not give us a basis for a comparison of these latter numbers over time.

For information on statisticians on the faculty, see Table 2-12.

## REMEDIAL MATHEMATICS

Table 1- 14 below shows the enrollments in the four remedial courses since 1975 in the various categories of institutions.

TABLE 1 - 14

ENROLLMENTS OVER TIME IN REMEDIAL COURSES BY CATEGORY OF INSTITUTIONS (in thousands)

Univ.
Arith. Gen. Math. Elem. Alg. Inter. Alg.

1975
1980
1985
Pu. 4-Yr.
1975
1980
1985
Pr. 4-Yr.
1975
1980
1985
Pu.
---- ----
$\begin{array}{ccc}---- & 4\end{array}$
13
15
$23 \quad 22$
46
54
52
26
44
36

| 5 | 23 | 22 | 46 |
| ---: | :--- | :--- | :--- |
| 11 | 37 | 54 | 48 |
| 8 | 18 | 52 | 77 |

1
1
4
500

With remedial mathematics courses playing an important role in many departments' instructional and faculty loads, a special one-page supplemental questionnaire on remediation was sent to all sampled mathematics departments. The response rate was noticeably less than the response rate from four-year college and university mathematics
departments and thus the data below is not as reliable as the rest of the data. The reader is referred to other parts of this chapter and to Appendix $E$ for additional enrollment and trend data on remedial mathematics.

Remedial mathematics was not explicity defined but in the four-year college and university questionnaires the courses listed as remedial (high school) were arithmetic, general math (basic skills), elementary algebra and intermediate algebra (high school). The data cited below are summaries from all responses considered together without regard to type of institution and without projecting by strata to the total population.
a) $19 \%$ of the academic units administering the remedial programs were outside the mathematics department.
b) $34 \%$ of the units handling remediation reported follow-up studies on success rates of students.
c) $35 \%$ of the faculty are full-time with $36 \%$ of the full-time faculty being tenured and another $30 \%$ on tenure track.
d) $18 \%$ of the combined full- and part-time faculty staffing the remedial program have doctorates with an additional $49 \%$ having master's degrees. Of the doctorates, $27 \%$ have their degrees in mathematics education and $19 \%$ have their degrees outside mathematics or mathematics education.
e) Course load credit practices varied from $65 \%$ giving credit in arithmetic to $90 \%$ in intermediate algebra (high school).
f) Credit-toward-graduation practices varied from $10 \%$ for arithmetic to $61 \%$ for intermediate algebra (high school). However, the question was worded, "Is credit toward graduation given", with "yes" and "no" boxes to check. Thus if credit were given only in some very special curricula or under special circumstances such as a student not having high school credit for the course, the
"yes" box would presumably have been checked. It is known from other sources that, in many institutions, majors in mathematics, engineering or physical science receive no credit toward graduation for any course below calculus.
g) The percentage of all remedial sections taught by part-time faculty varied from 34\% in intermediate algebra to about $45 \%$ in each of arithmetic, general mathematics (basic skills) and elementary algebra.

## CHAPTER 2

## FOUR-YEAR COLLEGE AND UNIVERSITY FACULTY CHARACTERISTICS

This chapter deals with characteristics of those faculty teaching mathematics, statistics and computer science. In Chapter 4, there is considerable additional information on the faculty teaching computer science. And Chapter 3 includes some data on instructional methods, on computer usage, and on teaching assistants. See Chapter 6 for two-year college faculty characteristics.

TERMINOLOGY USED FOR FOUR-YEAR COLLEGE AND UNIVERSITY FACULTY

The mathematics (departmental) faculty refers to all members of the nation's mathematics departments. The statistics (departmental) faculty refers to all members of statistics departments separate from mathematics departments. The mathematical sciences (departmental) faculty refers to the combined mathematics and statistics (departmental) faculties. The computer science (departmental) faculty refers to all members of separate computer science departments. Thus it is disjoint from the mathematical sciences departmental faculty. The total computer science faculty refers to the computer science departmental faculty together with all members of the mathematical sciences departmental faculty who taught at least one computer science course in their own department in fall 1985. Members are full- or part-time in this total faculty according as they taught computer science full- or part-time.
Any FTE (full-time equivalent) faculty size is computed as the size of the full-time faculty plus one-third the size of the part-time faculty. The references to the mathematical and computer science faculty in higher education refer to the combined two- and four-year college and university faculty.

- The full-time faculty in the mathematical and computer sciences grew by $21 \%$ in the period 1980-1985 and now numbers 22,194 while the part-time faculty grew by $46 \%$ to 9,189 .
- Since 1970, the FTE (full-time equivalent) faculty of all those teaching in the mathematical sciences in four-year colleges and universities increased by $6 \%$ while the course enrollments in the mathematical sciences increased by $41 \%$. In the same period, the overall FTE faculty in the mathematical and computer sciences grew by $40 \%$ while course enrollments grew by $72 \%$.
- The total computer science faculty (i.e. teachers of computer science) is now 5,651 full-time ( 3,605 in computer science departments), 5,342 part-time (1,984 in computer science departments) for a total 7,432 FTE, up from an estimated 1,182 FTE in 1970.
- The percentage of doctorates among the full-time faculty in the mathematical and computer sciences has decreased from $82 \%$ in 1975 to $73 \%$ in 1985 in the overall four-year college and university category.
- The percentages of tenured faculty in the mathematical and computer sciences have decreased to $66 \%, 54 \%$ and $49 \%$ in the university, public four-year college and private four-year college categories while the non-tenured non-doctorate full-time faculty percentages have increased to $7 \%, 17 \%$ and $28 \%$ respectively.
- The net outflow (outflow minus inflow) of the mathematical sciences faculty to industry, business and government was about $1 / 2 \%$ of the total faculty in 1984-1985.
- Teaching load assignments generally are similar to those in 1970. Typical computer science and statistics faculty teaching assignments are less than those for mathematics faculty.
- Of all sections taught by full-time and part-time faculty, full-time professorial level (assistant to full) faculty teach about two-thirds, other full-time faculty teach about one-seventh, and part-time faculty teach the rest (almost one-fifth). GTA's teach about $20 \%$ of all sections in universities and under $10 \%$ in public four-year colleges.


## FACULTY IN HIGHER EDUCATION

In Table 2-1 we give data on faculty size for all of higher education (from Department of Education publications: Digest of Educational Statistics and Projections of Educational Statistics).

In Table 2-2 we give the comparable data on faculty size for the mathematical and computer sciences combined (from the CBMS Survey). The totals for both tables refer to so-called "senior" faculty including those at the instructor or comparable level but not including graduate assistants.

TABLE 2-1

## FULL- AND PART-TIME FACULTY AND FTE's IN HIGHER EDUCATION

 (In Thousands)|  | 1970 | 1975 | 1980 | 1985 |
| :--- | ---: | ---: | ---: | ---: |
| Full-time | 369 | 440 | 458 | 456 |
| Part-time | 104 | 188 | 236 | 254 |
| Full-time Equivalents | 402 | 501 | 538 | 534 |
|  |  |  |  |  |
| 4-Yr. Coll. \& Univ. FTE | 333 | 397 | 420 | $409 *$ |
| 2-Yr. College FTE | 68 | 104 | 118 | $124 *$ |

[^2]TABLE 2-2

## FULL-, PART-TIME AND FTE FACULTY IN THE MATHEMATICAL AND COMPUTER SCIENCES IN HIGHER EDUCATION

23,927
28,471
Full-time
Part-time
FTE

4-Yr. Coll. \& Univ. FTE
2-Yr. College FTE

1970

21,922
22,807
1975

5,042
23,603

17,986
5,617

18,062
7,081
20,409
25,257
8,755

While the overall FTE faculty in higher education has increased $33 \%$ since 1970, the mathematics and computer science faculty has increased by 44\%. However in the same period, the FTE enrollments in higher education have gone up $30 \%$ (see Graph 1-A) while enrollments in the mathematical and computer sciences have gone up $74 \%$ (see Graph 1-B). Thus over the period 1970-1985 there has been a serious deterioration in the relative size of the overall mathematical and computer science faculty.

FACULTY SIZE TRENDS IN THE MATHEMATICAL AND COMPUTER SCIENCES

The faculty size changes in various categories of institutions and types of departments are shown in Tables 2-3 and 2-4. The 1985 figures generally agree with AMS Survey figures when allowances are made for known differences in the composition of the different sets of categories used. See the Introduction for more discussion of this issue.

TABLE 2 - 3

DEPARTMENTAL FACULTY SIZES IN FOUR-YEAR COLLEGES AND UNIVERSITIES

|  | 1970 |  | 1975 |  | 1980 |  | 1985 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Full | Part | Full | Part | Ful1 | Part | Full | Part |
| Universities |  |  |  |  |  |  |  |  |
| Math. Dept. | 6235 | 615 | 5405 | 699 | 5605 | 1038 | 5333 | 1044 |
| Stat. Dept. | 700 | 93 | 732 | 68 | 610 | 132 | 662 | 103 |
| C.S. Dept. | 688 | 300 | 987 | 133 | 1236 | 365 | 1448 | 491 |
| Public Colleges |  |  |  |  |  |  |  |  |
| Math. Dept. | 6068 | 876 | 6160 | 1339 | 6264 | 2319 | 7754 | 3337 |
| Stat. Dept. |  |  |  |  |  |  | 78 | 15 |
| C.S. Dept. |  |  |  |  | 436 | 361 | 1554 | 862 |
| Private Colleges |  |  |  |  |  |  |  |  |
| Math. Dept. | 3352 | 945 | 3579 | 1359 | 4153 | 2099 | 4762 | 2706 |
| C.S. Dept. |  | A |  | A |  | A | 603 | 631 |
| TOTAL | 17,043 | 2,829 | 16,863 | 3,598 | 18,304 | 6,314 | 22,194 | 9,189 |

The data above show a $21 \%$ increase in the overall full-time mathematical and computer science four-year college and university faculty and a 46\% increase in the part-time faculty from fall 1980 to fall 1985. These faculty increases occurred when the mathematical and computer science student enrollments, Table 1-6A, were increasing by $20 \%$. Thus the period from 1980 to 1985 has seen our faculty size slightly more than keep up with student enrollments.

In Table 2-4, we give the same counts summed different ways.

MATHEMATICS, STATISTICS AND COMPUTER SCIENCE DEPARTMENTAL FACULTY SIZES
IN FOUR-YEAR COLLEGES AND UNIVERSITIES

|  | 1970 | 1975 | 1980 | 1985 |
| :--- | ---: | ---: | ---: | ---: |
| Mathematics Depts. |  |  |  |  |
| Full-time | 15,655 | $15,144^{\star}$ | 16,022 | 17,849 |
| Part-time | 2,436 | 3,397 | 5,456 | 7,087 |
| FTE | 16,467 | 16,276 | 17,841 | 20,211 |
| Statistics Depts. |  |  |  |  |
| Full-time | 700 | 732 | $610^{\star}$ | 740 |
| Part-time | 93 | 68 | 132 | 118 |
| FTE | 731 | 755 | 654 | 779 |
| Computer Science Depts. |  |  |  |  |
| Full-time | 688 | 987 | 1,672 | 3,605 |
| Part-time | 300 | 133 | 726 | 1,984 |
| FTE | 788 | 1,031 | 1,914 | 4,266 |

* This may represent an undercount.

The departmental faculty size data in Table 2-4 show a rather slowly growing mathematics departmental faculty and a much more rapidly growing computer science departinental faculty over the past fifteen years. Since the mathematics departmental faculty teaches a considerable amount of computer science, it is perhaps even more appropriate to separate out the total computer science faculty and look at the trends over time. In Chapter 4, we have a count of the total computer science faculty (i.e. the faculty who taught computer science in Fall 1985), which shows 5,651 full-time and 5,342 part-time for an FTE total of 7,432. The total FTE faculty that taught mathematics is the difference between the total FTE mathematical and computer science faculty (from the last columns of Table 2-3) and the total FTE computer science faculty. Table 2-5 gives the breakdown of the total mathematical and computer science faculty into
those who teach the mathematical sciences and those who teach computer science, along with course enrollments in the mathematical and computer sciences. While the enrollments per FTE faculty member in the total computer science faculty have stayed almost constant from 1970 to 1985, the corresponding ratio for the mathematical sciences teaching faculty has gone up dramatically. Over the past fifteen years, while the mathematical sciences faculty has been helping to create, and spin off, the computer science faculty, it has been seriously neglected in terms of its own growth.

TABLE 2-5

FTE FACULTY AND COURSE ENROLLMENTS

|  | 1970 | 1985 |
| :--- | ---: | ---: |
| FTE Mathematical Science Teaching Faculty | 16,804 | 17,825 |
| Mathematical Science Enrollments | $1,296,000$ | $1,827,000$ |
| Enrollments per FTE Faculty | 77 | 102 |
|  |  |  |
| Total FTE Computer Science Faculty | $1,182 *$ | 7,432 |
| Computer Science Enrollments | 90,000 | 558,000 |
| Enrollments per FTE Faculty | 76 | 75 |

* The FTE computer science departmental count of 788 from Table 2-4 is the only count available from 1970. To be comparable to the 1985 figures, the count should include other teachers of computer science. We have arbitrarily assigned a $50 \%$ factor to 788 to get the 1,182 total. This total is consistent with the later enrollment-faculty ratio.

The faculty counts do not include any allowance for graduate teaching assistants. As stated above, the FTE mathematical science teaching faculty is used in Table 2-5 in a special sense: it is the complement of the total FTE computer science faculty. From Table 2-5 it follows that the FTE faculty of all those teaching mathematical science courses increased $6 \%$ from 1970 to 1985 while the course enrollments in the mathematical sciences increased $41 \%$.

The data given here is for combined mathematical and computer sciences faculty and enrollments. The undergraduate course enrollments per FTE faculty member have stabilized and, in fact, dropped slightly since 1980. The trends since 1965 reflect the rapid faculty expansion in the sixties, followed by fairly stable total faculty numbers in the seventies, while enrollments were going up in both mathematics and computer science, and in the eighties, the faculty expansion in the public and private college sectors with more modest enrollment increases.

GRAPH 2 - A
COURSE ENROLLMENTS PER FTE TOTAL MATHEMATICS
and computer science faculty


The data do not include either graduate teaching assistants on the one hand or graduate enrollments on the other.

## TEACHING LOADS

In each Survey questionnaire since 1970 there has been a question concerning expected or typical teaching loads of faculty. Because of the increasing incidence of full-time faculty below the assistant professor level (see Tables 2-9 and 2-10 for current data on the percentages of sections taught by various components of the faculty), it was decided in this Survey to separately collect and report the data on teaching loads for such faculty (Table 2-8).

The percentages of departments in various categories reporting various expected loads over the past 15 years are given in Tables 2-6 through 2-8. There are several observations worth making.
(1) University statistics and computer science departments have consistently had noticeably lower loads (median 6 hours) as contrasted with university mathematics departments (median 7 hours).
(2) The public and private colleges have consistently had median loads at the 12-hour level except for public four-year college computer science departments which had a median 10-hour load in 1985.
(3) In all categories for which data from 1970 are available, the 1985 load patterns are quite similar to the 1970 patterns.

## TABLE 2-6

EXPECTED OR TYPICAL CREDIT-HOUR TEACHING LOADS IN MATHEMATICS DEPARTMENTS (PROFESSORIAL FULL-TIME FACULTY)

Percentage of Departments Indicating Given Load Per Semester or Quarter

|  | < 6 | 6 | 7-8 | 9-11 | 12 | >12 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Univ |  |  |  |  |  |  |
| 1970 | 8\% | 40\% | 32\% | 13\% | 7\% | -- |
| 1975 | -- | 26\% | 39\% | 26\% | 10\% | -- |
| 1980 | 10\% | 23\% | 29\% | 30\% | 9\% | -- |
| 1985 | 11\% | 27\% | 36\% | 16\% | 10\% | -- |
| Pu. 4-Yr. |  |  |  |  |  |  |
| 1970 | -- | 3\% | 5\% | 39\% | 35\% | 18\% |
| 1975 | -- | 1\% | 5\% | 15\% | 57\% | 21\% |
| 1980 | -- | 3\% | 6\% | 11\% | 59\% | 22\% |
| 1985 | 3\% | 4\% | 4\% | 19\% | 50\% | 20\% |
| Pr. 4-Yr. |  |  |  |  |  |  |
| 1970 | -- | -- | -- | 24\% | 60\% | 16\% |
| 1975 | -- | 4\% | 2\% | 24\% | 56\% | 14\% |
| 1980 | 2\% | 3\% | 5\% | 24\% | 45\% | 22\% |
| 1985 | -- | -- | 6\% | 10\% | 64\% | 20\% |

The 1985 data refer to mathematics faculty teaching in the mathematical sciences, not in computer science. However, the computer science teaching loads in mathematics departments are quite similar. The 1970, 1975, and 1980 data presumably also refer primarily to professorial level faculty since that was the dominant faculty and only one percentage was recorded.

TABLE 2-7

EXPECTED OR TYPICAL CREDIT-HOUR TEACHING LOADS IN STATISTICS AND COMPUTER SCIENCE DEPARTMENTS
(PROFESSORIAL FULL-TIME FACULTY)

Percentage of Departments Indicating Given Load Per Semester or Quarter

| Univ. Statistics |  |  |  |  |  |  |
| :--- | ---: | ---: | ---: | ---: | ---: | :--- |
| 1970 | $44 \%$ | $28 \%$ | $12 \%$ | $16 \%$ | -- | -- |
| 1975 | $17 \%$ | $45 \%$ | $11 \%$ | $22 \%$ | $5 \%$ | -- |
| 1980 | $9 \%$ | $41 \%$ | $34 \%$ | $16 \%$ | -- | -- |
| 1985 | $25 \%$ | $54 \%$ | $3 \%$ | $17 \%$ | -- | -- |
| Univ. Comp. Sci. |  |  |  |  |  |  |
| 1970 | $17 \%$ | $46 \%$ | $27 \%$ | $7 \%$ | $3 \%$ | -- |
| 1975 | $14 \%$ | $34 \%$ | $19 \%$ | $28 \%$ | $5 \%$ | -- |
| 1980 | $24 \%$ | $44 \%$ | $8 \%$ | $20 \%$ | $4 \%$ | -- |
| 1985 | $25 \%$ | $39 \%$ | $25 \%$ | $5 \%$ | $5 \%$ | -- |
| Pu. |  |  |  |  |  |  |
| $4-$ Yr. Comp. Sci. |  |  |  |  |  |  |
| 1980 | -- | $7 \%$ | -- | $23 \%$ | $54 \%$ | $15 \%$ |
| 1985 | $6 \%$ | $14 \%$ | $17 \%$ | $19 \%$ | $34 \%$ | $10 \%$ |

It seems clear from Tables 2-6 and 2-7 that over the past five years, with the exception of private college mathematics departments, standard teaching loads are holding steady or dropping slightly. The data on private colleges seem inconsistent with the drop in course enrollments per FTE faculty member in that category, data given with Graph 2-A. But the data on recent trends in universities toward slightly lower expected loads also runs counter to the fifteen year rise in course enrollments per FTE faculty, data given with Graph 2-A. Perhaps the increase in the incidence of lecture sections in university departments and the hiring of more non-professorial faculty explain how expected professorial teaching loads
can be kept low in the face of rising enrollments per FTE faculty member. Another factor affecting university faculty teaching loads is the graduate component. The Survey data do not specifically address this issue.

Since 1980 there has been a dramatic increase in the percentage of the faculty which is full-time non-doctorate and non-tenured (Table 2-12). A good many of such faculty would be expected to be in the non-professorial component of the faculty.

TABLE 2-8

1985 EXPECTED OR TYPICAL CREDIT-HOUR TEACHING LOADS (NON-PROFESSORIAL FULL-TIME FACULTY)

Percentages of Departments Indicating Given Load Per Semester or Quarter

Math. Depts.

| Univ. | $8 \%$ | $9 \%$ | $5 \%$ | $20 \%$ | $46 \%$ | $12 \%$ |
| :--- | :--- | :--- | :--- | ---: | :--- | :--- |
| Pu. 4-Yr. | $2 \%$ | $3 \%$ | -- | $8 \%$ | $59 \%$ | $28 \%$ |
| Pr. 4-Yr. | -- | -- | $9 \%$ | $11 \%$ | $62 \%$ | $18 \%$ |

Stat. Depts.
Univ. $38 \% \quad 7 \% \quad 6 \% \quad 42 \% \quad 7 \% \quad$--
Comp. Sci. Depts.

| Univ. | $18 \%$ | $11 \%$ | $14 \%$ | $41 \%$ | $16 \%$ | -- |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: |
| Pu. 4-Yr. | $3 \%$ | $7 \%$ | $4 \%$ | $16 \%$ | $58 \%$ | $12 \%$ |

The combination of low loads for a few and high loads for many suggests that there are two different types of full-time faculty below the professorial level:
(1) a fairly small number of research-type instructors chiefly in university departments and;
(2) a much larger number of faculty hired primarily as teachers with relatively high course loads.

## TEACHING BY VARIOUS GROUPS OF FACULTY

This year, for the first time, the Survey reports on a more detailed analysis of teaching responsibilities by professorial level faculty (assistant to full), by other full-time faculty and by part-time faculty for the three categories of institutions and various types of departments. The results summarized in Tables 2-9 and 2-10 below show a rather consistent pattern: full-time professorial level faculty teach about $2 / 3$ of the sections taught, other full-time faculty teach about 1/7 of the sections taught, and part-time faculty teach the remainder. The teaching of TA's was not included in these data. See the discussion following Table 2-10 and also Tables 3-4 to 3-6 for other data on teaching assistants. Table 2-9 refers to sections taught within mathematics departinents only and Table 2-10 to sections taught in computer science and statistics departments.

## TABLE 2 - 9

MATHEMATICS DEPARTMENT SECTIONS TAUGHT BY FULL- AND PART-TIME FACULTY Rows sum to $100 \%$

Assistant to
Full Professors
Mathematics Sections
Univ. $\quad(n=12,185)$

Pu. 4-Yr. $(n=21,489)$
Pr. 4-Yr. ( $n=11,727$ )
Statistics Sections
Univ. $\quad(n=759)$
Pu. 4-Yr. ( $n=1,912$ )
Pr. 4-Yr. ( $n=1,531$ )
Computer Science Sections

| Univ. | $(n=681)$ | $78 \%$ | $7 \%$ |
| :--- | :--- | ---: | ---: |
| Pu. 4-Yr. | $(n=3,999)$ | $64 \%$ | $15 \%$ |
| Pr. 4-Yr. | $(n=5,064)$ | $64 \%$ | $15 \%$ |

# COMPUTER SCIENCE AND STATISTICS DEPARTMENT SECTIONS TAUGHT BY FULL- AND PART-TIME FACULTY <br> Rows sum to $100 \%$ 

Comp. Sci. Depts. ${ }^{(1)}$

| Univ. | $(n=3,208)$ | $63 \%$ | $18 \%$ | $19 \%$ |
| :--- | :--- | :--- | :--- | :--- |
| Pu. 4-Yr. | $(n=4,869)$ | $68 \%$ | $15 \%$ | $17 \%$ |
| Pr. 4-Yr. | $(n=2,313)$ | $54 \%$ | $13 \%$ | $33 \%$ |

Stat. Depts. ${ }^{(1)}$
Assistant to Other
Full Professors Full-Time
Part-Time

Univ. \& Pu. 4-Yr. $(n=1,212) \quad 83 \% \quad 10 \%$

To get an estimate on the percentage of sections in universities or public colleges taught by graduate teaching assistants, we can compare the total number of sections reported in each of mathematics, statistics and computer science for questions 3 and $6 D$ of the main questionnaire (Appendix B). The former gives total numbers of sections taught and the latter, as compiled, the numbers taught by full and part-time faculty (not GTA's) in each of the mathematics, statistics and computer science categories. For universities, this analysis shows the percentage of sections taught by GTA's for each of the three subject areas to be close to $20 \%$. For public colleges, the overall percentage of sections taught by GTA's is less than $10 \%$. Thus, to include the teaching of GTA's, the percentages of sections reported taught in universities in Tables 2-9 and 2-10 should be reduced by about $20 \%$ of the figures shown. In public colleges the percentages should be reduced by somewhat less than $10 \%$ of those figures. In private colleges there are a negligible number of

[^3]GTA's. The figures on numbers of sections taught by GTA's, by this analysis are generally consistent with the numbers, from Table 3-5, of GTA's in various categories, reported as teaching their own classes.

From the data from which the above tables are obtained, and Table 2-3, we can also find the average numbers of sections taught by part-time faculty in various types of departments. These numbers are given in Table 2-11.

TABLE 2-11

## AVERAGE NUMBER OF SECTIONS TAUGHT BY A PART-TIME FACULTY MEMBER

Math. Dept.
1.54
Stat. Dept.
Comp. Sci. Dept.
All Depts.
1.01
1.11
1.44

Since about $5 / 6$ of the total part-time faculty is in public or private colleges where the median expected load is close to 12 hours and most sections almost certainly are 3 hours per week, an estimate of a part-time faculty member as roughly equivalent to $1 / 3$ FTE is reasonable.

## DOCTORATES AMONG FULL-TIME MATHEMATICAL <br> AND COMPUTER SCIENCE FACULTY

The trends over time in the percentages of doctorates among the combined full-time mathematical and computer sciences faculty are given by category of institution in Graph 2-B. We do not know how to explain the non-decrease in the public college percentage since 1980. Being counter to the overall trend, there could be a sampling abnormality in either year or a recording error in 1980. The decreases in the university and private college sectors are consistent with the large increases in total faculty (Table 2-3), and the large increases in the non-doctorate non-tenured faculty (Table 2-12). The overall percentage of doctorates among the total full-time faculty in 1985 was $73 \%$.

GRAPH 2 - B

PERCENTAGES OF FULL-TIME MATHEMATICAL AND COMPUTER SCIENCES FACULTY HOLDING DOCTORATES


TENURE AND DOCTORAL STATUS OF THE FACULTY

In Table 2-12, we give 1975, 1980 and 1985 percentages of the total mathematical and computer sciences full-time faculty, with and without tenure and with and without doctorates. These data clearly show decreases in all categories of tenured doctorates and very marked increases in the
percentages of non-tenured non-doctorate faculty. From Table 2-9 concerning the distribution of the teaching of sections among professorial level faculty, other full-time faculty and part-time faculty, it follows that a good many of the non-tenured non-doctorate faculty reported in Table 2-12 for 1985 do have professorial status in both the public and private college categories.

TABLE 2-12

TENURE AND DOCTORAL STATUS OF TOTAL MATHEMATICAL AND COMPUTER SCIENCE FULL-TIME FACULTY FOR FALL 1975, 1980 AND 1985

|  | 1975 | 1980 | 1985 |
| :---: | :---: | :---: | :---: |
| Universities |  |  |  |
| Tenured, PhD | 67\% | 64\% | 63\% |
| Tenured, non-PhD | 5\% | 4\% | 3\% |
| Non-tenured, PhD | 26\% | 28\% | 27\% |
| Non-tenured, non-PhD | 2\% | 4\% | 7\% |
| Public 4-Year (1) |  |  |  |
| Tenured, non-PhD | 18\% | 19\% | 13\% |
| Non-tenured, PhD | 20\% | 16\% (1) | 19\% |
| Non-tenured, non-PhD | 6\% | 13\% | 17\% |
| Private 4-Year |  |  |  |
| Tenured, PhD | 45\% | 38\% | 35\% |
| Tenured, non-PhD | 25\% | 16\% | 14\% |
| Non-tenured, PhD | 24\% | 26\% | 23\% |
| Non-tenured, non-PhD | 6\% | 20\% | 28\% |
| All Institutions |  |  |  |
| Tenured, PhD | 58\% (2) | 55\% | 51\% |
| Tenured, non-PhD | 14\% ${ }^{\text {(2) }}$ | 12\% | 10\% |
| Non-tenured, PhD | 24\% | 23\% | 23\% |
| Non-tenured, non-PhD | 4\% | 10\% | 16\% |

(1) The figures given here from the 1980 report are slightly inconsistent with other numbers of faculty given on page 45 of that report showing $70 \%$ of the faculty with doctorates.
(2) The figures given in Table 3.13 on page 49 of the 1975-76 report for all institutions are inconsistent with the figures given there for various categories of institutions. The figures we use are based on a recalculation using faculty totals for the various categories given on page 48 of that report.

There are three factors, each of which would be expected to contribute to the modest reductions in percentages of total full-time faculty holding doctorates, from $82 \%$ in 1975 to $78 \%$ in 1980 to $73 \%$ in 1985, and the corresponding increases in the size of the non-tenured non-doctorate level faculty. First is the major increase in the teaching of remedial (high school level) mathematics between fall 1975 and fall 1980, from 141,000 course enrollments to 242,000. A doctorate is hardly a prerequisite for teaching courses at or below the level of second year high school algebra. Second is the major $21 \%$ expansion in the overall size of the full-time faculty between fall 1980 and fall 1985; there simply weren't enough PhD's available to maintain the percentage of doctoral holding faculty among all faculty. Third is the continuing major expansion of enrollments in computer science and, thus, in faculty teaching computer science. This occurs at a time when relatively few doctorates in computer science are being produced.

The percentages of tenured faculty and of doctorate-holding faculty are given in Table 2-13 by type of department and by category of institution. The overall percentages of the full-time mathematics departmental faculty and the full-time computer science departmental faculty that hold doctorates are $74 \%$ and $70 \%$ respectively $(73 \%$ in the combined total faculty in the mathematical and computer sciences). Whereas $65 \%$ of the mathematics departmental faculty is tenured, only $42 \%$ of the computer science departmental faculty is tenured.

# TENURE AND DOCTORATE-HOLDING PERCENTAGES AMONG FULL-TIME FACULTY IN 1985 

|  | Tenured | Doctorate-Holding |
| :---: | :---: | :---: |
| Math. Depts. |  |  |
| Univ. | $71 \%$ | $90 \%$ |
| Pu. 4-Yr. | $69 \%$ | $70 \%$ |
| Pr. 4-Yr. | $51 \%$ | $62 \%$ |
|  |  |  |
| Computer Sci. Depts. | $49 \%$ | $82 \%$ |
| Univ. | $40 \%$ | $69 \%$ |
| Pu. 4-Yr. | $31 \%$ | $35 \%$ |
| Pr. 4-Yr. |  |  |
| Statistics Depts. | $68 \%$ | $97 \%$ |

AGE AND SEX DISTRIBUTION OF FULL-TIME FACULTY

The age distributions of the full-time faculty in the mathematical and computer sciences for 1975 and 1985 are given in Table 2-14. The total faculty size in 1985 was $32 \%$ above that in 1975. In light of this increase in faculty size and assuming balanced attrition and new entrants, a 16\% 40-44 age cohort in 1975 should be a $12 \%$ 50-54 age cohort in 1985. The figures given in Table 2-14 verify this observation for middle-level age groups.

At the younger age groups there will have been considerable attrition as well as new hirings over the 10 year span so that one does not expect the cohort to stay the same absolute size.

TABLE 2-14

AGE DISTRIBUTION OF FULL-TIME FACULTY IN THE MATHEMATICAL AND COMPUTER SCIENCES

|  | 1975 | 1985 |
| :---: | :---: | :---: |
| $<30$ | 10\% | 7\% |
| 30-34 | 22\% | 15\% |
| 35-39 | 22\% | 16\% |
| 40-44 | 16\% | 20\% |
| 45-49 | 11\% | 16\% |
| 50-54 | 9\% | 12\% |
| 55-59 | 5\% | 8\% |
| 60 or more | 5\% | 6\% |

It is clear that the faculty is aging but not very rapidly. In the ten year span 1975-1985, the average faculty age has gone up from about 40.5 to over 43. Considering the big influx of new (younger) entrants, that seems about right.

The large increases in the part-time and in the non-tenured non-doctoral full-time components of the faculty, indicate that there is likely to be continuing turnover in the full-time faculty, producing, in the future, a more evenly spread out age distribution with a slowly increasing average age.

It should be noted that some individual university faculties, including some of the better research faculties, are reported to have aging problems. But the picture in-the-large does not look discouraging except for the drop in the under 40 populations.

The age distribution of the university mathematics faculty is almost identical to that of the overall mathematical sciences faculty in Table 2-15, differing by one or less in every age group percentage and having the average age of 44 . Only $35 \%$ of the university faculty is under 40 , in contrast to $55 \%$ in 1975 and $48 \%$ in 1980, a fact that may be of some
concern. It is difficult to state what the norms should be. From Table 2-15 and from comparable figures in the university sector it is clear that the faculty has not been going on to retire at age 70 but rather has been retiring in the early to mid-sixties.

The men on the mathematical sciences faculty average about 44.5 years, four years older than the women. In computer science, the men average about 40.5 years of age, and the women 37 . In Table 2-15 we give the age distributions of the separate departmental full-time faculties in the mathematical and computer sciences.

TABLE 2-15
age distribution of mathematical science and computer science DEPARTMENTAL FACULTIES
60

## MINORITIES

The percentages of minorities on the four-year college and university full-time faculty in each of the mathematical and computer sciences is given in the following table.

TABLE 2 - 16

## MINORITIES IN THE FULL-TIME MATHEMATICAL AND COMPUTER SCIENCES DEPARTMENTAL FACULTIES

Amer./Al. Asian Black Hispanic

| Math. Sci. Faculty | $0.1 \%$ | $7.1 \%$ | $3.5 \%$ | $3.4 \%$ |
| :--- | ---: | ---: | ---: | ---: |
| Computer Sci. Fac. | $0.1 \%$ | $11.7 \%$ | $.3 \%$ | $1.2 \%$ |

In 1980 the Survey reported almost $3 \%$ of the faculty were Black. The current figures, compared with the 1975 Survey, do show a noticeable growth in the number of Asians on our faculties over the past 10 years, generally compatible with the growth (reported in other studies) of Asians among the graduate student population. In statistics departments, 22.5\% of the faculty are Asian.

The Black faculty members are concentrated in the public college sector $(6.9 \%$ of the total faculty there), presumably reflecting the faculty at historically Black institutions. In the university sector slightly less than $1 \%$ of the faculty is Black. The Hispanic mathematics faculty members are spread proportionately over all sectors of the four-year and university populations (except for statistics).

The percentage of the full-time departmental faculty who were female was $15 \%$ for mathematics, $10 \%$ for statistics, and $13 \%$ for computer science for an overall 14\%, (the same percentage as that reported in 1980). As mentioned above, the average age of faculty women was about four years less than that of men.

Table 2-17 gives the percentages of faculty who are female by various types of departments and categories of institutions.

TABLE 2-17

PERCENTAGE OF FULL-TIME 1985 DEPARTMENTAL FACULTY WHO ARE FEMALE

-     - Mathematics Depts.- - - - Computer Science Depts.- - Stat. Depts. Univ. Pu. 4-Yr. Pr. 4-Yr. Univ. Pu. 4-Yr. Pr. 4-Yr. Combined


DOCTORATE-HOLDING FACULTY

The 1985 age distribution of the doctorate holding mathematical and computer sciences faculties are available from two sources: (1) this Survey and (2) the biennial NSF publication, "Characteristics of Doctoral Scientists and Engineers in the United States". The gross figures are compatible although the details of the age distributions vary in the two studies. The NSF data is for academically employed doctoral scientists rather than for faculty, per se. But the two sets of data should be roughly comparable.

The total count of doctoral-holding mathematical scientists in this Survey is 13,025 compared to 13,027 in the NSF figures. The total count
of doctoral-holding members of the computer science departmental faculty is 2,537 in this Survey while the NSF figure for doctoral-holding computer specialists is 5,124, twice as much. The NSF figure presumably includes people in computer centers and on special research projects and presumably includes some faculty who are in mathematics or other departments but teach computer science. From the Survey's special computer science questionnaire, there are a total of 3,754 doctoral-holding full-time teachers of computer science and 2,231 doctoral-holding part-time teachers of computer science. Of the 2,231 part-time doctoral-holding faculty, 181 have degrees in computer science and 1,360 in mathematics and many are full-time in the reporting institution. Thus the NSF and Survey figures seem to represent comparable populations.

The age distribution of the doctoral-holding faculty from the Survey data and of academic scientists from NSF data are given in Table 2-18. It is not clear how the conflicting age patterns on the tails of the distributions should be reconciled. The current Survey data are quite consistent with past Survey data.

TABLE 2-18

AGE PATTERNS OF DOCTORAL FACULTY (SURVEY) AND ACADEMIC SCIENTISTS (NSF)

|  |  |  |  | 60 <br> or <br> more |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Mathematics | 30 | $30-39$ | $40-49$ | $50-59$ |  |
| Survey | $5 \%$ |  |  |  |  |
| NSF Data | $3 \%$ | $26 \%$ | $40 \%$ | $22 \%$ | $7 \%$ |
| Computer Science |  |  | $40 \%$ | $22 \%$ | $10 \%$ |
| Survey | $8 \%$ | $37 \%$ | $41 \%$ | $11 \%$ |  |
| NSF Data | $2 \%$ | $39 \%$ | $40 \%$ | $13 \%$ | $6 \%$ |

## STATISTICS FACULTY

For all full-time faculty with highest degrees in statistics, Table 2-19 indicates their 1985 employment in mathematics, statistics and computer science departments.

TABLE 2-19

EMPLOYMENT OF STATISTICIANS IN VARIOUS TYPES OF DEPARTMENTS

| Univ. | Pu. 4-Yr. | Pr. 4-Yr. | Total |
| :---: | :---: | :---: | :---: |
|  |  |  |  |
| 283 | 488 | 158 | 929 |
| 572 | 38 | --- | 610 |
| $\frac{20}{875}$ | $\frac{6}{532}$ | $\frac{29}{187}$ | $\frac{55}{1594}$ |

Of these total full-time faculty, the numbers with doctorates are: universities, 814; public four-year colleges, 468; and private four-year colleges, 118; for a total of 1,400 in all university and four-year colleges. The Survey estimate on the total number of separate statistics departments in universities is 40 and in public colleges, 5, with none identified in private colleges. Because the numbers are so small in the public and private college sectors, it is quite probable that the sampling procedures used did not reveal the actual numbers. However the total faculty and PhD counts of statisticians should be fairly reliable. It is known (and is consistent with the data above) that many universities and some colleges which do not have separate statistics departments do have groups of statisticians on their mathematics faculties acting as subdepartments. For information on students in statistics see Tables 1-11 to 1-13.

## FACULTY MOBILITY IN THE MATHEMATICAL SCIENCES

Data on faculty mobility from academic year 1984-85 to academic year 1985-86 are given in Table 2-20 for the total full-time mathematical sciences departmental faculty. Details are not given by category of institution because the overall numbers concerned are fairly small. In the 1975 and 1980 Survey reports, comparable data were given for the combined mathematical and computer sciences departmental faculty. This year, results for computer science departments are given separately in Chapter 4. The data this year do not show significant differences from the 1980 data except that the overall hiring of non-doctorate faculty from graduate schools shows an increase of about $60 \%$ from the 1980 figures and the "other" categories this year are relatively larger, though still small in absolute numbers. The "deaths and retirements" category for faculty outflow is about $1.1 \%$ of the total faculty, a small percentage. For the 1980 Survey, the combined mathematical and computer science faculty had a $0.9 \%$ death and retirement rate. Interesting figures are the Inflow/Outflow ratios with respect to non-academic employment which are $76 / 157$ for doctorates and $116 / 33$ for non-doctorates. The net loss to non-academia for doctorate faculty is only about a half percent of all doctoral faculty. The total faculty who switched departments (institutions) was about 600 doctorates and 175 non-doctorates.

# FULL-TIME MATHEMATICAL SCIENCES DEPARTMENTAL FACULTY MOBILITY 1984-85 to 1985-86 

| Faculty Inflow | Doctorates | Non-Doctorates |
| :---: | :---: | :---: |
| From Graduate School | 362 | 463 |
| From Post-Doctoral or Research |  |  |
| Appointments | 75 | 4 |
| From Non-Academic Positions | 76 | 116 |
| From "Other" | 45 | 80 |
| Total Inflow | 558 | 663 |
| Faculty Outflow |  |  |
| Deaths and Retirements | 163 | 57 |
| To Graduate School | 27 | 90 |
| To Non-Academic Positions | 157 | 33 |
| Otherwise Occupied | 62 | 99 |
| Total Outflow | 409 | 279 |

It should be noted that these are one-year figures on mobility. They represent a one-year increase of 533 in total mathematical science departmental faculty which, with a 148 increase in computer science department faculty, is quite consistent with the reported overall full-time faculty growth from 18,304 in 1980 to 22,195 in 1985. The figures are also reasonably consistent with AMS Survey data which projected a total mathematical sciences faculty growth of 682 from fall 1983 to fall 1984.

The one-year Survey growth figures given above are from changes in existing departments. They do not include the creation or abolition of separate departments or institutions. However, chairpersons may well have reported only changes in that component of the faculty (still) in the department, if the department had been split.

Question 10 on the main questionnaire tried to identify faculty openings and whether or not they were filled by people meeting the advertised qualifications. The reader is referred to Appendix $B$ for the precise wording of this question. Because of spotty responses, the projections of the responses are statistically somewhat less reliable than those of most other questions. We present combined data for all four-year colleges and universities since there appeared to be only relatively minor differences between categories of institutions in most cases and the combined data is probably most reliable. Note from Table 2-21 that about three-fourths of all positions in mathematics and statistics and one-half of all positions in computer science were filled by people meeting advertised qualifications. Half the other openings were left unfilled.

TABLE 2-21

NEW JOB OPENINGS FOR 1985-86
PERCENTAGES OF OPENINGS FILLED IN VARIOUS WAYS


Question 10, itself, avoids the issues of whether individual departments are realistic in terms of educational qualifications and salary levels for advertised positions. The results suggest that most departments are realistic.

## CHAPTER 3

## ADMINISTRATIVE ISSUES AND DEPARTMENTAL PHENOMENA

This chapter deals with changes in administrative structures affecting the mathematical and computer sciences, teaching loads, the uses of various instructional formats, computer use in instruction, the teaching functions and discipline sources of graduate teaching assistants, and issues considered important by department chairpersons.

HIGHLIGHTS

- The creation of new computer science departments and the broadening of departmental duties and names to include computer science were frequent administrative changes.

1 In five major introductory courses, $41 \%$ of university students are taught in large lecture sections (over 80 students) whereas in private colleges only $2 \%$ are. About one-fifth of all students in these five courses are taught in sections of 40 to 80 students.

- There is little required use of computers in college algebra or calculus or in any mathematics course other than numerical analysis or other computing related courses.
- Since 1980 the number of graduate teaching assistants has been stable in university mathematics departments but has gone up markedly in statistics and computer science departments and in public college mathematics departments.
- About $95 \%$ of all graduate teaching assistants in mathematics, statistics or computer science are students in the same or related subjects.
- Salary levels and departmental support practices were widely regarded as major problems in many departments.


## ADMINISTRATIVE STRUCTURES

The Survey questionnaire sought information on administrative changes in the period 1980-1985 affecting departments in the mathematical and computer sciences. Questions 2 a and 2 b (see Appendix B) referred to consolidations or divisions of departments. Table 3-1 gives administrative changes reported in university, public four-year college and private four-year college categories.

TABLE 3-1

1980-1985 ADMINISTRATIVE CHANGES AFFECTING MATHEMATICAL
OR COMPUTER SCIENCES DEPARTMENTS

|  | Total Number <br> of Institutions |  | Consolidations |
| :--- | :---: | :---: | :---: | :---: |$\quad$| Divisions |
| :---: |
|  |
| Universities |

Of the institutions reporting consolidations:
(a) about $40 \%$ involved formation of schools or divisions with several new mathematics and computer science departments included in these changes;
(b) about $35 \%$ were mathematics and computer science consolidations but in many instances these appeared to be simple expansions of mathematics departments and/or name changes;
(c) about $25 \%$ involved new departments such as mathematics and physics, computer science and electrical engineering, etc.
The "division of departments" reported are almost all accounted for as new computer science departments. In the three categories of institutions, new computer science departments from 1980 to 1985 were sepaarately calculated as 11,59 and 102. Not all would have occurred as divisions of departments. In the university category a few other divisions into various mathematical science departments likely occurred.

As mentioned elsewhere, there are now projected to be separate computer science departments in 105 of the 157 universities, in 141 of the 427 public four-year colleges, and in 150 of the 839 private four-year colleges.

## INSTRUCTIONAL FORMATS

The Survey sought information (Question 4) from all respondents as to the sizes or types of classes taught in selected introductory subjects. The specific question, a slight variant of that used in the 1980 Survey, asked for the numbers of students taught in:
(1) small classes (less than 40 students),
(2) 1 large classes (between 40 and 80 students),
(3) lectures (over 80 students without recitation or quiz sections),
(4) lectures (over 80 students with recitation or quiz sections),
(5) self-paced instruction and
(6) other formats (See Appendix B).

The five subjects were College Algebra, Calculus (Math., Eng., Phys. Sci.), Calculus (Bio., Soc., Mgmt. Sci.), CS I (Computer Prog. I), and

Elementary Statistics. (The subjects were those used in the 1980 questionnaire except that "college algebra" replaced "finite math" since enrollments in college algebra were much higher than those in finite math).

To clarify the question, the various courses were listed with the identifying numbers used on the questionnaire form. The statistical analysis (projections) of the results were complicated by occasional incomplete or misleading answers to this particular question. However the overall results were generally consistent with those reported in 1980. In the 1975 Survey, a different type question was used and thus results from 1975 cannot be compared directly.

Generally, there were two major findings of which only the first is Vvident from Table 3-2:
(1) There are sharp differences in instructional formats between universities, public four-year colleges and private four-year colleges and
(2) Within any of the 3 categories of institutions, the reported differences in formats for the five subject areas studied were rather minor, particularly for the two calculus courses and computer programming. College algebra generally was taught in somewhat smaller sections and statistics in somewhat larger.

TABLE 3-2

PERCENTAGE OF STUDENTS TAUGHT IN VARIOUS FORMATS
IN FIVE STANDARD INTRODUCTORY COURSES

| Class Format | University |  | Public 4-Year |  | Private 4-Year |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1980 | 1985 | 1980 | 1985 | 1980 | 1985 |
| $<40$ | 36 | 38 | 67 | 62 | 79 | 82 |
| 40-80 | 31 | 20 | 21 | 22 | 13 | 16 |
| >80, no Quiz Sec. | 10 | 12 | 2 | 5 | 1 | - |
| 780 , Quiz Sec. | 21 | 29 | 9 | 10 | 7 | 2 |
| Self-Paced or Other | 1 | 1 | - | 1 | - | - |

The table shows that in universities there appears to be a trend away from large classes (40-80) toward lectures with quiz sections. In universities more than $40 \%$ of students in these five subject areas are taught in a large lecture format whereas in private colleges only $2 \%$ are.

It is also worthy of note that a negligible number of students (less than $1 \%$ in these five subject areas) are taught in "self-paced" or "other" modes; the standard formats totally predominate. The mathematical community is definitely not convinced of the efficacy of non-standard modes of instruction when it comes to course content needed for further work. The 1975 Survey showed that there was widespread experimentation with various alternative forms of instruction. It is clear from the 1980 and 1985 results that in the basic introductory courses the standard formats totally predominate. Similar turning away from various alternative modes or forms of instruction was evident in the two-year college category (see Chapters 5 and 6).

## COMPUTER USE IN INSTRUCTION

All respondents were asked to indicate (Question 5) the number of sections in various courses in which the use of computers (micros/ minis/ mainframes) is required. A comparable question had not been asked in 1980. The responses were not of good statistical quality. Thus the results, listed as percentages of the total number of sections for the named courses, are summaries of all responses rather than projections. The results reveal relatively little obligatory computer use in mathematics courses except for those subjects closely identified with computing or computation. See Chapter 4 for a discussion of computer use in computer science courses and Chapter 5 for related two-year college phenomena.

TABLE 3-3

REQUIRED COMPUTER USE IN MATHEMATICS AND STATISTICS COURSES as Percentage of all sections taught in selected subjects

| Course and Number | Univ. | Pu. 4-Yr. | Pr. 4-Yr. | Total |  |
| :--- | ---: | :---: | :---: | :---: | ---: |
|  |  |  |  |  |  |
| College Algebra (5) | $0 \%$ | $0 \%$ |  | $3 \%$ | $0 \%$ |
| Calculus (15) | $5 \%$ | $8 \%$ | $6 \%$ | $7 \%$ |  |
| Diff. Equations (17) | $15 \%$ | $11 \%$ | $13 \%$ | $13 \%$ |  |
| Discrete Math. (18) | $11 \%$ | $28 \%$ | $19 \%$ | $18 \%$ |  |
| Linear Algebra (19) | $15 \%$ | $7 \%$ | $23 \%$ | $13 \%$ |  |
| Numerical Analysis (37) | $91 \%$ | $85 \%$ | $82 \%$ | $87 \%$ |  |
| Elementary Statistics (45) | $29 \%$ | $23 \%$ | $43 \%$ | $29 \%$ |  |

The issue of the (required) use of calculators in mathematics or statistics courses in four-year colleges or universities was not pursued in the 1985 Survey.

## GRADUATE TEACHING ASSISTANTS

In the 1980 Survey there were two questions about teaching assistants: one about the total number of teaching assistants, including the numbers who were graduate students in various types of departments (those reporting, other mathematical (computer?) science or not mathematical science) or, who were undergraduates. The second question dealt with the utilization of teaching assistants (teaching own classes, conducting quiz or recitation sections, paper grading, tutoring, other). There seemed to be ambiguity about the term "teaching assistant" if undergraduates were counted: e.g. "Are undergraduate paper graders teaching assistants?" In 1980, $50 \%$ of all mathematics teaching assistants
in private colleges were tutors, whereas only $8 \%$ of teaching assistants in the university category were tutors, presumably indicating an uncertainty as to whether or not to count undergraduate students. From the last three columns of Table 3-4, it appears evident that some undergraduate paper graders or tutors were counted in various categories in 1980.

To clarify the terms in use, it was decided to request information for graduate teaching assistants only in the 1985 Survey. Thus the 1985 data are not directly comparable to the 1980 data, particularly in the private college category. According to the 1980 Survey report "more than one-fifth" of all teaching assistants reported were undergraduates. See Table 3-5 for a comparison of counts of teaching assistants or graduate teaching assistants reported in 1980 and 1985. In Table 3-5, the private college mathematics category clearly reveals a count of many undergraduates classed as teaching assistants in 1980. For 1985, with only GTA's included, the number of teaching assistants was much lower. For other phenomena, see the discussion following Table 3-5.

In Table 3-4 are given the 1985 percentage distribution of graduate teaching assistants by principal teaching function by category of department.

The reader should note, as pointed out in the introduction to this report and in Chapter 2, that the university and public college categories are not identical, or directly comparable with, the AMS Survey Groups I, II, and III and M. For technical reasons, the Department of Education lists from which the Survey sampling was drawn produces a set of institutions for the university category which effectively replaces a number of large public universities in AMS Groups I, II, and III with smaller private universities. These larger universities then appear in the public four-year college category. Thus the Survey totals on GTA's in universities would be expected to be somewhat lower than in AMS Group I, II, and III data and the public four-year college totals would be expected to be somewhat higher than in AMS Group M data. That is the case. But the overall totals are not inconsistent.

TABLE 3-4

## PRINCIPAL TEACHING FUNCTIONS OF GRADUATE TEACHING ASSISTANTS

 1985(Rows sum to 100\%)

| Type of Department: | $\begin{aligned} & \text { Teaching } \\ & \text { Own } \\ & \text { Class } \end{aligned}$ | Conducting Quiz/Recit. Sections | Paper Grading | Tutoring | Other |
| :---: | :---: | :---: | :---: | :---: | :---: |
| University |  |  |  |  |  |
| Math. ( $n=5038$ ) | 47\% | 40\% | 8\% | 4\% | 1\% |
| Stat. ( $n=711$ ) | 24\% | 52\% | 14\% | 6\% | 4\% |
| C.S. ( $n=1746$ ) | 36\% | 26\% | 23\% | 11\% | 4\% |
| Public 4-Year |  |  |  |  |  |
| Math. ( $n=2077$ ) | 44\% | 41\% | 9\% | 6\% | 0\% |
| Stat. ( $n=85$ ) | 29\% | 15\% | 56\% | 0\% | 0\% |
| C.S. ( $n=530$ ) | 23\% | 15\% | 35\% | 24\% | 3\% |
| Private 4-Year |  |  |  |  |  |
| Math. ( $n=111$ ) | 60\% | 34\% | 3\% | 3\% | 0\% |
| C.S. ( $n=30$ ) | 40\% | 20\% | 40\% | 0\% | 0\% |

The high incidences of "paper grading" and/or "tutoring" functions in statistics and computer science departments probably reflect the different nature of homework or projects in those subject areas as compared to mathematics. They presumably reflect both (1) the handling of data and/or computers, requiring different types of activities and knowledge than grading freshman mathematics papers and (2) some different patterns of instruction including a higher percentage of lecture sections.

The following table of reported numbers of graduate teaching assistants (teaching assistants for 1980) with their principal teaching function is perhaps even more revealing than would be corresponding percentages. The numbers for which data are given for 1980 are extracted from the totals and percentages reported in 1980, since the actual numbers for 1980 are not available.

## TABLE 3-5

NUMBER OF TEACHING ASSISTANTS FOR 1980 AND GRADUATE TEACHING ASSISTANTS FOR 1985

BY PRINCIPAL TEACHING FUNCTION

| Teaching <br> Own | Conducting <br> Quiz/Recit. |
| :---: | :--- |
| Class Paper |  |
| Sections |  |$\quad$| Grading |
| :--- | Tutoring Other

University
Mathematics Depts.

| 1980 | 2745 | 1592 | 604 | 439 | 55 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 1985 | 2368 | 2015 | 403 | 202 | 50 |

Statistics Depts.
1980
$229 \quad 153 \quad 120 \quad 0$
$\begin{array}{llllll}1985 & 171 & 369 & 100 & 43 & 28\end{array}$
Computer Science Depts.
198032938
$653 \quad 471$
0
1985
$629 \quad 453$
402
192
70
Public 4-Year
Mathematics Depts.

| 1980 | 445 | 230 | 230 | 414 | 230 |
| ---: | ---: | ---: | ---: | ---: | ---: |
| 1985 | 913 | 852 | 187 | 125 | 0 |

Computer Science Depts.
1980

| 0 | 51 | 15 | 0 |
| ---: | ---: | ---: | ---: |
| 80 | 185 | 127 | 16 |

Private 4-Year
Mathematics Depts.

| 1980 | 81 | 219 | 277 | 577 | 0 |
| :--- | ---: | ---: | ---: | ---: | ---: |
| 1985 | 67 | 38 | 3 | 3 | 0 |

The universally higher numbers in the "paper grading" and "tutoring" functions for 1980 over 1985 (except for Public 4-Year Computer Science Departments with almost twice as many departments in 1985) strongly
suggest that many undergraduates assigned to these functions were counted as teaching assistants in 1980. The sum of the actual numbers in columns 1 and 2 for university mathematics departments shows a small gain from 1980 to 1985 in teaching assistants actually teaching rather than a small loss superficially suggested by gross data. The impressive five year gains in columns (1) and (2) for most public college and university categories indicate a substantially broader use of teaching assistants for teaching, consistent with the generally sizeable increases in part-time and non-professorial full-time faculties in these categories (compare with the figures in Table 2-4).

By comparing the 1980 and 1985 data and questions, it seems clear that some private colleges as well as public four-year colleges use some undergraduates for teaching functions.

It would be nice to have fairly reliable estimates of the percentage changes in the numbers of graduate teaching assistants in the various categories of departments for which we have data on the number of teaching assistants in 1980. Based on estimates from the "over 20\%" figure of undergraduates among the 1980 teaching assistants and from an analysis of the principal teaching functions of teaching assistants in 1980 and 1985, it seems clear that:
(1) the number of graduate teaching assistants in university mathematics departments in 1985 was substantially the same as that in 1980;
(2) the number of graduate teaching assistants in university computer science departments who actually performed teaching functions increased by about $50 \%$ from 1980 to 1985, and;
(3) the number of mathematics department graduate teaching assistants in public four-year colleges who actually performed teaching functions more than doubled from 1980 to 1985.
In other categories the 1980 figures were sufficiently small and the procedures too uncertain to make meaningful estimates of percentage increases from 1980 to 1985.

With respect to the public four-year college computer science category, it should be noted that the number of departments went up $100 \%$ from 1980 to 1985.

## WHAT DO GRADUATE TEACHING ASSISTANTS STUDY?

In the 1980 Survey report, it was stated that in university mathematics departments more than $20 \%$ of teaching assistants were not mathematics graduate students. The exact figure was not given, nor was there a breakdown into undergraduate or graduate students in another statement that "more than 20\%" were in "other departments". Table 3-6 below gives information for graduate teaching assistants in 1985. Overall, almost all (92\%) of the graduate teaching assistants are students in the departinent for which they teach and half of the rest are students in other mathematics or computer science departments.

TABLE 3-6

DEPARTMENTS IN WHICH GRADUATE TEACHING ASSISTANTS STUDY 1985
$\left.\begin{array}{lrcc}\text { University } & \text { Number } & \begin{array}{c}\text { Percentage } \\ \text { In Own } \\ \text { Department }\end{array} & \begin{array}{c}\text { Percentage } \\ \text { In Other } \\ \text { Mathematics Or }\end{array} \\ \text { Mathematics } & & \\ \text { Computer Sci. Dept。 }\end{array}\right]$

The widely reported earlier use by state university mathematics departments of graduate teaching assistants who were students in engineering or other disciplines seems to have largely ended.

Since this Survey dealt with undergraduate phenomena including, of course, teaching assistants, but not with graduate education, per se, there was no attempt to identify numbers of graduate research assistants or associates. There was also, perhaps regrettably, no attempt to identify citizenship status of graduate teaching assistants. AMS, NSF and other studies address parts of this latter issue.

DEPARTMENTAL CONCERNS

As a new initiative to give a statistical base for possible new studies on the status of the profession in academe, the Survey included two lists of questions, one on professional activities of faculty and how they affect faculty advancement and/or salary decisions and the second on problems of the mid-80's as seen by department chairpersons. Each question had a scale of 0 to 5 with zero representing no importance and 5 representing major importance. The results were tabulated for all categories of institutions for both mathematics and computer science departments and for university statistics departments. The numbers shown in the remaining tables in this chapter are (1) the percentage of all departments giving a 4 or 5 response for the particular question and (2), in parentheses, the percentage giving a 0 or 1 response for the same question. The percentage giving a 2 or 3 response can be found by subtracting the sum of the two percentages given from 100. The difference in the two numbers given is a measure of the preponderance of departmental attitudes on the subject. Note that high percentages do not measure the intensity of feeling, as such, but rather the breadth of concern.

Table 3-7 gives the results of the questionnaire on the importance of various professional activities in faculty advancement and/or salary decisions by category of institution. The results confirm conventional wisdom, university departments value published research and colleges, particularly private colleges, value teaching performance. Service to the department or institution is much more commonly important to colleges than to universities. In universities, mathematics departments and statistics departments have remarkably similar priorities.

Generally the computer science department responses on professional activities were quite similar to the mathematics department responses. They are given separately in Chapter 4.

## TABLE 3-7

## IMPORTANCE OF PROFESSIONAL ACTIVITIES IN ADVANCEMENT AND/OR SALARY DECISIONS

|  | Univ. | Mathemati Pu. 4-Yr. | $\text { Sr. } \overline{\mathrm{Pr}}-\overline{\mathrm{Yr}} .$ | Stat. Univ. |
| :---: | :---: | :---: | :---: | :---: |
| Classroom Teaching Performance | 70 (3) | 81 (2) | 96 (4) | 71 (6) |
| Published Research | 96 (0) | 70 (10) | 26 (39) | 100 (0) |
| Service to Department and/or University (College) | 31 (5) | 63 (5) | 66 (0) | 31 (11) |
| Talks at Profess. Mtgs. | 42 (5) | 49 (11) | 13 (28) | 25 (11) |
| Activities in Profess. Societies and/or Pub. Service | 22 (8) | 45 (4) | 33 (9) | 31 (6) |
| Supervision of Grad. Students | 34 (7) | 21 (32) | ------- | 81 (0) |
| Undergraduate/Grad. Advising | 9 (22) | 24 (20) | 39 (12) | 21 (21) |
| Years of Service | 1 (52) | 34 (29) | 46 (16) | 15 (47) |
| Expository and/or Pop. Articles | 22 (13) | 37 (14) | 14 (40) | 14 (19) |
| Textbook Writing | 9 (35) | 17 (35) | 11 (58) | 12 (50) |

## PROBLEMS OF THE MID-80'S

In the 23 questions on problems of the mid-80's there were several questions where the responses stood out significantly. The results for these questions are given separately in Table 3-8A. The remaining results are given in three tables, (1) those dealing with student issues, Table 3-8B, (2) those dealing with faculty issues, Table 3-8C and those dealing with support issues, Table 3-8D. We give the results in approximate order of decreasing importance as seen by departmental chairpersons. The concerns not commonly considered as major problems are almost as interesting as those considered important. Generally, those concerns identified as major problems are those which need addressing by the community. As to be expected, for some concerns there are wide variations reported among departments in the various types of universities or colleges and between departments in the mathematical and computer sciences. The responses for computer science are summarized separately in Chapter 4 in Tables $4-18$ and 4-19A to $D$ of this report. The heavy emphasis on salary and support issues reported in Table 3-8A means there is continuing pressure for upward salary adjustments and that there should be continuing pressure for better departmental support services. Clearly the larger community should be concerned with departmental support practices.

As in Table 3-7, the percentage of departments identifying the concerns as of major (minor) importance is given in Tables 3-8A to $D$.

TABLE $3-8 \mathrm{~A}$

## MAJOR PROBLEMS

|  | Univ. | Mathemat Pu. 4-Yr. | $\text { Pr. } \overline{4}-\overline{Y r} .$ | Stat. Univ. |
| :---: | :---: | :---: | :---: | :---: |
| Salary Levels/Patterns | 66 (6) | 69 (2) | 60 (0) | 64 (8) |
| Departmental Support Services |  |  |  |  |
| (Travel, Secret. etc.) | 61 (13) | 62 (10) | 36 (23) | 70 (0) |
| Research Funding | 71 (8) | 45 (17) | 17 (63) | 51 (14) |
| Maintaining Faculty Vitality | 54 (13) | 54 (5) | 41 (21) | 48 (18) |

TABLE 3 - 8B

STUDENT ISSUES

-     -         - Mathematics - . - Stat. Univ. Pu. 4-Yr. Pr. 4-Yr. Univ.

Lack of Quality of
$\begin{array}{lllllllll} \\ \text { Undergraduate Majors } & 38 & (15) & 62 & \text { (6) } & 39 & \text { (7) } & 31 & \text { (9) }\end{array}$
Lack of Quantity of
Undergraduate Majors 39 (18) 54 (20) 42 (9) 22 (21)
Lack of Quality of Department
Graduate Students
Lack of Quantity of Department
Graduate Students
Remediation
Class Size

50 (2) 44 (21) ------* 56 (14)

| $52(14)$ | $53(24)$ | $\cdots-A^{*}$ | $55(20)$ |  |
| :--- | :--- | ---: | ---: | ---: | ---: |
| $39(28)$ | $66(5)$ | $45(17)$ | $0(42)$ |  |
| $52(12)$ | $39(21)$ | $21(32)$ | 60 | $(6)$ |

* Since relatively few of the departments in this category have graduate programs, the responses are not given.

TABLE 3 - 8C

## OTHER FACULTY ISSUES

|  | Univ. | Mathemat Pu. 4-Yr. | $\text { Pr. } 4-\mathrm{Yr} .$ | Stat. Univ. |
| :---: | :---: | :---: | :---: | :---: |
| Teach. Load of Full-Time Fac. | 44 (22) | 59 (17) | 59 (9) | 40 (27) |
| The Need to Use Temporary Fac. | 42 (18) | 44 (28) | 42 (31) | 35 (32) |
| Promotion-Tenure Process Above |  |  |  |  |
| Departmental Level | 24 (47) | 39 (26) | 15 (29) | 36 (22) |
| Advancing Age of Tenured Fac. | 29 (24) | 25 (31) | 14 (39) | 21 (41) |
| Lack of Experienced Senior Fac. | 11 (55) | 14 (48) | 15 (51) | 33 (52) |
| Losing Full-Time Faculty to |  |  |  |  |
| Industry/Government | 15 (48) | 10 (64) | 9 (65) | 51 (34) |

TABLE 3-8D

OTHER SUPPORT ISSUES

-     -         - Mathematics - - - Stat. Univ. Pu. 4-Yr. Pr. 4-Yr. Univ.

Upgrading/Maint. of Computer
Facilities $\quad 34$ (21) 42 (29) 46 (33) 48 (9)
Office/Lab Facilities $\quad 45$ (23) 30 (29) 19 (37) 50 (23)
Computer Facilities
(Classroom)
Classroom Lab Facilities
Computer Facilities (Fac. Use)
Networking Facilities
Library: Holdings,
Access, etc.
38 (18) $\quad 37$ (31) $\quad 40$ (23) $\quad 39$ (18)
41 (16) $22(25) \quad 26(33) \quad 29(20)$
31 (23) 33 (32) 25 (30) 39 (18)

26 (35) 30 (35) 16 (46) 27 (27)
$20(46) \quad 25(35) \quad 10(43) \quad 16$ (40)

## CHAPTER 4

## COMPUTER SCIENCE IN FOUR-YEAR COLLEGES AND UNIVERSITIES

In this year's Survey serious attempts were made to get more information concerning the status of computer science in undergraduate instruction. The titles of the Survey and questionnaire were changed to reflect the Survey's concern with undergraduate programs in the mathematical sciences and in the computer sciences. A special supplemental one page computer science questionnaire (see Appendix D) was sent to "those departments which offer undergraduate programs (not necessarily degree programs) in computer science."

## COMPUTER SCIENCE REFERENCES

Specific references to various aspects of computing and computer science will also be found in Tables: 1-1, 1-6A, 1-6B, 1-8, 1-9, 1-10, $2-3,2-4,2-5,2-7,2-8,2-9,2-10,2-11,2-13,2-15,2-16,2-17,2-18$, 2-19, 2-21, 3-3, 3-5, 3-6, 5-2, 5-3, 5-4, and 5-5.

The reader should refer to the beginning of Chapter 2 for explanations of faculty terms used in this report.

HIGHLIGHTS IN 1985

- Two-thirds of all universities, one-third of all public four-year colleges, and more than one-sixth of private four-year colleges have separate computer science departments. In the public four-year
college category the number is five-thirds that for 1980.
- There were 5,651 members of the full-time total computer science faculty of whom 3,605 were in computer science departments. There were 5,342 part-time computer science faculty of whom 1,984 were in computer science departments.
- Of the 3,754 doctorates who teach computer science full-time, 1,291 have their degrees in computer science and 1,555 in mathematics. Of the 2,231 doctorates who teach computer science part-time, 181 have their degrees in computer science whereas 1,369 have their degrees in mathematics.

1 Half of all part-time computer science faculty teach full-time in the same institution, almost a third are employed outside education and a tenth are not employed full-time anywhere.

- Half (49\%) of all computer science sections are taught in mathematics departments, the other $51 \%$ in computer science departments.
- In a substantial number of institutions, some computer science is taught outside mathematics and computer science departments, chiefly in business, engineering and education academic units.
- Total reported enrollments in computer science have climbed from 107,000 in 1975 to 321,000 in 1980 to 558,000 in 1985.
- There were 29,107 computer science undergraduate degrees in fiscal year 1984-85, with 8,646 of these in mathematics departments. In addition there were 3,084 joint majors with mathematics. The number of computer science degrees reported in the 1980 Survey for fiscal year 1979-80 was 8,917.
- About two-thirds of all institutions require calculus for computer science majors, one-half require linear or matrix algebra and more
than two-fifths require discrete mathematics.
- The most common problems reported by computer science departments are salary levels and patterns, departmental support services, the need to use temporary faculty, and the upgrading and maintenance of computer facilities.


## NUMBERS OF SEPARATE COMPUTER SCIENCE DEPARTMENTS

In all, 155 of the special computer science questionnaires were returned with the following overall distribution

|  | Univ. | Pu. 4-Yr. | Pr. 4-Yr. |
| :--- | :---: | :---: | :---: |
| By Math. Depts. | 13 | 42 | 36 |
| By Comp. Sci. Depts. | 35 | 22 | 7 |

reflecting the fact that in the universities there are many separate computer science departments whereas in the colleges some computer science is taught in many mathematics departments. These numbers are not identical with the numbers of such departments that returned the main questionnaire.

Based on estimates from reports from all institutions responding to any aspect of the questionnaire, the numbers of computer science departments in the various categories of institutions are given in Table 4-1 along with comparable data from the 1980 report.

TABLE 4-1

NUMBERS OF SEPARATE COMPUTER SCIENCE DEPARTMENTS With Numbers of Institutions

1980
Univ.
Pu. 4-Yr.
Pr. 4-Yr.

94 of 160
85 of 407
48 of 830

1985
105 of 157
141 of 427
150 of 839

Using data from both the special computer science questionnaire and the main questionnaire, we can identify many characteristics of those who taught computer science in 1985. We have numbers and various characteristics for the computer science departmental faculty and for the total computer science faculty, both full and part-time. The departmental faculty numbers are obtained from computer science departments on the main questionnaire. The total or overall faculty numbers are obtained from the special computer science questionnaire. The numbers for the faculty teaching computer science but not in computer science departments are obtained by subtracting the former from the latter. See Appendices B and D for copies of the questionnaires.

It is very important to note the implied definitions of the full-time and part-time components of the total computer science faculty. In Tables 4-2A through 4-6B, full-time (or part-time) refers to faculty teaching computer science full-time (or part-time). It does not refer to full-time (or part-time) faculty members at the institution. Table 4-5 makes it clear that about half of all part-time computer science faculty are, in fact, full-time at the same institution. In Table 4-8, there is a different analysis of computer science teaching phenomena wherein, for example, a full-time mathematics department faculty member teaching computer science part-time in the mathematics department would be classified as a full-time faculty member. It is worthwhile to compare the faculty and teaching divisions in Tables $4-2 A$ to $4-6 B$ with those in Table 4-8.

We begin by giving the numbers of the full-time and the part-time total computer science faculty in Tables 4-2A and 4-2B.

## FULL-TIME TOTAL COMPUTER SCIENCE FACULTY

|  | Univ. | Pu. $4-\mathrm{Yr}$. | $\underline{\text { Pr. }} \mathbf{4 - Y r}$. | Total |
| :---: | :---: | :---: | :---: | :---: |
| C.S. Depts. | 1,448 | 1,554 | 603 | 3,605 |
| Other Depts. | $\underline{91}$ | $\underline{853}$ | $\underline{1,102}$ | $\underline{2,046} \mathrm{Z}$ |
| Total | 1,539 | 2,407 | 1,705 | 5,651 |

TABLE 4 - 2B

PART-TIME TOTAL COMPUTER SCIENCE FACULTY

| Univ. | $\underline{\text { Pu. 4-Yr. }}$ | Pr. 4-Yr. | Total |
| :---: | :---: | :---: | :--- |
| 491 | 862 | 631 | 1,984 |
| $\underline{178}$ | $\underline{1,454}$ | $\underline{1,726}$ | $\underline{3,358} \leqslant$ |
| 669 | 2,316 | 2,357 | 5,342 |

The figures above are not surprising in light of the distribution of computer science departments as shown in Table 4-1. The part-time faculty will in many instances represent faculty in other departments at the same institution. See Table 4-5 for sources of part-time faculty. The fact that the number of part-time faculty is almost as large as the number of full-time faculty is of interest.

It should also be noted that in universities and colleges without computer science departments it would be expected that most, or in some cases all, of those who teach computer science would be part-time and generally borrowed from other departments.

In Tables $4-3 A$ and $4-3 B$ are given (1) the numbers of full-time and part-time computer science faculty with highest degrees in various categories and (2), in parentheses, the percentages of those counted who have the doctoral degree. Thus, in Table 4-3A, $83 \%$ of the 796 full-time computer science faculty in universities with highest degree in computer science have doctoral degrees in computer science. Of course, the numbers of faculty with highest degree in various areas can be read independently of the percentages of doctorates.

Tables $4-4 \mathrm{~A}$ and $4-4 \mathrm{~B}$ below give the numbers of doctorates on the total computer science faculty with degrees in various areas. The numbers in the "other" categories may seem large but "other" includes the various physical and social sciences.

TABLE 4 - 3A

FULL-TIME TOTAL COMPUTER SCIENCE FACULTY BY FIELD OF HIGHEST DEGREE

The Parenthetical Percentages Show Those With Doctorates

| Field of <br> Highest <br> Degree | $\underline{\text { Univ. }}$ |  | Pu. 4-Yr. | Pr. 4-Yr. | Total |
| :--- | :---: | ---: | ---: | ---: | ---: |
| Comp. Sci. | $796(83 \%)$ | $990(51 \%)$ | $627(20 \%)$ | $2413(54 \%)$ |  |
| Math. | $388(91 \%)$ | $899(83 \%)$ | $670(68 \%)$ | $1957(80 \%)$ |  |
| Engin. | $131(85 \%)$ | $89(87 \%)$ | $37(22 \%)$ | $257(76 \%)$ |  |
| Educ. | $45(69 \%)$ | $56(75 \%)$ | $114(68 \%)$ | $215(70 \%)$ |  |
| Stat. | $32(75 \%)$ | $32(0 \%)$ | $21(0 \%)$ | $85(29 \%)$ |  |
| Other | $\underline{147(88 \%)}$ | $\underline{341}(81 \%)$ | $\underline{236(56 \%)}$ | $\underline{724(74 \%)}$ |  |
|  |  |  |  |  |  |
| Total | $1539(85 \%)$ | $2407(68 \%)$ | $1705(47 \%)$ | $5651(67 \%)$ |  |

From the last column in Table 4-3A we compute that $43 \%$ of the full-time faculty teaching computer science have their highest degree in computer science. From Table 4-4A, we may note that only $34 \%$ of the doctorates teaching computer science have their doctorates in that field.

TABLE 4 - 3B

## PART-TIME TOTAL COMPUTER SCIENCE FACULTY BY FIELD OF HIGHEST DEGREE

## The Parenthetical Percentages Show Those With Doctorates

Field of Highest

| Degree | Univ. | Pu. 4-Yr. | Pr. 4-Yr. | Total |
| :--- | ---: | ---: | ---: | ---: |
| Comp. Sci. | $319(25 \%)$ | $820(10 \%)$ | $472(4 \%)$ | $1,611(11 \%)$ |
| Math. | $133(65 \%)$ | $845(60 \%)$ | $1,251(62 \%)$ | $2,229(61 \%)$ |
| Engin. | $68(57 \%)$ | $117(32 \%)$ | $122(48 \%)$ | $307(41 \%)$ |
| Educ. | $18(100 \%)$ | $88(67 \%)$ | $21(100 \%)$ | $127(77 \%)$ |
| Stat. | $23(48 \%)$ | $42(36 \%)$ | $68(68 \%)$ | $133(55 \%)$ |
| Other | $\underline{108(65 \%)}$ | $\underline{404(16 \%)}$ | $\underline{423(57 \%)}$ | $\underline{935(40 \%)}$ |
|  |  |  |  |  |
| Total | $669(45 \%)$ | $2,316(33 \%)$ | $2,357(49 \%)$ | $5,342(41 \%)$ |

The data in Tables $4-3 A$ and $4-3 B$ strongly support the evidence from Table 4-5 that a substantial part (50\%) of the part-time total faculty in computer science is full-time faculty in the same institution and from Table 4-8 that it has a large component which is full-time mathematics faculty teaching computer science courses within the mathematics department.

## DOCTORATE-HOLDING COMPUTER SCIENCE FACULTY

From the numbers and percentages in Tables $4-3 A$ and $B$ we can get a detailed analysis by their fields of degrees of those doctorates who teach computer science. Tables 4-4A and B below give these counts summed both ways. As in Tables $4-3 A$ and $B$ the counts are for all faculty teaching computer science.

TABLE 4 - 4A

DOCTORATES ON FULL-TIME TOTAL COMPUTER SCIENCE FACULTY

| Field of Doctorate | Univ. | Pu. 4-Yr. | Pr. 4-Yr. | Total |
| :---: | :---: | :---: | :---: | :---: |
| Comp. Sci. | 661 | 505 | 125 | 1,291 |
| Math. | 353 | 746 | 456 | 1,555 |
| Engin. | 111 | 77 | 8 | 196 |
| Educ. | 31 | 42 | 78 | 151 |
| Stat. | 24 | 0 | 0 | 24 |
| Other | 129 | 276 | 132 | 537 |
| Total | 1,309 | 1,646 | 799 | 3,754 |

There are two noteworthy observations from Table 4-4A.
(1) Of the doctorates who teach computer science full-time in universities, slightly more than half have their degrees in computer science and more than half of the rest have their degrees in mathematics.
(2) Of the doctorates who teach computer science full-time in the public and private colleges, almost half have their degrees in mathematics and more than half of the rest have their degrees in computer science.

DOCTORATES ON PART-TIME TOTAL COMPUTER SCIENCE FACULTY

| Field of Doctorate | Univ. | Pu. 4-Yr. | Pr. 4-Yr. | Total |
| :---: | :---: | :---: | :---: | :---: |
| Comp. Sci. | 80 | 82 | 19 | 181 |
| Math. | 86 | 507 | 776 | 1,369 |
| Engin. | 39 | 37 | 59 | 135 |
| Educ. | 18 | 59 | 21 | 98 |
| Stat. | 11 | 15 | 46 | 72 |
| Other | 70 | 65 | $\underline{241}$ | 376 |
| Total | 304 | 765 | 1,162 | 2,231 |

Almost two-thirds of the doctorates who teach computer science parttime in the public and private four-year colleges have their degrees in mathematics. A large number of part-time faculty with doctorates, particularly in the private college category, presumably are faculty from the same institution. Many of those with degrees in mathematics will be in mathematics departments as such, since mathematics departments in the college sectors teach a great deal of computer science. Note Table 4-5 where it is shown that $59 \%$ of all part-time computer science faculty in the private college sector are employed full-time in the same institution.

The sources of part-time computer science faculty in terms of their full-time employment is given in Table 4-5. Each column adds to $100 \%$.

TABLE 4-5

## SOURCES OF REGULAR EMPLOYMENT OF PART-TIME TOTAL COMPUTER SCIENCE FACULTY

Columns sum to $100 \%$

| Employed |  |  |  |  |  |
| :--- | ---: | :---: | :---: | :---: | :---: |
| Full-Time at: | Univ. | Pu. $4-Y r$. | Pr. 4-Yr. | All |  |
|  |  |  |  |  |  |
| Own Institution | $52 \%$ | $42 \%$ | $59 \%$ | $50 \%$ |  |
| Other Univ. or College | $7 \%$ | $2 \%$ | $5 \%$ | $4 \%$ |  |
| High School | $1 \%$ | $3 \%$ | $5 \%$ | $4 \%$ |  |
| Outside Education | $23 \%$ | $41 \%$ | $23 \%$ | $31 \%$ |  |
| Not Employed Full-time |  |  |  |  |  |
| $\quad$ Anywhere | $17 \%$ | $12 \%$ | $8 \%$ | $11 \%$ |  |

It seems reasonably clear that part-time computer science faculty members are selected from whatever resources are available. Many private colleges are in small towns where the source of part-time faculty would be the same institution. Public colleges are perhaps more likely to be in or near larger centers where non-academic personnel are available. The data tend to support this analysis.

About half of the part-time faculty in computer science are employed full-time in the same institution, with more than three-tenths employed full-time outside academia and more than one-tenth not employed full-time anywhere. Some retired persons or faculty spouses employed to teach part-time may be in this last category.

A question was designed to find how broadly competent the computer science faculty was judged to be: specifically, what percentages of the computer science faculty teach only lower-level courses or only specialty courses. It should be expected that much of the part-time faculty would be in such categories. From the responses recorded in Table 4-6B below it would appear that most chairpersons reported limits in qualifications in one or the other but not both "lower level" and "specialty" course categories.

TABLE 4 - 6A

PERCENTAGES OF FULL-TIME TOTAL COMPUTER SCIENCE FACULTY
TEACHING ONLY LOWER LEVEL OR SPECIALTY COURSES

|  | Univ. | Pu. 4-Yr. | Pr. 4-Yr. |  | Total |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Lower Level Courses | $11 \%$ |  | $18 \%$ |  | $31 \%$ |

TABLE 4 - 6B

PERCENTAGES OF PART-TIME TOTAL COMPUTER SCIENCE FACULTY TEACHING ONLY LOWER LEVEL OR SPECIALTY COURSES

|  | Univ. | Pu. 4-Yr. | Pr. 4-Yr. | Total |
| :---: | :---: | :---: | :---: | :---: |
| Lower Level Courses | 43\% | 58\% | 42\% | 49\% |
| Specialty Courses | 21\% | 11\% | 10\% | 12\% |

From Tables 4-6A and B we conclude that perhaps one-third of the full-time and three-fifths of the part-time computer science faculty teach only lower level or specialty courses.

FACULTY MOBILITY

Data on faculty mobility from academic year 1984-85 to academic year 1985-86 is available for the national faculty in computer science departments. Separate data for computer science faculty within mathematics departments is not available - the figures given in Table 2-20 are for faculty mobility in mathematics and statistics departments, including those who teach computer science there.

The data show an increase for the one year of 60 doctorate faculty and 88 non-doctorate faculty in computer science departments. From the nature of the question (\#9 on the main questionnaire) it is likely that figures from departments newly created for 1985-86 are not included. Thus the total size of the national computer science departmental faculty should have increased somewhat more. It is interesting that the outflow/ inflow ratios to/from non-academic employment are 52/32 for doctorates and 70/48 for non-doctorates. The ratios for mathematics and/or statistics departments are $157 / 76$ and $33 / 116$. At the doctorate level the ratios are not dissimilar. There were also approximately 120 doctorates and 40 non-doctorates who went from one computer science department (school) to another.

## TABLE 4-7

# MOBILITY OF THE FULL-TIME COMPUTER SCIENCE DEPARTMENTAL FACULTY 1984-85 To 1985-86 

|  | Doctorates | Non-Doctorates |
| :--- | :---: | ---: |
| Faculty Inflow |  |  |
| From Graduate School | 91 | 165 |
| From Post-Doctoral or Research Appts. | 21 | 0 |
| From Non-Academic Positions | 32 | 48 |
| From Other Sources | 6 | 0 |
|  |  |  |
| Total Inflow | 150 | 213 |
| Faculty Outflow |  |  |
| Died or Retired | 5 | 21 |
| Returned to Graduate School | 23 | 34 |
| To Non-Academic Positions | 52 | 70 |
| To Other Status | 10 | 0 |
| Total Outflow | 90 | 125 |

Data on the field of study of either doctorates or non-doctorates is not available in this mobility study. Presumably the doctorates (and the non-doctorates as well) who are going back to graduate school are seeking training in computer science, per se.

The net outflow to non-academic positions was about $1.2 \%$ of the total departmental faculty.

The number of sections of computer science taught by various components of the nation's four-year college and university faculty is shown in Table 4-8 below. The total number of sections taught in mathematics departments, 9,744 , is just under the total number taught in computer science departments, 10,102.

The definitions of "full-time and part-time faculty" are not the same as those used in Tables $4-2 A$ and $B$ and $4-3 A$ and $B$ and elsewhere in this chapter. The data for Table 4-8 came from the main questionnaire and part-time would refer to part-time in the department reporting. Thus mathematics department chairpersons would report a full-time departmental faculty member as "full-time" even though he/she taught only one or two computer science sections.

TABLE 4-8

## PERCENTAGE OF SECTIONS OF COMPUTER SCIENCE TAUGHT <br> (Columns sum to 100\%)

Math. Depts.
By Full-time Faculty
By Part-time Faculty
C.S. Depts.
$\begin{array}{llrll}\text { By Full-time Faculty } & 66 \% & 45 \% & 19 \% & 40 \% \\ \text { By Part-time Faculty } & 16 \% & 9 \% & 10 \% & 11 \%\end{array}$

From the $36 \%$ and $10 \%$ figures for public colleges and the $56 \%$ and $15 \%$ figures for private colleges it follows that in both public and private four-year college mathematics departments almost four-fifths of the computer science taught there is taught by full-time mathematics department faculty members. The data above seems generally consistent
with the data in Tables $4-2 A$ and $B$ to $4-4 A$ and $B$. In part, it corroborates the preponderance of mathematically trained faculty among the teachers of computer science.

The percentage of all computer science sections taught in computer science departments ranges from $82 \%$ in universities, to $54 \%$ in public four-year colleges to $29 \%$ in private four-year colleges. These data agree reasonably well with the current ratios of numbers of computer science departments to numbers of institutions, Table 4-1, with the caveat that institutions with separate computer science departments would be expected to teach relatively more computer science than would those without computer science departments.

OTHER UNITS TEACHING UNDERGRADUATE COMPUTER SCIENCE COURSES

Departments were asked to identify units other than mathematics or computer science departments within the institution which taught computer science courses. The responses are summarized in the following table.

TABLE 4-9

OTHER UNITS TEACHING SOME UNDERGRADUATE COMPUTER SCIENCE COURSES
Percentages Of All Institutions Responding

|  | Univ. | Pu. 4-Yr. | Pr. 4-Yr. |
| :---: | :---: | :---: | :---: |
| Business | 56\% | 53\% | 22\% |
| Engineering | 47\% | 22\% | 15\% |
| Education Plupieal | 20\% | 27\% | 9\% |
| Other Natural Science | 17\% | 6\% | 15\% |
| Computer Center | 8\% | 10\% | 2\% |
| Social Science | 4\% | 10\% | 4\% |
| $\triangle$ Humanities स्Qute | 4\% | 2\% | 0\% |
| Library | 0\% | 5\% | 0\% |

The figures reported do not seem surprising. Some forms of computer science are taught rather widely in the institutions. Since elementary data processing is not listed as a computer science course, per se (See Appendix $A$ or $E$ ), it seems likely that data processing in some form may account for much of the high incidence of teaching in the "business" category.

## COMPUTER SCIENCE COURSE ENROLLMENTS

Since computer science as a subject has developed only over the past quarter century as the computer age has gone from a few very expensive mainframes to minis and micros and hand calculators, there have, of course, been massive changes in student enrollments. Indeed, the nature of computer science and of specific course content continues to change with the changing technology. It was only in the 1970 Survey (after the curriculum guidelines of ACM-68 were issued) that a detailed listing of computer science courses (more than 2 at any level) was used by the Survey. It was only with this year's Survey that a name distinction was made between the mathematical and computer sciences and that a separate chapter on computer science was introduced in the report.

Table 4-10 gives the trend in enrollments in computer science. The course numbers refer to courses listed in Appendix E.

TABLE 4-10

TRENDS IN COMPUTER SCIENCE COURSE ENROLLMENTS BY LEVEL (in Thousands)

|  | 1960 | 1965 | 1970 | 1975 | 1980 | 1985 |
| :---: | ---: | ---: | ---: | ---: | ---: | ---: |
| Lower (55-61) | - | 2 | 64 | 63 | 206 | 350 |
| Middle (62-65) | - | 12 | 12 | 19 | 35 | 66 |
| Upper (66-92) | $\underline{9}$ | $\underline{8}$ | $\underline{30}$ | $\underline{31}$ | $\underline{80}$ | $\underline{142}$ |
| $\quad$ Total | 9 | 22 | 106 | 113 | 321 | 558 |

The computing or computer science courses for 1960 and 1965 were listed along with mathematics courses. The titles "Programming for Digital Computers" and "Other Computer Science Mathematics" suggest subject matter now identified chiefly with elementary and middle level courses.

The distribution of enrollments by level for 1970 to 1980 are "best estimates" from specific course enrollments given in the Survey reports. Only with the current Survey were the lower, middle and upper level designations used.

Computer science, along with mathematics and statistics, has a major service component for other disciplines. The fact that $63 \%$ of the 1985 course load is at the elementary level supports this view. However, the very large number of majors in computer science, Table 4-11, means that unlike mathematics and statistics, a sizable part of the upper level enrollment is for those within the discipline.

## COMPUTER SCIENCE STUDENTS

As noted in Chapter 1, Table 1-9, there were 29,107 computer science undergraduate degrees reported in 1984-85 plus another 3,084 joint majors with mathematics and 157 with statistics. Of the (single) computer science majors 20,416 were from computer science departments, 8,646 were from mathematics departments and 45 were from statistic departments. Of the joint majors with mathematics, 2,519 were from mathematics departments and 565 from computer science departments. Of the joint majors with statistics, all but nine were from computer science departments. As shown in Table 1-8, the reported numbers of computer science majors went from 3,636 in 1974-75 to 8,917 in 1979-80 to 29,107 in 1984-85.

The division of the computer science majors among universities, public four-year colleges and private four-year colleges is given in Table 4-11.

1984-85 COMPUTER SCIENCE UNDERGRADUATE DEGREES BY CATEGORY OF INSTITUTION AND DEPARTMENT (Does not include joint majors)

| Department | Univ. | Pu. 4-Yr. | Pr. 4-Yr. | Total |
| :---: | :---: | :---: | :---: | :---: |
| Comp. Sci. | 9,122 | 8,335 | 2,959 | 20,416 |
| Mathematics | 1,865 | 3,175 | 3,606 | 8,646 |
| Statistics | 45 | 0 | 0 | 45 |
| Total | 11,032 | 11,510 | 6,565 | 29,107 |

The 2,519 joint mathematics-computer science majors from mathematics departments were distributed as follows: 605 in universities, 1,102 in public four-year colleges and 811 in private colleges. Of the 565 joint mathematics-computer science majors from computer science departments, 136 were in universities, 169 in public and 260 in private four-year colleges.

## MATHEMATICS AND STATISTICS COURSES TAKEN BY COMPUTER SCIENCE MAJORS

The special computer science questionnaire sought information on (1) the total number of mathematics and statistics semester or quarter courses (at the calculus level or above) normally taken by computer science majors and (2) the mathematics and statistics courses required of computer science majors. The average (mean) numbers of mathematics and statistics courses normally taken by computer science majors are shown below in Table 4-12. Thus computer science majors take very little more mathematics and statistics courses than do engineering majors.

Robert M. Aiken, Chair of the Education Board of the ACM, who reviewed this report, expressed some surprise at the data in Tables 4-12 and 4-13 and their implications. He states, "My experience in consulting
with a number of programs and participating in computer science accreditation efforts leads me to believe that computer science majors take a minimum of two (mathematics and statistics) courses beyond the freshman-sophomore level." But he suggests that the fact that courses such as discrete mathematics (discrete structures) and numerical analysis are frequently taught within computer science departments and thus may be classified as computer science courses in this Survey may help explain the apparent discrepancy of his experience with Survey data.

TABLE 4-12

NUMBER OF SEMESTER OR QUARTER COURSES IN MATHEMATICS OR STATISTICS NORMALLY TAKEN BY COMPUTER SCIENCE MAJORS

Number of Courses
$\begin{array}{lccc}\text { Taken in } & \text { Univ. } & \text { Pu. 4-Yr. } & \frac{\text { Pr. 4-Yr. }}{4.3} \\ \text { Math/Statistics } & 5.4 & 4.3\end{array}$

The table below lists the percentages of schools in the university and college categories which require various mathematics and statistics courses for computer science majors. The courses are listed in approximate decreasing order of frequency of being required. All courses for which at least $10 \%$ of departments in any category of institution require the course are listed. The course numbers are those identifying the courses in the Survey questionnaire (Appendix B or E).

TABLE 4-13

## PERCENTAGES OF INSTITUTIONS REQUIRING THE GIVEN MATHEMATICS OR STATISTICS COURSE FOR COMPUTER SCIENCE MAJORS

|  |  | Univ. | Pu. 4-Yr. | Pr. $4-\mathrm{Yr}$. |
| :--- | :--- | :---: | :---: | :---: |
|  |  |  |  |  |
| 15 | Calculus (Math, Phys. Sci., Eng.)* | $88 \%$ | $61 \%$ | $69 \%$ |
| 19 | Linear Alg. \& Matrix Theory | $65 \%$ | $44 \%$ | $43 \%$ |
| 18 | Discrete Mathematics | $48 \%$ | $34 \%$ | $47 \%$ |
| 37 | Numerical Analysis | $27 \%$ | $24 \%$ | $24 \%$ |
| 47 | Math. Statistics (Calc. prereq.) | $29 \%$ | $15 \%$ | $13 \%$ |
| 27 | Discrete Structures | $21 \%$ | $13 \%$ | $17 \%$ |
| 17 | Differential Equations | $22 \%$ | $9 \%$ | $6 \%$ |
| 22 | Combinatorics | $13 \%$ | $5 \%$ | $0 \%$ |
| 45 | Elem. Stat. (no Calc. prereq.) | $6 \%$ | $13 \%$ | $12 \%$ |
| 46 | Prob. \& Stat. (no Calc. prereq.) | $3 \%$ | $2 \%$ | $12 \%$ |
| 48 | Probability (Calc. prereq.) | $12 \%$ | $5 \%$ | $11 \%$ |
| 50 | Applied Statistical Analysis | $5 \%$ | $10 \%$ | $0 \%$ |

* The questionnaire does not reveal explicitly whether one, two or more semesters (quarters) of calculus are required.

The results rather clearly support the view that undergraduate computer science has evolved (or is evolving) into a discipline quite distinct from mathematics. Only about $70 \%$ of institutions require computer science majors to take calculus, about $60 \%$ to take discrete mathematics or discrete structures, only about $50 \%$ to take linear algebra/matrix theory, about $50 \%$ to take some statistics course and $25 \%$ to take numerical analysis. Differential equations and combinatorics are required of only a small percentage of majors.

Furthermore, the fact that the average computer science major takes five or fewer semester (or quarter) mathematics or statistics courses suggests that only a fairly small percentage of computer science majors
opt for (or are advised to take) more than core courses in freshmansophomore mathematics. (But see the comments preceding Table 4-12).

## TYPES OF COMPUTER SCIENCE DEGREES

Schools (departments) teaching computer science were asked to identify the type of degree, if any, offered in computer science. Some institutions have several types of degrees. Because the questionnaire was directed to departments offering computer science, per se, it is likely that many business-oriented data processing programs were simply not included as respondents.

TABLE 4-14

PERCENTAGES OF SCHOOLS WHICH OFFER COMPUTER SCIENCE HAVING VARIOUS TYPES OF DEGREE PROGRAMS
(Columns Do Not Sum to 100\%)

| Type of Comp. Sci. |  |  |  |
| :--- | :---: | :---: | :---: |
| Degree | Univ. | Pu. $4-\mathrm{Yr}$. | Pr. $4-\mathrm{Yr}$. |
| None | $17 \%$ | $22 \%$ | $18 \%$ |
| Science | $79 \%$ | $64 \%$ | $77 \%$ |
| Business | $9 \%$ | $14 \%$ | $28 \%$ |
| Engineering | $18 \%$ | $5 \%$ | $5 \%$ |
| Education | $1 \%$ | $2 \%$ | $0 \%$ |
| Other | $0 \%$ | $6 \%$ | $2 \%$ |

In computer science courses with programming projects, minicomputers and mainframes were used much more widely than micro-computers. The use reported is given in Table 4-15.

TABLE 4-15

USE OF TYPES OF COMPUTERS IN COMPUTER SCIENCE PROGRAMMING PROJECTS Percentage of Students Enrolled at Given Levels

|  | Univ. | Pu. 4-Yr. | Pr. 4-Yr. |
| :--- | :---: | :---: | :---: |
| Lower Leve1 C.S. Courses | $35 \%$ |  |  |
| Micros | $65 \%$ |  | $30 \%$ |
| Minis/Mainframes |  | $60 \%$ | $39 \%$ |
|  |  |  | $61 \%$ |
| Middle or Upper Level C.S. Courses |  |  |  |
| Micros | $21 \%$ | $26 \%$ | $30 \%$ |
| Minis/Mainframes | $79 \%$ | $74 \%$ | $70 \%$ |

Thus about three-eighths of lower level students and one-fourth of middle or upper level students used micros in programming projects in computer science, the rest used minis or mainframes.

CONTROL OF WORK STATIONS

Data on the control of student work stations used in computer science courses are given in Table 4-16.

PERCENTAGE OF TEACHING DEPARTMENTS HAVING CONTROL OF STUDENT WORK STATIONS

|  | Univ. | Pu. 4-Yr. |  |
| :--- | :---: | :---: | :---: |
|  | $53 \%$ |  | $39 \%$ |
| Micros | $5-Y r$. |  |  |
| Minis/Mainframes | $21 \%$ | $28 \%$ | $61 \%$ |

Clearly departments teaching computer science in private colleges are much more likely to have control of student work stations, particularly for minis or mainframes. As expected, the teaching departments are more likely to control micro work stations than those for larger computers.

STUDENT ENROLLMENTS PER WORK STATION

For students taking computer science courses and using the computer in Fall 1985 we have the following pattern of work station availability.

$$
\text { TABLE } 4-17
$$

ENROLLED AND ACTIVE COMPUTER SCIENCE STUDENTS PER WORK STATION Percentage of Departments by Category Columns sum to $100 \%$

| No. of Students <br> Per Work Station | Univ. | Pu. 4-Yr. | Pr. 4-Yr. |
| :---: | :---: | :---: | :---: |
| $0-5$ | $12 \%$ |  | $24 \%$ |
| $6-10$ | $33 \%$ |  | $18 \%$ |
| $11-15$ | $38 \%$ | $29 \%$ | $60 \%$ |
| $16-20$ | $9 \%$ | $15 \%$ | $19 \%$ |
| 20 or more | $8 \%$ | $17 \%$ | $0 \%$ |

Thus in terms of the number of students sharing a work station, the private four-year colleges are, on the average, noticeably better off than the universities or public colleges.

## DEPARTMENTAL CONCERNS IN COMPUTER SCIENCE DEPARTMENTS

The Survey included two lists of questions, one on professional activities of faculty and how they affect faculty advancement and/or salary decisions and the second on problems of the mid-80's as seen by department chairpersons. Each question had a scale of 0 to 5 with zero representing no importance and 5 representing major importance. The results tabulated here are in the university, public four-year college and private four-year college categories for computer science departments. The numbers shown in the following tables in this chapter are (1) the projected percentage of all departments giving a 4 or 5 response for the particular question and (2), in parentheses, the projected percentage giving a 0 or 1 response for the same question. Obviously the percentage giving a 2 or 3 response can be found by subtracting the sum of the two percentages given from 100. The difference of the two numbers given is a measure of the preponderance of departmental attitudes regarding the issue as important.

The responses of departments in the mathematical sciences are given at the end of Chapter 3 in similarly designed tables. To assist the reader in comparing the two sets of data, the grouping and order of listing of issues for the mathematical sciences and computer science departments are the same. The issues are listed in approximate decreasing order of importance as viewed by departments in mathematics and statistics. Thus the grouping and order for computer science departments may seen unnatural.

TABLE 4-18

## IMPORTANCE OF PROFESSIONAL ACTIVITIES IN FACULTY ADVANCEMENT AND/OR SALARY DECISIONS

|  | Computer Science Departments |  |  |
| :---: | :---: | :---: | :---: |
|  | Univ. | Pu. 4-Yr. | Pr. 4-Yr. |
| Classroom Teaching Performance | 48 (1) | 90 (0) | 67 (0) |
| Published Research | 96 (0) | 60 (5) | 25 (33) |
| Service to Department and/or |  |  |  |
| University (College) | 37 (5) | 54 (0) | 46 (0) |
| Giving Talks at Profess. Mtgs. | 39 (8) | 43 (11) | 9 (49) |
| Professional Activities in Profess. |  |  |  |
| Societies and/or Pub. Service | 36 (0) | 21 (5) | 9 (16) |
| Supervision of Graduate Students | 40 (10) | 47 (16) | ------- |
| Undergraduate/Graduate Advising | 5 (31) | 31 (12) | 21 (33) |
| Years of Service | 5 (54) | 42 (22) | 63 (0) |
| Expository and/or Popular Articles | 10 (26) | 21 (14) | 9 (16) |
| Textbook Writing | 27 (25) | 14 (35) | 4 (66) |

Classroom teaching performance is relatively more important in college departments than in university departments whereas published research is much more important in university departments. Professional activities including talks and textbook writing are of considerable importance in university departments and of little importance in college departments whereas years of service are generally important only in college departments.

Generally the computer science departmental responses on professional activities were quite similar to the mathematics department responses given separately in Table 3-7.

## PROBLEMS OF THE MID-EIGHTIES

In the 23 questions on problems of the mid-80's there were several concerns where the responses stood out significantly. The results for four concerns are given separately in Table 4-19A. The remaining results are given in three tables, (1) those dealing with student issues, Table 4-19B, (2) those dealing with faculty issues, Table 4-19C and (3) those dealing with support issues, Table 4-19D. The concerns not commonly considered as major problems are almost as interesting as those considered important. Note that high percentages do not measure the intensity of feeling, as such, but rather the breadth of concern. Generally, those concerns identified as major problems are those which need addressing by the community. As is to be expected, for some concerns wide variations were reported among departments in the various types of universities and colleges and between departments in the mathematical and computer sciences. The responses for mathematics and statistics departments are summarized separately in Tables 3-8A to D.

The broad emphasis on salary and support issues identified in Table 4-19A means there is continuing pressure for upward salary adjustments and that there should be continuing pressure for better departmental support services. Clearly the larger community should be concerned with departmental support practices.

As in Table 4-18, the percentages of departments identifying the concerns as of major (minor) importance are given in Tables 4-19A to D.

TABLE 4 - 19A

MAJOR PROBLEMS

> Computer Science Departments Univ. Pu. 4-Yr. Pr. 4-Yr.

| Salary Levels/Patterns | 61 | $(1)$ | 89 | $(6)$ | $58 \quad(0)$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Departmental Support Services |  |  |  |  |  |
| $\quad$ (Travel, Secretarial, etc.) | 81 | $(1)$ | 60 | $(3)$ | $54(14)$ |
| Research Funding | $60(14)$ | $73(14)$ | $58(26)$ |  |  |
| Maintaining Faculty Vitality | $32(24)$ | 38 | $(3)$ | $25(66)$ |  |

TABLE 4 - 19B

STUDENT ISSUES

| Computer | Science D | rtments |
| :---: | :---: | :---: |
| Univ. | Pu. 4-Yr. | Pr. 4-Yr. |
| 14 (46) | 28 (25) | 37 (16) |
| 5 (80) | 9 (57) | 16 (34) |

Lack of Quality of Department
Graduate Students
29 (18)
12 (38)
Lack of Quantity of Department
Graduate Students
18 (43)
14 (56)
------*
Remediation
4 (46)
5 (48)
26 (37)
Class Size
49 (22)
40 (20)
30 (66)

* Since relatively few of the departments in this category have graduate programs, the responses are not given.


## TABLE 4 - 19C

OTHER FACULTY ISSUES

|  | Computer Science Departments |  |  |
| :---: | :---: | :---: | :---: |
|  | Univ. | Pu. 4-Yr. | Pr. 4-Yr. |
| Teaching Load of Full-Time Faculty | 43 (13) | 39 (19) | 51 (33) |
| The Need to Use Temporary Faculty | 58 (13) | 44 (19) | 51 (0) |
| Promotion-Tenure Process Above |  |  |  |
| Departmental Level | 42 (20) | 63 (20) | 33 (59) |
| Advancing Age of Tenured Faculty | 5 (60) | 3 (51) | 4 (86) |
| Lack of Experienced Senior Faculty | 52 (24) | 54 (10) | 63 (33) |
| Losing Full-Time Faculty to |  |  |  |
| Industry/Government | 32 (20) | 38 (21) | 41 (49) |

TABLE 4 - 19D

OTHER SUPPORT ISSUES

|  | Computer Science Departments |  |  |
| :---: | :---: | :---: | :---: |
|  | Univ. | Pu. 4-Yr. | Pr. 4-Yr. |
| Upgrading/Maint. of Computer |  |  |  |
| Facilities | 59 (21) | 60 (0) | 33 (30) |
| Office/Lab Facilities | 54 (0) | 54 (12) | 4 (49) |
| Computer Facilities (Classroom) | 33 (17) | 50 (0) | 21 (21) |
| Classroom Lab Facilities | 44 (5) | 40 (12) | 4 (70) |
| Computer Facilities (Faculty Use) | 30 (32) | 59 (14) | 21 (79) |
| Networking Facilities | 33 (41) | 49 (24) | 41 (59) |
| Library: Holdings, Access, etc. | 15 (34) | 17 (28) | 21 (0) |

The issue of maintaining faculty vitality (see Tables 3-8A and 4-19A) was a major problem in mathematics departments but not in computer science departments. The quality and quantity of undergraduate majors and of graduate students were minor problems in computer science but important problems in the mathematical sciences. It is interesting that losing faculty to industry or government was not considered a major concern for most computer science departments. Generally, the responses were consistent with commonly perceived faculty age and supply and demand phenomena in computer science. There were major differences in responses on several support issues between university and public college departments of computer science on the one hand and private college departments on the other. Generally private college departments are much better satisfied with computer access and availability, class size and facilities.

## CHAPTER 5

# MATHEMATICAL SCIENCE OFFERINGS, ENROLLMENTS, AND INSTRUCTIONAL PRACTICES IN THO-YEAR COLLEGES 

This chapter reports estimated national enrollments in two-year college (tyc) mathematical science courses for fall 1985. The data are compared and contrasted with results of previous CBMS surveys of 1966, 1970, 1975, and 1980 and with general enrollment trends in two-year colleges. For information on the sampling procedure used in this survey, see the Introduction and Appendix A.

HIGHLIGHTS
(1980-1985)

- Mathematical science enrollments remained almost unchanged, decreasing by $1 \%$.
- Overall tyc enrollments decreased by $2 \%$.
* Part-time students continued to account for nearly two-thirds of all tyc students.
* Nearly two-thirds of tyc associate degrees are now in occupational programs.
- Mathematical science faculty increased by $12 \%$. Full-time and part-time sectors each increased by $12 \%$.
- Courses showing increases were as follows:
* Statistics increased by 29\%.
* Calculus increased by $13 \%$.
* Remedial course enrollments reached 482,000, increasing by $9 \%$ since 1980. They now account for $47 \%$ of all tyc mathematical science enrollments and two-thirds of all remedial enrollments in higher education.
* Other precalculus increased by $4 \%$.
* Computing increased by $3 \%$.
- Courses showing decreases were as follows:
* Technical mathematics decreased by $56 \%$.
* Business mathematics decreased by $42 \%$.
* Mathematics for liberal arts decreased by 42\%. Enrollments in this course are now below 1966 levels.
- Access to computers increased and the impact of computers and calculators on mathematics teaching increased.
- Mathematics labs continued to grow in popularity and now can be found in $82 \%$ of two-year colleges.
. Self-paced instruction decreased sharply in the period 1980-1985.


## AN OVERVIEN OF THO-YEAR COLLEGES: <br> IS THE BOOM OVER?

During the $60^{\prime} \mathrm{s}$ and $70^{\prime} \mathrm{s}$, no other sector of higher education grew as rapidly as did two-year colleges. In the 60's their enrollments tripled; in the 70's they doubled. But in the 80's two-year college enrollment growth stopped; the period 1980-1985 showed an actual decrease. In 1960 two-year colleges accounted for only one-sixth of all undergraduate enrollments in mathematics. Today, the figure is nearly one-third.

Explosive growth of such proportions was accompanied by changes in programs, student populations, and faculty populations. In the early 60's, most two-year colleges had a liberal arts orientation, serving as feeders for four-year colleges. By the mid-60's, program emphases had undergone considerable change. A host of new programs in occupational areas were introduced: data processing, dental hygiene, electronics, practical nursing, automotive mechanics, accounting, bricklaying, carpentry, and police and fire science, to name a few. Today, less than half of two-year college students are enrolled in college transfer programs. The growing majority of students are enrolled in occupational programs, and two-thirds of associate degrees are in occupational programs.

Most of the students of the 60's were 18- and 19-year old high school graduates, planning to transfer to four-year colleges. Most of them were single, white, male, and attending on a full-time basis. Today, two-thirds of students are over 21, one-third are married, some lack high school diplomas, one-fourth are minority students, and more than one-half are women. Nearly two-thirds of these students are attending on a part-time basis, and one-half start their studies after age 21. Many of these students require training in remedial mathematics (arithmetic, high school geometry, elementary and intermediate algebra, and general mathematics). The growth of remedial courses has been dramatic; today they account for nearly half of all two-year college mathematics
enrollments. By way of contrast, calculus enrollments now account for only $10 \%$ of enrollments, down from $12 \%$ fifteen years ago but up slightly since 1980.

Faculty populations have also changed since 1960. Then nearly twothirds of full-time faculty had previously taught in high schools. Many of them entered two-year colleges expecting to move up to teach calculuslevel courses. In a short time, they found themselves teaching courses in arithmetic. Since then, economic pressures have resulted in a sharp swing toward the use of part-time faculty. In the mid-60's, full-timers outnumbered part-timers by two to one; today, part-timers outnumber fulltimers. Another aspect of the economic times is the phenomenon of overload teaching. At present, $43 \%$ of all full-time faculty in mathematics are teaching overloads, most for extra pay.

Self-paced instruction appeared in a variety of forms in the 60's and 70's: CAI, audio tutorial, television, modules, PSI, and film. With the current decrease in class sizes, we note a sharp decrease in their popularity.

Additional details on trends in course offerings, faculty populations, and changes in two-year college teaching environments are given in the following pages.

Two-year college enrollments total about 5,000,000. They decreased by $2 \%$ over the period 1980-1985.

During that five-year period, mathematical science course enrollments showed virtually the same percentage decrease. This is the first decrease we have observed in our regular surveys. See Graph 5-C for mathematical science enrollments.

GRAPH 5 - A

TRENDS IN OVERALL TWO-YEAR COLLEGE ENROLLMENTS, 1966-1985


Source: 1986 Community, Junior, and Technical College Directory, AACJC, One Dupont Circle, N.W., Washington, D.C. 20036.

## FULL-TIME VERSUS PART-TIME ENROLLMENTS IN TWO-YEAR COLLEGES,

 1966-1985Part-time enrollments overtook full-time enrollments in 1972. In 1985 part-time enrollments accounted for $65 \%$ of total enrollments.

GRAPH 5 - B

OVERALL FULL-TIME VERSUS PART-TIME ENROLLMENTS IN TWO-YEAR COLLEGES


* The sum of full-time and part-time enrollments does not agree with total enrollments given on the previous page because the AACJC totals include "non-respondent" projections.
Source: Community, Junior, and Technical College Directories 1967, 1972, 1976, 1981, and 1986.


## GROWTH OF ASSOCIATE DEGREES IN OCCUPATIONAL PROGRAMS <br> IN TWO-YEAR COLLEGES, 1970-1985

Since 1973-74 associate degrees in occupational programs have outnumbered associate degrees in college transfer programs. According to Cohen*, students in occupational programs tend to graduate at approximately the same rate as students in other programs. However, some students who transfer to four-year colleges do not complete associate degrees before transferring.

TABLE 5-1

ASSOCIATE DEGREES IN TWO-YEAR COLLEGE PROGRAMS

$$
\begin{array}{llll}
1970-71 & 1975-76 & 1980-81 & 1981-82
\end{array}
$$

OCCUPATIONAL
COLLEGE TRANSFER
42.6\%
55.2\%
62.6\%
63.5\%
57.4\%
44.8\%
37.4\%
36.5\%

Source: Digest of Educational Statistics 1983-84, National Center for Educational Statistics, Washington, D.C., p. 137.

TRENDS IN TWO-YEAR COLLEGE MATHEMATICS ENROLLMENTS

A slight decrease in mathematics enrollments marked the period 1980-1985. This is the first decrease noted since CBMS began monitoring enrollments in 1966. The decrease was fueled by large percentage drops in business mathematics (down $42 \%$ ), technical mathematics (down 53\%), and mathematics for liberal arts (down 42\%). Enrollments in mathematics for liberal arts are now one-half of the 1966 level.

Remedial courses continued to gain (up 9\%) and now account for $47 \%$ of

[^4]total enrollments. Calculus enrollments increased by $13 \%$ and statistics was up 29\%. Computing course enrollments slowed dramatically, growing by only $3 \%$ in the period 1980-1985. Computing course enrollments are nearly equal to calculus enrollments.

In 1980 we observed: "Courses of an applied nature showed the largest percentage increase in enrollments over the period 1975-1980, reflecting the greatly increased occupational/technical focus of two-year colleges." Five years later, enrollments in applied courses slowed, with technical mathematics and business mathematics decreasing. The continuing decline in business mathematics, first noted in 1980, is puzzling. Business mathematics enrollments also decreased in divisions outside mathematics.

## REMEDIAL COURSES

Since 1966, the growth of remedial courses has been large indeed. In fact, the remedial course group (arithmetic, general mathematics, elementary algebra, intermediate algebra, and high school geometry) now accounts for nearly one-half of all tyc mathematics enrollments. This growth has alarmed many individuals who are concerned about tyc mathematics.

In spite of the large overall enrollments, there is an indication that some improvement is occurring at the pre-algebra level (arithmetic and general mathematics): Over the period 1980-1985, pre-algebra enrollments decreased by $3 \%$, the first decrease noted since 1966.

ENROLLMENT TRENDS IN MATHEMATICAL SCIENCE COURSE GROUPS 1966-1985

Overall enrollments in mathematics courses decreased by $1 \%$ from 1980-1985 and thus mirrored the overall enrollment decrease of $2 \%$ in two-year colleges.

## GRAPH 5 - C

## MATHEMATICS COURSE ENROLLMENTS OVER TIME



Table 5-2 gives enrollment trends by various courses and Graph 5-D, percentage trends in various course groups. Remedial course enrollments continued to grow over the 1980-1985 period, but their rate of growth decreased. Since 1980 the percentage shares of calculus, precalculus, and statistics have remained nearly level.

The computing boom of 1975-1980 seems to be over. Course enrollments in computing (including data processing enrollments) are only slightly higher than they were in 1980.

TABLE 5-2
DETAILED FALL ENROLLMENTS IN MATHEMATICAL SCIENCES IN TWO-YEAR COLLEGES, 1966-1985 (in thousands)

| SUBJECT | 1966 | 1970 | 1975 | 1980 | 1985 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| REMEDIAL |  |  |  |  |  |
| 1 Arithmetic | 15 | 36 | 67 | 121 | 77 |
| R General Mathematics | 17 | 21 | 33 | 25 | 65 |
| 3 Elementary Algebra | 35 | 65 | 132 | 161 | 181 |
| 4 Intermediate Algebra | 37 | 60 | 105 | 122 | 151 |
| 5 High School Geometry | 5 | 9 | 9 | 12 | 8 |
| PRECALCULUS |  |  |  |  |  |
| 6 College Algebra | 52 | 52 | 73 | 87 | 90 |
| 7 Trigonometry | 18 | 25 | 30 | 33 | 33 |
| 8 College Alg. \& Trig. (Combined) | 15 | 36 | 30 | 41 | 46 |
| 9 Elementary Functions | 7 | 11 | 16 | 14 | 13 |
| CALCULUS |  |  |  |  |  |
| 10 Analytic Geometry | 4 | 10 | 3 | 5 | 6 |
| 11 Analytic Geometry \& Calculus | 32 | 41 | 40 | 45 | 49 |
| 12 Calculus (math., physics \& engr.) | 8 | 17 | 22 | 28 | 31 |
| 13 Calculus (bio., soc., \& mgt. sci.) | NA* | NA | 8 | 9 | 13 |
| 14 Differential Equations | 2 | 1 | 3 | 4 | 4 |
| SERVICE COURSES |  |  |  |  |  |
| 15 Linear Algebra | 1 | 1 | 2 | 1 | 3 |
| 16 Discrete Mathematics | NA | NA | NA | NA | L* |
| 17 Finite Mathematics | 3 | 12 | 12 | 19 | 21 |
| 18 Mathematics for Liberal Arts | 22 | 57 | 72 | 19 | 11 |
| 19 Mathematics of Finance | 4 | 5 | 9 | 4 | 1 |
| 20 Business Mathematics | 17 | 28 | 70 | 57 | 33 |
| 21 Math. for Elem. School Teachers | 16 | 25 | 12 | 8 | 9 |
| 22 Elementary Statistics | 4 | 11 | 23 | 20 | 29 |
| 23 Probability \& Statistics | 1 | 5 | 4 | 8 | 7 |
| 24 Technical Mathematics | 19 | 26 | 46 | 66 | 31 |
| 25 Technical Math. (calculus level) | 1 | 3 | 7 | 14 | 4 |
| 26 Use of Hand Calculators | NA | NA | 4 | 3 | 6 |
| COMPUTING |  |  |  |  |  |
| 27 Data Processing (elem. or adv.) | NA | NA | NA | NA | 36 |
| $28 \text { Elem. Progr. (BASIC, COBOL, }$ | 3 | 10 | 6 | 58 | 37 |
| 29 Advanced Programming | NA | NA | NA | NA | 5 |
| 30 Assembly Language Programming | NA | NA | NA | NA | 4 |
| 31 Data Structures | NA | NA | NA | NA | 2 |
| 32 Other Comp. Sci. Courses | 2 | 3 | 4 | 37 | 14 |
| 33 Other Mathematics Courses | 8 | 14 | 32 | 27 | 14 |
| TOTALS | 348 | 584 | 874 | 1048 | 1034 |
| *(NA means "not available" and | d L | ns s | but | ess th | 500. |

GRAPH 5 - D
FALL ENROLLMENTS IN SELECTED TYPES OF MATHEMATICAL SCIENCE COURSES
IN TWO-YEAR COLLEGES, BY LEVEL (As Percent of Total)


ENROLLMENTS IN THOUSANDS AND PERCENTAGES OF TOTAL

| LEVEL | $\stackrel{1966}{\text { NUMBER }}$ \% |  | $\stackrel{1970}{ }$ |  | $1975$ <br> NUMBER \% |  | $\begin{aligned} & 1980 \\ & \text { NUMBER } \end{aligned}$ |  | $\begin{array}{r} 1985 \\ \text { NUMBER } \% \\ \hline \end{array}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Remedial* <br> (Courses 1-5) | 109 | 31\% | 191 | 33\% | 346 | 40\% | 441 | 42\% | 482 | 47\% |
| $\begin{aligned} & \text { Precalculus** } \\ & (6-9) \end{aligned}$ | 92 | 26\% | 124 | 21\% | 149 | 17\% | 175 | 17\% | 182 | 18\% |
| Calculus (10-14) | 46 | 13\% | 69 | 12\% | 76 | 9\% | 91 | 9\% | 103 | 10\% |
| $\underset{(27-32)}{\text { Computing \& D.P. }}$ | 5 | 1\% | 13 | 2\% | 10 | 1\% | 95 | 9\% | 98 | 9\% |
| Statistics (22-23) | ) 5 | 1\% | 16 | 3\% | 27 | 3\% | 28 | 3\% | 36 | 3\% |
| Other | 91 | 26\% | 171 | 29\% | 266 | 30\% | 218 | 21\% | 133 | 13\% |

$\begin{array}{llllll}\text { Total } & 348 & 584 & 874 & 1048 & 1034\end{array}$
Note: This table was constructed using table on previous page. Percentages may not add to $100 \%$ due to rounding.

* Remedial courses include arithmetic, high school geometry, elementary algebra, intermediate algebra, and general mathematics (courses 1-5).
** Precalculus courses include college algebra, college algebra and trigonometry, trigonometry, and elementary functions (courses 6-9).

FIFTEEN YEAR TRENDS IN AVAILABILITY OF MATHEMATICS COURSES

Since 1970, remedial courses have become more widely available. In 1970, courses in arithmetic were taught in one-third of tyc's. In 1985, arithmetic was taught in more than one-half of tyc's. Calculus courses designed for engineering, science, mathematics, and physics are unchanged in availability since 1970. This steady availability may be explained in part by the introduction of new "soft" calculus courses designed for students in the biological, social, and managerial sciences. Soft calculus courses are available in $30 \%$ of tyc's.

Statistics is now taught in about three-fifths of tyc's; in 1970 it was taught in only two-fifths of tyc's.

The next table provides additional details on fifteen-year trends in availability. In contrast to the situation on availability of courses in four-year colleges where the questions asked were different in 1985 than in previous years (see the discussion preceding Table 1-7) the tyc questions for 1970 and 1985 seemed comparable. The results generally bear this judgment out. In the four-year college questionnaire, the issue was one of availability of upper division courses on a two-year cycle - an issue that hardly exists for two-year colleges where almost all courses would normally be taught every year.

TABLE 5-3
AVAILABILITY OF MATHEMATICAL SCIENCE COURSES IN TWO-YEAR COLLEGES
FIFTEEN-YEAR TRENDS, $1970-1985$
Percentage of two-year colleges teaching the course

| SUBJECT | FALL 1970 | FALL 1985 |
| :---: | :---: | :---: |
| REMEDIAL |  |  |
| 1 Arithmetic | 37\% | 53\% |
| 2 General Mathematics | 20\% | 41\% |
| 3 Elementary Algebra | 48\% | 75\% |
| 4 Intermediate Algebra | 56\% | 74\% |
| 5 High School Geometry | 24\% | 18\% |
| PRECALCULUS |  |  |
| 6 College Algebra | 53\% | 76\% |
| 7 Trigonometry | 64\% | 67\% |
| 8 College Alg. \& Trig. (Combined) | 41\% | 47\% |
| 9 Elementary Functions | 25\% | 21\% |
| CALCULUS |  |  |
| 10 Analytic Geometry | 18\% | 17\% |
| 11 Analytic Geometry \& Calculus | 63\% | 58\% |
| 12 Calculus (math., physics \& engr.) | 41\% | 41\% |
| 13 Calculus (bio., soc., \& mgt. sci.) | NA* | 30\% |
| 14 Differential Equations | 49\% | 40\% |
| SERVICE COURSES |  |  |
| 15 Linear Algebra | 17\% | 24\% |
| 16 Discrete Mathematics | NA | 3\% |
| 17 Finite Mathematics | 19\% | 27\% |
| 18 Mathematics for Liberal Arts | NA | 25\% |
| 19 Mathematics of Finance | 13\% | 5\% |
| 20 Business Mathematics | 38\% | 34\% |
| 21 Math. for Elem. School Teachers | 48\% | 31\% |
| 22 Elementary Statistics | 41\% | 61\% |
| 23 Probability \& Statistics | 16\% | 15\% |
| 24 Technical Mathematics | 41\% | 42\% |
| 25 Technical Math. (calculus level) | 19\% | 18\% |
| 26 Use of Hand Calculators | NA | 4\% |
| COMPUTING |  |  |
| 27 Data Processing (elem. or adv.) | NA | 28\% |
| 28 Elem. Progr. (BASIC, COBOL, FORTRAN, Pascal) | 27\% | 46\% |
| 29 Advanced Programming | NA | 19\% |
| 30 Assembly Language Programming | NA | 12\% |
| 31 Data Structures | NA | 5\% |
| 32 Other Comp. Sci. Courses | 16\% | 16\% |

* (NA means not available - not gathered in 1970)


## MATHEMATICS COURSES TAUGHT OUTSIDE OF MATHEMATICS PROGRAMS

We have previously noted the shift of two-year college enrollments to occupational programs. Many of these programs provide their own mathematics instruction. To get an approximation of the size of such "outside" offerings, we asked for estimates of enrollments in mathematics courses given by other divisions or departments. The estimates are probably not as reliable as other data presented in this report, because respondents did not have direct responsibility for these outside courses.

The majority of outside enrollments are found in computer science courses, data processing, and business mathematics. The divisions providing most of the outside courses are those which specialize in business and occupational programs.

In 1967, Jewett and Lindquist observed that "...The mathematics curriculum in junior colleges seems overwhelmingly designed for transfer students." Their words take on added importance in view of the continuing growth of occupational programs. Outside enrollments in mathematics and computer science, primarily in such programs, have nearly auadrupled since 1970 and are now estimated to be $35 \%$ of mathematics enrollments in mathematics programs. Without data processing, the estimate would be $20 \%$.

Trends in "outside" enrollments had some parallels with "inside" enrollments: business mathematics and technical mathematics decreased and computing courses demonstrated little change from 1980. Other trends may be seen in Tables 5-4 and 5-5.

In 1985, computer science and data processing are the most prominent courses for "outside" mathematics enrollments. Computer science accounts for $27 \%$ of "outside" enrollments, decreasing slightly from 1980. "Outside" enrollments in business mathematics have decreased by $29 \%$ since 1980. "Inside" business mathematics enrollments also decreased, but by 42\%. "Data processing" was not listed on previous surveys and may have been interpreted by some as "computer science and programming." If data processing is deleted, "outside" enrollments would have shown a decrease of $23 \%$. However, some data processing may have been included in computer science totals prior to 1985.

TABLE 5-4

## ESTIMATED ENROLLMENTS IN MATHEMATICS COURSES TAUGHT OUTSIDE OF MATHEMATICS PROGRAMS IN TYC'S, FALL 1985

(Enrollments in Thousands)

| COURSES | 1970 | 1975 | 1980 | 1985 |
| :--- | :---: | :---: | ---: | ---: |
| Arithmetic |  |  |  |  |
| Business Mathematics | 36 | 27 | 18 | 18 |
| Calculus or Differential Eqns. | L* $^{*}$ | 53 | 70 | 50 |
| Computer Science \& Programming | 21 | 51 | 8 | L |
| Data Processing | NA* | NA | NA | 159 |
| Pre-Calculus Coll. Mathematics | 6 | 17 | 29 | 37 |
| Statistics and Probability | 6 | 14 | 12 | 7 |
| Technical Mathematics | NA | NA | 25 | 23 |
| Other | 9 | 12 | 10 | 4 |
|  |  |  |  |  |
| Total | 92 | 178 | 264 | 361 |

[^5]Business and occupational program faculties teach substantial numbers of mathematics courses.

TABLE 5-5

ENROLLMENTS IN COURSES IN OTHER DIVISIONS
(Enrollment in Thousands)

| COURSES | NATURAL SCIENCES | OCCUPAT. PROGRAMS | BUSINESS | SOCIAL SCIENCES | OTHER | TOTAL |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Arithmetic | L* | 10 | 3 | 0 | 4 | 18** |
| Bus. Mathematics | 0 | 4 | 46 | 0 | L | 50 |
| Statistics \& Prob. | 0 | 0 | 4 | 2 | L | 7** |
| Pre-Calculus |  |  |  |  |  |  |
| College Math. | 0 | 3 | 0 | 0 | 0 | 3 |
| Calculus or |  |  |  |  |  |  |
| Diff. Eqns. | 0 | L | 0 | 0 | 0 | L |
| Comp. Sci. \& Prog. | L | 27 | 44 | 0 | 26 | 97 |
| Data Processing | 3 | 25 | 93 | 0 | 37 | 159** |
| Technical Math. | L | 23 | L | 0 | 0 | 23 |
| Other | 0 | 4 | 0 | 0 | 0 | 4 |
| Total | 3 | 96 | 190 | 2 | 67 | 361** |

* L denotes some but less than 500.
** denotes disagreement due to rounding.

The percentage of two-year colleges reporting access to computers has increased from $57 \%$ in 1975 and now amounts to $84 \%$ of all tyc's. The mean number of computer terminals and microcomputers available for student use in mathematics courses is 19, with a median of 13 . Department heads estimate that $59 \%$ of the full-time faculty know a computer language, the same percentage as in 1980. The number of faculty making use of computers in their teaching has doubled since 1975 and $32 \%$ of full-time faculty give some class assignments involving the use of the computer each year (in courses other than computer science). This figure is up from $21 \%$ in 1980. The impact of computers on mathematics teaching is growing but is still small; less than $7 \%$ of all sections of mathematics (excluding computer science) reported the use of computer assignments for students.

The impact of hand calculators on mathematics teaching is substantially larger than that of computers. Hand calculators are recommended for use in $43 \%$ of all course sections, up from $29 \%$ in 1980. Then, usage of calculators was concentrated in a small number of courses. Only courses in college algebra and trigonometry, trigonometry, statistics, and technical mathematics had usage rates in excess of $50 \%$. (That is, the fraction of sections in which hand calculators was recommended exceeded 50\%.) In 1985, 13 courses had usage rates over 50\%: analytic geometry and calculus, business mathematics, calculus, college algebra and trigonometry, elementary functions, finite mathematics, mathematics for liberal arts, mathematics of finance, probability and statistics, soft calculus, statistics, technical mathematics (calculus level), and trigonometry.

## INSTRUCTIONAL FORMATS FOR TWO-YEAR COLLEGE MATHEMATICS

The 1975 CBMS survey of two-year college mathematics noted the emergence of a variety of self-pacing instructional methods. The 1980 survey showed continued growth in use of self-pacing methods. The 1985 survey reveals a marked decrease in the use of self-pacing methods. The simplest explanation for this change is the decrease in teaching demands of faculty. From 1980-85
mathematical science enrollments decreased by $1 \%$ and the size of the faculty increased by $12 \%$. Some would argue that the use of self-pacing methods increased, in part, during the 70's as a result of overloaded classrooms (and teachers).

For each of eleven instructional methods, the table below shows the percentage of two-year colleges reporting no use, use by some faculty, or use by most faculty of that instructional method in mathematics courses in 1985. The pronounced increase in the percentages of tyc's reporting no use of various alternative systems clearly shows the decline in popularity of all non-traditional instructional methods.

TABLE 5-6
INSTRUCTIONAL FORMATS

INSTRUCTIONAL METHOD

| Not Being <br> Used | Used By Some <br> Faculty | Used By Most <br> Faculty ty |  |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 1980 1985 | 1980 1985 | 1980 | 1985 |

Standard Lecture-Recit. Sys.
(class size <or = to 40)
Large Lecture Classes
( $>40$ ) with recitation sections $\quad 63 \% \quad 77 \% \quad 16 \% \quad 19 \% \quad 21 \% \quad 4 \%$

Large Lecture Classes
(>40) with no recitation
Organized Program of
Independent Study
Courses by Television (closedcircuit or broadcast)
Courses by Film
Courses by Programmed Instruc.
Courses by Computer-Assisted
Instruction (CAI)
Modules
Audio-Tutorial
PSI (Personalized System of Instruction)
$76 \% \quad 81 \% \quad 12 \% \quad 17 \% \quad 12 \% \quad 1 \%$
$2 \% \quad 14 \% \quad 97 \% \quad 85 \%$

16\% 19\% 21\% 4\%
$37 \% \quad 61 \% \quad 62 \% \quad 38 \% \quad 1 \% \quad 2 \%$

| $73 \%$ | $91 \%$ | $27 \%$ | $9 \%$ | $0 \%$ | $0 \%$ |
| ---: | ---: | ---: | ---: | ---: | ---: |
| $75 \%$ | $96 \%$ | $24 \%$ | $4 \%$ | $1 \%$ | $0 \%$ |
| $40 \%$ | $69 \%$ | $56 \%$ | $27 \%$ | $4 \%$ | $4 \%$ |


| $68 \%$ | $74 \%$ | $31 \%$ | $24 \%$ | $1 \%$ | $2 \%$ |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $42 \%$ | $68 \%$ | $54 \%$ | $25 \%$ | $4 \%$ | $6 \%$ |
| $55 \%$ | $75 \%$ | $43 \%$ | $24 \%$ | $2 \%$ | $2 \%$ |

$51 \% \quad 76 \% \quad 46 \% \quad 20 \% \quad 3 \% \quad 4 \%$

## USE AND STAFFING OF MATHEMATICS LABORATORIES IN TWO-YEAR COLLEGES

Mathematics labs (math help centers, math tutorial centers) are relatively new adjuncts to mathematics instruction in two-year colleges. They may contain some or all of the following: tutors, calculators, computers, films, film strips, television units for playback of lectures or video cassettes, models, audio-tape units, learning modules, etc. Math labs have been established at a fairly constant rate since 1970 and can now be found in $82 \%$ of all two-year colleges, up from $68 \%$ in 1980. As shown in the table below, personnel of labs come from a variety of sources.

TABLE 5-7

SOURCES OF PERSONNEL FOR MATHEMATICS LABORATORIES

## Percent of TYC's Using Source

Students 48\%
Full-time Members of Mathematics Staff 38\%
Paraprofessionals 34\%
Part-time Members of Mathematics Staff 30\%
Members of Other Departments 19\%
Other $3 \%$

## COORDINATION OF COLLEGE-TRANSFER PROGRAMS WITH FOUR-YEAR INSTITUTIONS

For two-year colleges with large degree-credit programs it is important to coordinate program offerings, advisement, and academic standards with the most likely four-year college or university destination of their students. Sixty-six percent of the responding tyc's reported that their mathematics offerings are subject to state regulation, and thirty-five percent reported official state-wide coordination of tyc mathematics offerings with those of
four-year institutions.
This may help to explain the low level of reported consultation of tyc mathematics departments with four-year college and university departments: less than once a year for thirty-five percent, yearly for forty-one percent, and more than once a year for twenty-three percent.

## CHAPTER 6

## MATHEMATICAL SCIENCE FACULTY IN TWO-YEAR COLLEGES

This chapter describes the number, educational qualifications, professional activities, and selected personal characteristics of two-year college mathematical science faculty. For two-year colleges the terms "mathematical science" and "mathematics" describe the same faculty and are used interchangeably in that context. There is generally no separate computer science faculty. Computer science type courses are taught in many mathematics departments or divisions and as shown in Table 5-5, are also widely taught in occupational and business type programs. See the questionnaire, Appendix $C$, for interpretation of "mathematics department". The chapter includes profiles of the age, sex, and ethnic composition of mathematics faculty and information on mobility into, within, and out of two-year college teaching positions. Also included is a section on the teaching environment of mathematics faculty. While, prior to the 1980 report separate profiles were given for public and private tyc faculties, in the 1980 report the two faculties were combined, since only about $5 \%$ of the total faculty was in private tyc's. We continue this pattern started in 1980.

HIGHLIGHTS
1980-85

- The full-time mathematics faculty increased by $12 \%$ since 1980 and now numbers 6,277.
- The part-time mathematics faculty also increased by $12 \%$ and now numbers 7,433. Since 1980, part-timers have accounted for more than
one-half of the total mathematics faculty.
- The percentage of doctorates on the mathematics faculty decreased from $15 \%$ to $13 \%$ of the total, the first decrease noted by CBMS since 1970.
- The percentage of mathematics faculty having highest degrees in computer science increased from $3 \%$ to $8 \%$.
- The percentage of mathematics faculty having highest degrees in statistics increased to $3 \%$.
- Women on the mathematics faculty increased to $31 \%$, a gain of 10 percentage points in ten years.
- Ethnic minorities on the mathematics faculty increased to $12 \%$, up from 8\% in 1975.
- Overload teaching, usually for extra pay, remains prominent among tyc mathematics faculty, with $43 \%$ of faculty reported as teaching overloads.
\| Standard teaching loads decreased for the first time since 1970.
- Remediation was cited as the biggest problem facing mathematics departments in the mid-80's.

NUMBER AND EDUCATIONAL QUALIFICATIONS OF TWO-YEAR COLLEGE FACULTY

As of fall 1985, two-year colleges employed 93,611 full-time faculty and 135,195 part-time faculty. More than $75 \%$ hold a master's degree and $14 \%$ hold a doctorate. Since two-year colleges emphasize teaching and not research, two-year college faculty spend significantly more time in the classroom than do faculty in four-year colleges and universities. Most two-year college faculty teach about 16 hours per week.

Since more than $50 \%$ of all students enrolled at two-year colleges are taking courses in occupational fields, faculty trained and experienced in such areas as health technologies, business, data processing, and public service fields and disciplines that serve these fields are currently in greatest demand. Even so, our survey results show that the growth, since 1980, of the full-time equivalent (FTE) mathematics faculty was $12 \%$, in marked contrast to the $7 \%$ decrease of all two-year college faculty shown in Graph 6-A.

GRAPH 6 - A

NUMBERS OF FULL-TIME EQUIVALENT (FTE) TYC FACULTY, ALL FIELDS
(In Thousands)

FTE Faculty
SOURCE: 1986 Community, Junior, and Technical College Directory

## TRENDS IN NUMBERS OF FULL- AND PART-TIME MATHEMATICS FACULTY

For mathematics in two-year colleges, part-time faculty now outnumber full-time faculty, making up 54\% of the total. For all fields in tyc's, part-timers constitute $59 \%$ of the faculty. The part-time component of the mathematics faculty increased by $12 \%$ over the period 1980-1985, down sharply from the $95 \%$ increase observed in 1975-1980. The $12 \%$ increase in the size of the full-time faculty matched the increase of the part-time faculty.

GRAPH 6 - B

FULL- AND PART-TIME MATHEMATICS FACULTY DISTRIBUTION OVER TIME
(In Thousands)


TRENDS IN DOCTORATES AMONG FULL-TIME MATHEMATICS FACULTY

The percentage of doctorates among the full-time mathematics faculty in two-year colleges declined over the period 1980-1985. This ends a period of steady growth in the percentage of doctorates on mathematics faculty. The current figure of $13 \%$ is close to the $14 \%$ figure of doctorates on the total tyc faculty. The percentage of doctorates on the four-year college and university mathematical and computer science faculty also decreased over the period 1980-1985.

GRAPH 6 - C

PERCENTAGE OF DOCTORATES AMONG FULL-TIME MATHEMATICS FACULTY


## HIGHEST ACADEMIC DEGREES OF FULL-TIME MATHEMATICS FACULTY 1985

Table 6-1 gives the percentages of the total tyc mathematics faculty by field of highest degree and the level of that training. Since 1980 the percentages of the faculty holding highest degrees in statistics and in computer science went up markedly, from $1 \%$ to $3 \%$ in statistics and from $3 \%$ to $8 \%$ in computer science. But note that fewer than one-half of one percent had doctorates in these areas. Except for increases at the non-doctorate levels in computer science and statistics, the overall matrix for 1985 is very similar to that for 1980. The degree level "Masters +1" (or Mast. +1) refers to one year beyond the Masters level.

TABLE 6-1

TYC FULL-TIME MATHEMATICS FACULTY BY FIELD AND LEVEL OF HIGHEST DEGREE Degree Level

| Field | Doct. | Mast. +1 | Masters | Bachelors | Total |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Mathematics | 6\% | 26\% | 24\% | 2\% | 58\% |
| Statistics | 0\% | 1\% | 1\% | 1\% | 3\% |
| Computer Science | 0\% | 3\% | 4\% | 1\% | 8\% |
| Mathematics Educ. | 4\% | 6\% | 8\% | 0\% | 18\% |
| Other Fields | 3\% | 3\% | 6\% | 1\% | 13\% |
| Total | 13\% | 39\% | 43\% | 5\% | 100\% |

TABLE 6-2

DEGREE STATUS OF FULL-TIME TYC MATHEMATICS FACULTY, 1970-1985
(As Percent of Total Full-Time Mathematics Faculty)

| Highest Degree | 1970 | 1975 | 1980 | 1985 |
| :--- | ---: | ---: | ---: | ---: |
|  |  |  |  |  |
| Doctorate | $4 \%$ | $11 \%$ | $15 \%$ | $13 \%$ |
| Masters + 1 year | $47 \%$ | $35 \%$ | $38 \%$ | $39 \%$ |
| Masters | $42 \%$ | $47 \%$ | $42 \%$ | $43 \%$ |
| Bachelors | $7 \%$ | $7 \%$ | $5 \%$ | $5 \%$ |

AGE, SEX, AND ETHNIC COMPOSITION OF TWO-YEAR COLLEGE MATHEMATICS FACULTY

Since 1980 the full-time faculty in mathematics has increased by $12 \%$ at a time when there has been a percentage decrease in the group under age 40 and a percentage increase in the 40-49 age group. There are continuing indications that a substantial number of faculty in the over 45 age group are leaving two-year college mathematics teaching.

During the ten-year period 1975-85, the female percentage of two-year college full-time mathematics faculty has risen from $21 \%$ to $31 \%$, with a numerical increase in the number of female faculty from 1,250 in 1975 to 1,946 in 1985. From 1980 to 1985, the rate of growth of the number of women on the two-year college mathematics faculty was three times the growth rate of the overall mathematics faculty.

Ethnic minorities have continued to increase, from $8 \%$ of the total faculty in 1975 to $12 \%$ in 1985.

## TRENDS IN AGE DISTRIBUTION OF FULL-TIME MATHEMATICS FACULTY, 1975-1985

Trite as it may sound, the full-time tyc mathematics faculty is not getting any younger. In 1975, $47 \%$ of the faculty was under 40 years of age; today the figure is $34 \%$. Over the same ten year period, the percentage between 40 and 49 has increased from $28 \%$ to $42 \%$. The percentage of faculty over 50 years of age has remained fairly steady.

In Table 6-3 the trends since 1975 of the age composition of the full-time faculty are shown. The diagonal arrows indicate the translation of an age group to the corresponding five year older group five years later. Clearly, hiring occurs up to age 45 or 50. The table also indicates early retirements or dropouts among faculty who were over 45 years of age in 1980.

TABLE 6-3

AGE DISTRIBUTION OF FULL-TIME TYC MATHEMATICS FACULTY

|  | Percent of Full-Time Mathematics Faculty |  |  | Numb Mat | of Fu tics | Time ulty | Change: $1980-1985$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Age Range | 1975 | 1980 | 1985 | 1975 | 1980 | 1985 |  |
| $<30$ | 9\% | 5\% | 5\% | 535 | 28 | 314 | - 314 |
| 30-34 | 18\% | 15\% | 11\% | 1070 | 843 | 690 | - 409 |
| 35-39 | 20\% | 24\% | 18\% | 1188 | 1350 | 130 | - 287 |
| 40-44 | 15\% | 18\% | 24\% | 892 | 1012 | 506 | - 156 |
| 45-49 | 13\% | 16\% | 18\% | 773 | 900 | 130 | - 118 |
| 50-54 | 13\% | 10\% | 13\% | 773 | 562 | 816 | $\longrightarrow-84$ |
| 55-59 | 8\% | 7\% | 7\% | 475 | 394 | 439 | $\rightarrow-123$ |
| 60 or more | 4\% | 5\% | 4\% | 238 | 281 | 252 | $\rightarrow-142$ |
| Totals |  |  |  | 5944 | 5623 | 6277 |  |

# AGE DISTRIBUTION OF FULL-TIME MATHEMATICS FACULTY BY SEX, 1985 

From 1975 to 1985 the number of women on full-time mathematics faculties of two-year colleges has increased from $21 \%$ to $31 \%$ of the total. As might be expected, women are more heavily represented in younger age groups, with more than one-fourth less than 35 years of age. Only $28 \%$ of female faculty members are 45 or more years of age as contrasted to $48 \%$ of male faculty members. The total number of men is 4,331 and the total number of women is 1,946 .

## TABLE 6-4

1985 AGE DISTRIBUTION OF FULL-TIME FACULTY BY SEX

| Age Range | Male | Female |
| :---: | :---: | :---: |
| < 35 | 13\% | 26\% |
| 35-44 | 40\% | 45\% |
| 45-54 | 36\% | 19\% |
| 55 or more | 12\% | 9\% |

Totals may not be $100 \%$ due to rounding.

ETHNIC GROUPS AMONG FULL-TIME MATHEMATICS FACULTY, 1985

The ethnic-group distribution of the full-time mathematics faculty of two-year colleges in 1985 is shown in the Table 6-5. The total minority-group fraction is now 12\%, up from $8 \%$ in 1975. Hispanics registered the greatest gains. (The total number of non-Caucasian ethnic group faculty is 753.)

## TABLE 6 - 5

1985 ETHNIC GROUP DISTRIBUTION OF FULL-TIME FACULTY

| Ethnic Group | Percentage of Total |
| :--- | ---: |
|  |  |
| Caucasian | $88 \%$ |
| Asian | $3 \%$ |
| Hispanic | $4 \%$ |
| Black | $4 \%$ |
| American Indian | $1 \%$ |

The age distribution of the ethnic minority part of the full-time mathematics faculty of two-year colleges in 1985 is shown in Table 6-6. It differs from the overall faculty age distribution shown in Table 6-3 primarily in having a larger fraction under age 35 and a smaller fraction of age 55 or over, but is quite similar to the female faculty age distribution shown in Table 6-4.

TABLE 6-6

1985 AGE DISTRIBUTION OF ETHNIC MINORITY FACULTY

| Age Range | Percent of <br> Total Ethnic |
| :--- | :---: |
| < 30 | $27 \%$ |
| $35-44$ | $46 \%$ |
| $45-54$ | $20 \%$ |
| 55 or more | $7 \%$ |

The part-time faculty now numbers 7,433 and increased by $12 \%$ over the period 1980-1985, down sharply from a 95\% increase in 1975-1980. Overall, for all fields, part-timers account for $59 \%$ of the two-year college faculty. Mathematics, until the year 1980, used part-timers more sparingly than did other departments, but now the part-time fraction is 54\%. For all intents and purposes, mathematics faculty now have the dubious distinction of being on a vertical par with other departments.

As compared with the 1970 figures, the percentages of part-time mathematics faculty in the doctorate or "masters + 1" highest degree categories have declined. During the same fifteen-year period, the percentage of part-timers in the bachelors category has doubled and is now more than one-fourth of the total. Given an increase in the number of industrial opportunities for mathematicians, it is not likely that the educational qualifications of part-timers will soon increase.

TABLE 6-7

DEGREE STATUS OF PART-TIME MATHEMATICS FACULTY SINCE 1970
(As Percentage of Total Part-time Mathematics Faculty)

| Highest Degree | 1970 | 1975 | 1980 | 1985 |
| :--- | ---: | ---: | ---: | ---: |
|  |  |  |  |  |
| Doctorate | $9 \%$ | $4 \%$ | $7 \%$ | $7 \%$ |
| Masters + 1 | $31 \%$ | $30 \%$ | $18 \%$ | $15 \%$ |
| Masters | $46 \%$ | $49 \%$ | $58 \%$ | $50 \%$ |
| Bachelors | $14 \%$ | $17 \%$ | $17 \%$ | $28 \%$ |

HIGHEST ACADEMIC DEGREES OF PART-TIME MATHEMATICS FACULTY, 1985

As might be expected, the degree qualifications of the full-time faculty exceed those of the part-time faculty. Compare Table 6-8 below with Table 6-1.

TYC PART-TIME MATHEMATICS FACULTY BY FIELD AND LEVEL OF HIGHEST DEGREE

| Field | Percent with Highest Degree |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | Doctorate | Masters + 1 | Masters | Bachelors |
| Mathematics | 3\% | 8\% | 30\% | 17\% |
| Statistics | 1\% | 0\% | 0\% | 0\% |
| Computer Science | 0\% | 1\% | 1\% | 3\% |
| Mathematics Educ. | 1\% | 4\% | 7\% | 3\% |
| Other Fields | 2\% | 2\% | 12\% | 5\% |
| Totals | 7\% | 15\% | 50\% | 28\% |

For 1985, high school teachers constitute the largest source of parttime mathematics faculty in two-year colleges, as shown in Graph 6-D.

$$
\text { GRAPH } 6 \text { - D }
$$



# SOURCES OF NEW FULL-TIME MATHEMATICS FACULTY 

IN TWO-YEAR COLLEGES, 1985

Twenty-nine percent of new full-time mathematics faculty in 1985 entered two-year college mathematics teaching directly from graduate school. Teaching part-time in a two-year college continues to be a viable path to full-time status, with $25 \%$ of new hires coming from that source. High schools seem to be a smaller source of new faculty than they were earlier. A 1979 survey showed that more than $60 \%$ of all mathematics faculty in two-year colleges had previously taught in secondary schools.*

## TABLE 6-9

## INFLOW OF NEW FULL-TIME MATHEMATICS FACULTY 1985

| Source | Math. | Type of Do Math. Ed. | torate Other | None | Totals |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Graduate School | 17 | 0 | 2 | 134 | 153 |
| Employed by same tyc | 2 | 0 | 4 | 123 | 129 |
| Teaching in another tyc | 0 | 0 | 2 | 76 | 78 |
| Teaching in a secondary school | 0 | 7 | 4 | 59 | 70 |
| Non-academic employment | 0 | 0 | 0 | 39 | 39 |
| Teaching in four-year college or univer. | 2 | 0 | 2 | 13 | 17 |
| Otherwise occupied or unknown | 0 | 0 | 32 | 2 | 34 |
| Totals | 21 | 7 | 46 | 446 | 520 |

* Robert McKelvey, Donald J. Albers, Shlomo Liebeskind, and Don 0. Loftsgaarden, An Inquiry into the Graduate Training Needs of Two-Year College Teachers of Mathematics, Rocky Mountain Mathematics Consortium, 1979.


## FULL-TIME MATHEMATICS FACULTY LEAVING TWO-YEAR COLLEGES, 1985

The "death or retirement" category is at variance with the 1980 age distribution constructed by CBMS. The 1980 age distribution showed 5\% of the faculty to be over 60 years of age. Assuming retirement at an average age of 65 that translates to approximately 56 retirements per year. Our total of 217 is about four times that estimate and suggests other phenomena at work, perhaps early retirements. A substantial portion of the 55-59 age group left two-year college teaching between 1980 and 1985. Many of them may be in the retiree group. In contrast to retirement conditions in four-year colleges and universities, many two-year colleges may have retirement systems like the those in public school systems, thereby presumably encouraging early retirements.

TABLE 6 - 10

## OUTFLOW OF FULL-TIME MATHEMATICS FACULTY 1985

| Source | Math. | Math. Ed. | Other | None | Totals |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Died or retired | 10 | 10 | 2 | 195 | 217 |
| Teaching in 4-Yr. |  |  |  |  |  |
| College or Univ. | 10 | 0 | 5 | 47 | 62 |
| Teaching in a sec. school | 0 | 0 | 0 | 42 | 42 |
| Non-academic employment | 0 | 0 | 5 | 29 | 34 |
| Teaching in a $2-Y r$. College | 10 | 0 | 0 | 18 | 28 |
| Otherwise occupied or |  |  |  |  |  |
| Unknown | 0 | 0 | 0 | 66 | 66 |
| Returned to Grad. school | 0 | 0 | 0 | 0 | 0 |
| Totals | 30 | 10 | 12 | 397 | 449 |

# THE TEACHING ENVIRONMENTS OF MATHEMATICS FACULTY <br> IN TWO-YEAR COLLEGES 

There is evidence in our CBMS Survey data that the teaching environments of two-year college mathematics faculty have improved since 1980. The bulk of that evidence is contained in the next three tables dealing with the number of students taught by an average faculty member, professional activities, and problems of the mid-80's. These tables tell us the following about two-year college mathematics faculty over the period 1980-85:

1. Student loads per FTE faculty have decreased.
2. Professional activity of faculty has increased.
3. There is a greatly increased concern about the use of part-time faculty for instruction and a heightened interest in maintaining vitality of faculty.

TRENDS IN STUDENT LOADS FOR TWO-YEAR COLLEGE MATHEMATICS FACULTY

Student loads have decreased sharply in two-year college mathematics programs, down by 16 students per FTE faculty member. In 1985, mathematics program heads reported that $43 \%$ of the full-time faculty were teaching overloads, usually one additional course (3 semester hours) beyond the standard load of 16 contact hours. Department heads reported that not all faculty teaching overloads received additional pay for such work. They, in fact, reported that $29 \%$ of faculty teaching overloads did not receive extra compensation. This overload faculty work might mask an undercount of the part-time share in FTE faculty time and thus overestimate the number of students per FTE faculty member. For the faculty actually teaching the overloads, the added responsibility means they must provide mathematics instruction for even more students.

The total number of sections taught by part-time faculty was $11,900,28 \%$ of the total number of sections. This figure is supported by the FTE number of part-time faculty, 2,478, which is $28 \%$ of the total FTE faculty. (The average teaching load of full-time faculty is 16.1 contact hours and for part-timers it is 5.7). The ratio 5.7/16.1=0.35 provides support for the $1 / 3$ conversion factor used in computing FTE (full-time equivalent faculty) numbers.

## GRAPH 6 - E

## MATHEMATICS ENROLLMENTS PER FTE FACULTY MEMBER



Mathematics program heads in two-year colleges reported a continuing increase in professional activities of the faculty from 1975 to 1985. There is now more participation in conference attendance, reading of journals, and continuing education. Only textbook writing appears to have declined.

TABLE 6-11

## PERCENT OF FACULTY ENGAGING IN ACTIVITY

$\begin{array}{llll}\text { Activity } & 1975 & 1980 & 1985\end{array}$
$\begin{array}{lllll}\text { Attends at least one profess. mtg. per year } & 47 & 59 & 70\end{array}$ Taking additional math. or computer science
courses during the year 21
2122
31
Attend mini-courses or short courses NA* NA 31
$\begin{array}{llll}\text { Giving talks at professional meetings } & 9 & 15 & 16\end{array}$
$\begin{array}{lllll}\text { Regular reading of articles in prof. journals } & 47 & 57 & 72\end{array}$ Writing of expository and/or popular articles Publishing research articles Writing textbooks

NA
10311663

4
*NA denotes not available

## ADMINISTRATION OF MATHEMATICS PROGRAMS IN TWO-YEAR COLLEGES

Department heads have served in their positions for an average period of 8 years. Rotating department heads can be found in $22 \%$ of those twoyear colleges reporting the existence of a department head, with 3 years being the typical length of term. When asked to indicate the most serious problems they faced, the administrators mentioned most frequently the use
of temporary faculty, "dealing with remediation", the use of part-time faculty, salary patterns, and problems related to computer facilities.

TABLE 6 - 12

PROBLEMS OF THE MID-80's

|  | Rank | Percent Classifying Problem As Major |
| :---: | :---: | :---: |
| The need to use temporary faculty for instruction | 1 | 61\% |
| Remediation | 2 | 60\% |
| Salary levels/patterns | 3 | 53\% |
| Computer facilities for classroom use | 4 | 50\% |
| Departmental support sources (travel funds, staff, secretary, etc.) | 5 | 41\% |
| Maintaining vitality of faculty | 6 | 39\% |
| Staffing computer science courses | 7 | 34\% |
| Upgrading/maintaining computer facilities | 8 | 30\% |
| Computer facilities for faculty use | 9 | 27\% |
| Class size | 9 | 27\% |
| Advancing age of tenured faculty | 11 | 25\% |
| Coordinating math. courses for four-year colleges and universities | 12 | 22\% |
| Classroom/lab facilities | 13 | 21\% |
| Coordinating and/or developing math. with voc./tech. programs | 14 | 20\% |
| Coordinating math. courses with sec. schools | 15 | 19\% |
| Office/lab facilities | 15 | 19\% |
| Library: holdings, access, etc. | 17 | 7\% |
| Lack of experienced senior faculty | 17 | 7\% |
| Losing full-time faculty to industry/government | 17 | 7\% |

## APPENDIX A

## SAMPLING AND ESTIMATION PROCEDURES

## Sampling Procedure

The sampling frame was extracted from the 1982 National Center for Educational Statistics' HEGIS list which also gave Fall 1982 enrollments. The population frame consisted of those 2-year colleges, 4-year colleges or universities in the U.S.A., the District of Columbia or Puerto Rico that offered undergraduate Mathematics courses. There was a total of 2463 such institutions.

The population was divided into 22 strata on the basis of Control (Public or Private), Type (University, 4-year college or 2-year college) and Fall 1982 enrollment. This stratification is similar to but simpler than the one used for the 1980-81 CBMS study. Standard sampling techniques were used to determine the sample size for each stratum and then a random sample of institutions was chosen from each stratum.

Since the Stratification was based on enrollment, large schools were sampled much more heavily than small schools. Table A-1 gives a summary of the stratification.

Addresses were determined for sampled schools with the main sources of addresses being the 1985 Mathematical Sciences Administrative Directory and the 1985 Community, Technical, and Junior College Directory.

TABLE A-1

# NUMBER OF INSTITUTIONS IN EACH CONTROL/TYPE STRATUM AND SAMPLE SIZE IN EACH STRATUM 

| Control/Type | \# of Strata | Population | Sample |
| :--- | :---: | :---: | ---: |
| Public Universities | 4 |  |  |
| Private Universities | 3 | 95 | 46 |
| Public 4-Year Schools | 4 | 62 | 26 |
| Private 4-Year Schools | 4 | 837 | 105 |
| 2-Year Schools | $\underline{7}$ | $\underline{1040}$ | 80 |
| Total | 22 | 2463 | 172 |
|  |  |  | 429 |

Appropriate questionnaires were sent to all Mathematics Departments in the sampled institutions or to the Division in charge of Mathematics courses. In addition questionnaires were mailed to all Computer Science, Statistics or other Mathematical Sciences Departments that were determined to exist at the sampled schools. Two-year colleges had a different questionnaire than the other schools. In addition, two short questionnaires dealing with remedial Mathematics and Computer Science were mailed to appropriate departments. The questionnaires are discussed in more detail in the report and copies of all questionnaires are found elsewhere in Appendices $B$ to $D$.

Table A-2 summarizes the population and sample sizes for the separate Computer Science and Statistics Departments in four-year colleges and universities.

TABLE A - 2

NUMBER OF COMPUTER SCIENCE AND STATISTICS DEPARTMENTS IN POPULATION AND SAMPLE
Control/Type Population*Sample
Computer Science
Universities ..... 105 ..... 51
Public Colleges ..... 141 ..... 40
Private Colleges ..... 150 ..... 16
396 ..... 107
Statistics
Universities ..... 4021Public Colleges5ㄴ
45 ..... 23
*Population sizes are estimated from the sample.

Less than 10 Mathematical Sciences Departments other than Mathematics, Statistics and Computer Science were found in the sampled schools.

All projected enrollments in Mathematics courses and other information in this report are based on the information supplied by the Mathematical Sciences Departments mentioned earlier in this section. For example, no attempt was made to determine enrollments in Mathematics, Statistics or Computer Science courses that were taught in non-Mathematical or Computer Sciences Departments in four-year colleges or universities.

## Estimation Procedures

Course enrollments and other information in this report are estimated national figures for all institutions in the frame described earlier in this Appendix for Fall 1985. The projections were made using standard
procedures for stratified samples. For example, if stratum $\boldsymbol{i}$ has $N_{i}$ schools in it, $n_{i}$ schools respond with enrollments for course $A$ and $E_{i}$ is the total enrollment in Course $A$ reported by these $n_{i}$ schools, then the estimated total enrollment in Course $A$ in Stratum $i$ is given by:

$$
\frac{N_{i}}{n_{i}} \cdot E_{i}
$$

Required totals are then computed by adding estimates for appropriate strata.

The procedure used to handle separate Mathematical Sciences Departments at the same institution varied with the question. For course enrollments, data from all departments at each school were combined before projections were made. On the other hand, most information on faculty members was kept separate for the departments at each school.

Accuracy of Estimates

The response rates are given in Table A-3. They are down slightly from the 1980-81 study which had the highest response rates of any in this series of studies dating back to 1965-66.

## TABLE A - 3

## RESPONSE RATES IN DEPARTMENTS OF MATHEMATICS, STATISTICS, AND COMPUTER SCIENCE

Pop.* Sample Respondents Response | Rate |
| :---: |

1. Public Universities

| Mathematics | 95 | 45 | 38 | $83 \%$ |
| :--- | :--- | :--- | :--- | :--- |
| Statistics | 34 | 19 | 17 | $89 \%$ |
| Computer Science | 78 | 39 | 24 | $62 \%$ |

2. Private Universities

| Mathematics | 62 | 26 | 18 | $69 \%$ |
| :--- | ---: | ---: | ---: | ---: |
| Statistics | 6 | 2 | 2 | $100 \%$ |
| Computer Science | 27 | 12 | 8 | $67 \%$ |

3. Public Four-Year Colleges

| Mathematics | 427 | 105 | 81 | $77 \%$ |
| :--- | ---: | ---: | ---: | ---: |
| Statistics | 5 | 2 | 2 | $100 \%$ |
| Computer Science | 141 | 40 | 24 | $60 \%$ |

4. Private Four-Year Colleges

| Mathematics | 839 | 80 | 57 | $71 \%$ |
| :---: | ---: | ---: | ---: | ---: |
| Computer Science | 150 | 16 | 8 | $50 \%$ |
| 5. Two-Year Colleges | 1040 | 172 | 110 | $64 \%$ |

SUMMARY BY DEPARTMENT

| Mathematics | 1423 | 257 | 194 | $75 \%$ |
| :--- | ---: | ---: | ---: | ---: |
| Statistics | 45 | 23 | 21 | $91 \%$ |
| Computer Science | $\underline{396}$ | $\underline{107}$ | $\frac{64}{279}$ | $\frac{60 \%}{72 \%}$ |

*Figures for Statistics and Computer Science Departments were estimated from the sample.

Followup phone calls were made to all departments not responding by a certain date as was done in earlier studies. Later when the statistical
analysis was carried out, selected projections were made using only the first $60 \%$ of the questionnaires to be returned. These results agreed very well with the results for the entire data set.

The population frame (discussed earlier) had Fall 1982 enrollments for all schools. These enrollment figures for the responding schools were used to project total enrollments for all schools in the population. Actual enrollments were found by adding enrollments for all schools. Table A-4 contains a comparison of these results.

## TABLE A - 4

COMPARISON OF ACTUAL AND ESTIMATED ENROLLMENTS

|  | Estimated | Actual |  |
| :--- | ---: | ---: | ---: |
| Enrollment | Enrollment | Error |  |
| Universities | $2,866,665$ | $2,903,490$ | $-1.27 \%$ |
| Public Four-Year Colleges | $3,026,499$ | $2,978,696$ | $+1.60 \%$ |
| Private Four-Year Colleges | $1,515,073$ | $1,582,379$ | $\mathbf{- 4 . 2 5 \%}$ |
| Two-Year Colleges | $4,810,920$ | $4,642,187$ | $+3.63 \%$ |

A list of all responding departments is included as Appendix $F$.

## APPENDIX B

## FOUR-YEAR COLLEGE AND UNIVERSITY QUESTIONNAIRE (SEE PAGE B-8 FOR REMEDIAL QUESTIONNAIRE)

## SURVEY OF UNDERGRADUATE PROGRAMS

IN
THE MATHEMATICAL AND COMPUTER SCIENCES
1985

## General Instructions

You are asked to report on programs in the mathematical and computer sciences (including statistics) under the cognizance of your department. This same questionnaire is being sent to each department in the mathematical or computer sciences on your campus which is listed in the 1985 Mathematical Sciences Professional Directory published by the AMS. It is not being routinely sent to computer centers or to non-departmental groups or programs listed there. Do not include data for branches or campuses of your institution that are geographically or budgetarily separate. Questions 1-9 are generally quantitative and non-judgmental in nature. Questions $10-13$ involve more qualitative answers.

Please return completed questionnaire by 27 November 1985 to:
Conference Board of the Mathematical Sciences
1529 Eighteenth Street, N.W.
Washington, D.C. 20036
(202) 387-5200

*     *         * 

1. Name of your institution: $\qquad$
Name of your department:
2. Changes in Administrative Structure:
(a) Between 1980 and 1985 was your department, together with one or more other departments, consolidated into a larger administrative unit (e.g., a Division of Mathematical Sciences or Department of Electrical Engineering and Computer Science)? Yes __ No _
$\qquad$
Names of other departments involved in this consolidation $\qquad$

Name of larger administrative unit
(b) Between 1980 and 1985 was your department divided with part of your faculty entering a new department (e.g., a new department of Statistics or Computer Science?)

Yes $\qquad$ No $\qquad$
Name of new department(s) $\qquad$
(c) If you answered no to (a) and (b), was your present department created since 1980? $\qquad$ No $\qquad$
(d) Other major changes in administrative structure. Please specify:
$\qquad$


Appendix B - 2



Appendix B - 4





## APPENDIX C

# THO-YEAR COLLEGE QUESTIONNAIRE (SEE PAGE C-6 FOR REMEDIAL QUESTIONNAIRE) 

## SURVEY OF PROGRAMS IN MATHEMATICS

IN
TWO-YEAR COLLEGES
1985
General Instructions
This questionnaire should be completed by the person who is directly in charge of the mathematics program at your institution.

You are asked to report on all the courses and faculty in your institution which fall under the general heading of the mathematical or computer sciences except for remedial programs taught in a special unit outside the mathematics department. For some colleges this may involve courses and faculty in statistics, applied mathematics and computer science that, although mathematical in nature, are taught outside the mathematics department. If your institution does not have a departmental or divisional structure, consider the group of all mathematics and computer science professors to be the "mathematics department" for the purpose of this questionnaire. Question III below refers to courses taught in the "mathematics department" as explained above. Question IV refers to mathematics and/or computer science courses taught outside the "mathematics department" but not courses taught in a special unit for remediation. Courses in a special unit for remediation taught outside the mathematics department should be reported by the head of that unit in the special questionnaire on remediation (blue page.) Please include data on part-time and evening students and faculty as well as data on occupational and terminal programs. Include non-credit and remedial courses. Do not, however, include data concerning campuses jurisdictionally separate from yours, if such exist.

If the mathematics department offers the remedial program, then the person in charge of the mathematics department should fill in and return the special remediation questionnaire. If another unit offers the remedial program, then the person in charge of that unit should fill out and return the special remediation questionnaire which will be sent to him/her following receipt of the return postcard.

Please return completed questionnaire by 27 November 1985 to:
Conference Board of the Mathematical Sciences
1529 Eighteenth Street, N.W.
Washington, D.C. 20036
(202) 387-5200

I. A. NAME OF INSTITUTION $\qquad$
If this two-year institution is part of a larger organization, identify this relationship: $\qquad$
B. Total institutional enrollment Fall 1985 (approximate):

|  | $\begin{gathered} \frac{\text { College Transfer Program }}{\text { Full-time Part-time }} \\ \text { Students } \end{gathered}$ | Occupational/TechnicalFull-time Part-time <br> Students |
| :---: | :---: | :---: |
| Freshman |  |  |
| Sophomores |  |  |
| Unclassified or other |  |  |
| Total |  |  |







## APPENDIX D

## SPECIAL QUESTIONNAIRE ON COMPUTER SCIENCE

## SPECIAL COMPUTER SCIENCE QUESTIONNAIRE

This part of the questionnaire is designed for those departments which offer undergraduate programs (not necessarily degree programs) in computer science. It is limited to courses in computer science and the faculty which teach them. It is intended to give more detailed information about computer science itself than that recorded in the general survey. Summary information on your faculty has been included in the main questionnaire. All questions refer to Fall 1985 data. For computer science departments, per se, a few of the questions may be duplicates.

1. A. Which of the following subject areas best describes the Computer Science bachelor's degree(s), if any, offered by your department (check as many as apply):
$\qquad$ No bachelor's degree in computer science
$\qquad$ Science (Liberal Arts and Science)
$\qquad$ Engineering
$\qquad$ Business
$-\quad 25-26$

-     - $^{27-28}$
$-\quad 29-30$
B. Which, if any, departments or units (other than your own) on your campus teach undergraduate computer science courses (check as many as apply):
Mathematics
Engineering
Business
Other Natural Science
 Library

$$
-\quad 33-34
$$

$$
\begin{array}{r}
35-36 \\
27 \quad 20
\end{array}
$$

2. A. Percentage of students enrolled in departmental Computer Science courses with

$$
\begin{aligned}
& -37-3 \\
& -\quad 39
\end{aligned}
$$ programming projects using:

$\left.\begin{array}{c|c|c|c|} & \text { Micros } & \text { Minis/Mainframes } & \text { Total } \\ \hline \text { 3C of main questionnaire in }\end{array}\right)$
B. Percentage of work stations used in departmental Computer Sciences courses controlled by:

|  | Department | Non-Department | Total |
| :--- | :--- | :--- | :--- |
| Micros |  |  | $100 \%$ |
| Minis/Mainframes |  |  | $100 \%$ |

C. Consider the number of students taking departmental computer science courses and using the computer in Fall 1985. Check the average number of student enrollments per work station
$\qquad$
$\qquad$ ; 6-10 $\qquad$ ; 11-15; $\qquad$ ; 16-20 $\qquad$ ; 21 or more $\qquad$ .
3. A. Of the non-computer science courses listed in $3 A$ of the main questionnaire, encircle (by code numbers in $3 A$ ) those required for computer science majors. $\begin{array}{llllllllllllllllllll}15 & 16 & 17 & 18 & 19 & 20 & 21 & 22 & 23 & 24 & 25 & 26 & 27 & 28 & 29 & 30 & 31 & 32 & 33 & 34\end{array}$ $\begin{array}{llllllllllllllllllllllll}35 & 36 & 37 & 38 & 39 & 40 & 41 & 42 & 43 & 44 & 45 & 46 & 47 & 48 & 49 & 50 & 51 & 52 & 53 & 54\end{array}$

4. A. Full-time Computer Science faculty. Report the number of full-time computer science faculty in your department in the table below, by the highest degree and subject field in which it was earned (if the number is zero, check here (The numbers should total to your full-time computer science faculty.)

|  | Field |  | CS | Stat | Math | Educ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Highest degree | Engin | Other |  |  |  |  |
| Doctor's degree |  |  |  |  |  |  |
| Master's degree |  |  |  |  |  |  |
| Bachelor's degree |  |  |  |  |  |  |

$\qquad$ ): -49
$50-61$
$\frac{62-73}{\left[\frac{13}{3}\right.}$
B. Part-time Computer Science faculty, other than your teaching assistants. Report the number of faculty teaching Computer Science part-time in your department in the table below, by highest degree and subject field in which it was earned: (If the number is zero, check here $\qquad$ .)

| Highest degree Field | CS | Stat | Math | Educ | Engin | Other |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Doctor's degree |  |  |  |  |  |  |
| Master's degree |  |  |  |  |  |  |
| Bachelor's degree |  |  |  |  |  |  |

C. Of the part-time computer science faculty reported in $4 B$ above, how many were
(a) Employed full-time by your university or college
(b) Employed full-time by some other university or college
(c) Employed full-time by a high school
(d) Employed full-time but not in education
_ (e) Not employed full-time anywhere
D. How many of the full-time and part-time departmental faculty reported in 4 A and 4 B teach:

|  | Full-time | Part-time |
| :--- | :--- | :--- |
| (a) basically only lower level courses? |  |  |
| (b) only specialty courses? |  |  |

E. Of the faculty reported in $4 A$ and $4 B$ above, how many have joint appointments in Computer Science and:
$\quad$ Mathematics
Engineering
Business

Library | Science |
| :---: |
| $* * *$ |

Other Natural Sciences

- Social Sciences
- Humanities
_ Research Institutes
Other

Information supplied by: $\qquad$ Title \& Dept.: $\qquad$
Institution \& Campus: $\qquad$ Phone: $\qquad$
Date: $\qquad$
Please return completed questionnaire by 27 November 1985 to:
Conference Board of the Mathematical Sciences
1529 Eighteenth Street, N.W.
Washington, D.C. 20036

## APPENDIX E

COURSE BY COURSE ENROLLMENTS IN UNIVERSITIES AND FOUR-YEAR COLLEGES (In Thousands)

Sums may not total, because of rounding.
(L means some but less than 500)

| Name of Course (or equivalent) | Universities | $\begin{aligned} & \text { Public } \\ & \text { Colleges } \\ & \hline \end{aligned}$ | Private Colleges | Total |
| :---: | :---: | :---: | :---: | :---: |
| A. MATHEMATICS |  |  |  |  |
| Remedial |  |  |  |  |
| 1. Arithmetic | 3 | 8 | 4 | 15 |
| 2. General Math. (basic skills, operations) | 2 | 18 | 11 | 31 |
| 3. Elem. Algebra (High School) | 15 | 52 | 8 | 75 |
| 4. Intermed. Alg.(High School) | 36 | 77 | 17 | 130 |
| Total Remedial | 56 | 155 | 40 | 251 |
| Pre-calculus |  |  |  |  |
| 5. College Algebra | 53 | 73 | 25 | 150 |
| 6. Trigonometry | 12 | 22 | 3 | 37 |
| 7. College Alg. \& Trig. combined | 31 | 35 | 12 | 78 |
| 8. Elem. Functions, Pre-calc. Math. | h. 26 | 30 | 18 | 74 |
| 9. Math. for Liberal Arts | 12 | 30 | 17 | 59 |
| 10. Finite Mathematics | 35 | 30 | 23 | 88 |
| 11. Business Mathematics | 12 | 22 | 3 | 37 |
| 12. Math. for Elem. School Teachers | s 12 | 31 | 10 | 54 |
| 13. Analytic Geometry | L | 2 | 1 | 3 |
| 14. Other Pre-calculus | 7 | 5 | 1 | 13 |
| Total (Non-remedial) Pre-calc. | . 200 | 280 | 113 | 593 |
| Calculus Level |  |  |  |  |
| 15. Calc. (Math., Phys. Sci. \& Eng.) | .) 162 | 163 | 77 | 402 |
| 16. Calc. (Bio., Soc. \& Mgmt. Scis.) | .) 73 | 49 | 8 | 129 |
| 17. Differential Equations | 22 | 18 | 6 | 45 |
| 18. Discrete Mathematics | 5 | 8 | 2 | 14 |
| 19. Linear Alg. and/or Matrix Theory | ry 19 | 20 | 8 | 47 |
| Total Calculus | 281 | 258 | 101 | 637 |
| Advanced Level |  |  |  |  |
| 20. Modern Algebra | 5 | 6 | 2 | 13 |
| 21. Theory of Numbers | 1 | 1 | 1 | 3 |
| 22. Combinatorics | 2 | 3 | L | 4 |
| 23. Graph Theory | 1 | L | L | 1 |
| 24. Coding Theory | - | L | - | L |
| 25. Foundations of Mathematics | 1 | 2 | 1 | 3 |
| 26. Set Theory | L | 1 | - | 1 |
| 27. Discrete Structures | 1 | 3 | 3 | 7 |


| Name of Course (or equivalent) | Universities | Public Colleges | Private Colleges | Total |
| :---: | :---: | :---: | :---: | :---: |
| A. MATHEMATICS |  |  |  |  |
| Advanced Level (Continued) |  |  |  |  |
| 28. History of Mathematics | L | 1 | - | 2 |
| 29. Geometry | 2 | 4 | 1 | 7 |
| 30. Math. for Secondary School Teachers (Methods, etc.) | 1 | 3 | 1 | 5 |
| 31. Mathematical Logic | 1 | L | 1 | 2 |
| 32. Advanced Calculus | 5 | 6 | 3 | 14 |
| 33. Advanced Math. for Eng. \& Physics | 4 | 5 | 1 | 10 |
| 34. Vector Analysis. Linear Algebra | ra 4 | 8 | 2 | 14 |
| 35. Advanced Diff. Equations | 1 | 2 | L | 4 |
| 36. Partial Diff. Equations | 1 | 3 | - | 5 |
| 37. Numerical Analysis | 5 | 7 | 2 | 13 |
| 38. Applied Mathematics, Math. Modelling | 1 | 1 | 1 | 4 |
| 39. Operations Research | 3 | 2 | 1 | 6 |
| 40. Complex Variables | 2 | 2 | 1 | 5 |
| 41. Real Analysis | 2 | 2 | 2 | 5 |
| 42. Topology | 1 | L | L | 2 |
| 43. Senior Seminar/Independ. Stud. Mathematics <br> 44. Other Mathematics | $\begin{array}{r}L \\ \hline\end{array}$ | 1 | 1 | 2 |
| Total Advanced Level | 47 | 66 | 25 | 138 |
| B. STATISTICS |  |  |  |  |
| 45. Elem. Stat. (no Calc. prereq.) | ) 40 | 41 | 34 | 115 |
| 46. Probability (\& Stat.) <br> (No Calc. prerequisite) | 12 | 13 | 5 | 29 |
| 47. Mathematical Statistics (Calc.) | ) 10 | 9 | 6 | 24 |
| 48. Probability (Calculus) | 7 | 5 | 3 | 15 |
| 49. Stochastic Processes | $L$ | - | - | L |
| 50. Applied Stat. Analysis | 7 | 3 | 1 | 11 |
| 51. Design \& Analysis of Experiments | ts 1 | L | - | 1 |
| 52. Regression (and Correlation) | 1 | L | - | 1 |
| 53. Senior Seminar/Indep. Stud. Stat. | tat. L | - | - | L |
| 54. Other Statistics | 11 | 1 | L | 12 |
| Total - All Statistics | 89 | 72 | 49 | 208 |
| C. COMPUTER SCIENCE |  |  |  |  |
| Lower Level |  |  |  |  |
| 55. Computers \& Society | 10 | 36 | 23 | 69 |
| 56. CS1 '78 or CS1 ' 84 (Computer Programming I) | 36 | 50 | 43 | 129 |
| 57. CS2 ${ }^{\prime} 78$ (Computer Prog. II) | 6 | 13 | 8 | 28 |


| Name of Course (or equivalent) Univ | Universities | Public Colleges | Private Colleges | Total |
| :---: | :---: | :---: | :---: | :---: |
| C. COMPUTER SCIENCE |  |  |  |  |
| Lower Level (Continued) |  |  |  |  |
| 58. CS2, '84 | 4 | 7 | 4 | 15 |
| 59. Database Mgmt. Systems | 1 | 4 | 2 | 7 |
| 60. Discrete Mathematics | 3 | 8 | 2 | 12 |
| 61. Other Lower Level Service | 34 | 37 | 19 | 90 |
| Total Lower Level | 94 | 155 | 101 | 350 |
| Middle Level |  |  |  |  |
| 62. Intro. to Comp. Systems (CS3) | 4 | 11 | 3 | 18 |
| 63. Assembly Lang. Programming | 6 | 13 | 5 | 24 |
| 64. Intro. to Comp. Organization | 5 | 6 | 3 | 14 |
| 65. Intro. to File Processing (CS5) | 5) 3 | 4 | 2 | 10 |
| Total Middle Level | 18 | 34 | 13 | 66 |
| Upper Level |  |  |  |  |
| 66. Operating Sys. \& Computer Arch. | h. 2 | 1 | 1 | 4 |
| 67. Operating Systems | 4 | 5 | 2 | 11 |
| 68. Computer Architecture | 2 | 2 | 2 | 6 |
| 69. Data Structures (CS7) | 7 | 10 | 7 | 24 |
| 70. Survey of Prog. Languages | 3 | 5 | 1 | 9 |
| 71. Computers \& Society (CS9) | L | L | L | 1 |
| 72. Operating Systems \& Comp. Architecture II (CS10) | 1 | 1 | L | 2 |
| 73. Principles of Database Design | 3 | 2 | 2 | 7 |
| 74. Artificial Intelligence (CS12) | ) 3 | 1 | 1 | 5 |
| 75. Discrete Structures | 2 | 2 | 1 | 4 |
| 76. Algorithms (CS13) | 2 | 3 | - | 5 |
| 77. Software Design \& Develop.(CS14) | 14) 3 | 3 | 2 | 8 |
| 78. Principles of Prog. Languages | 2 | 3 | 1 | 6 |
| 79. Automata, Computability, \& Formal Languages (CS16) | 2 | 2 | L | 4 |
| 80. Automata Theory | 1 | 1 | - | 2 |
| 81. Numerical Math.: Analysis (CS17) | 17) 1 | 2 | 1 | 4 |
| 82. Numerical Methods | 1 | 1 | L | 2 |
| 83. Numerical Math: Linear Alg. (CS18) | CS18) 1 | 1 | 1 | 2 |
| 84. Compiler Design | 2 | 2 | - | 4 |
| 85. Networks | 1 | 1 | 1 | 3 |
| 86. Modelling \& Simulation | L | 1 | L | 1 |
| 87. Computer Graphics | 2 | 2 | 1 | 6 |
| 88. Semantics \& Verification | L | L | - | L |
| 89. Complexity | L | L | - | L |
| 90. Computational Linguistics | - | - | - | - |
| 91. Senior Seminar/Independ. Stud. CS | . CS 2 | 1 | 1 | 4 |
| 92. Other Computer Science | 7 | 9 | 3 | 18 |
| Total Upper Level | 54 | 61 | 28 | 142 |

## APPENDIX F

## LIST OF RESPONDENTS TO SURVEY

## A: Public Universities

Arizona State University
Bowling Green State University

Indiana State University Indiana University - Bloomington
Iowa State University
Michigan State University
New Mexico State University
North Dakota State University
North Texas State University
Northern Illinois University
Ohio State University
Ohio University-Athens
Oklahoma State University-Stillwater
Penn State University-University Park
SUNY at Buffalo
South Dakota State University
Texas A \& M University
University of Akron
University of Arizona
University of Cincinnati
University of Delaware University of Florida

University of Georgia

University of Idaho University of Kentucky
Univ. of Maryland-College Park
Univ. of Michigan-Ann Arbor
Univ. of Minnesota-Minneapolis

Decis. \& Info. Sci., Mathematics Computer Science
Applied Stat. \& Oper. Res.,
Computer Science, Mathematics \&
Statistics
Mathematics \& Computer Science
Computer Science
Computer Science, Statistics, Mathematics
Mathematics, Computer Science, Statistics \& Probability
Exper. Statistics, Mathematical
Sciences, Computer Science Mathematical Sciences
Computer Science
Mathematical Sciences
Computer \& Info. Sciences, Statistics
Computer Science, Mathematics
Mathematics, Statistics
Statistics, Mathematics, Computer
Science
Mathematics, Statistics
Mathematics, Computer Science
Computer Science, Mathematics, Statistics
Mathematical Sciences
Statistics
Mathematics, Computer Science
Mathematical Sciences
Mathematics, Statistics, Computer and Informational Systems
Mathematics, Mathematics Education, Computer Science, Statistics
Mathematics, Computer Science Mathematics, Statistics
Mathematics, Computer Science Mathematics, Statistics
Computer Science, Mathematics, Statistics

| Univ. of Missouri-Columbia | Computer Science, Statistics Mathematics |
| :---: | :---: |
| Univ. of Nebraska-Lincoln | Mathematics \& Statistics, Computer Science |
| University of Nevada | Mathematics |
| University of New Hamshire | Mathematics, Computer Science |
| University of New Mexico | Computer Science |
| Univ. of North Carolina-Chapel Hill | Mathematics, Biostatistics |
| University of Oregon | Mathematics |
| Univ. of Puerto Rico-Rio Piedras | Mathematics |
| University of South Dakota | Mathematical Sciences |
| University of Texas-Austin | Mathematics |
| Uni versity of Vermont | Mathematics \& Statistics |
| University of Wisconsin-Madison | Statistics, Mathematics |
| Washington State University | Pure \& Applied Mathematics, Computer Science |
| Wichita State University | Mathematics and Statistics, Computer Science |

## B. Private Universities

Boston University
Carnegie-Mellon University
Drake University
Duke University
George Washington University
Georgetown University
Johns Hopkins University

New York University
Northeastern University-Boston
Northwestern University-Evanston
Seton Hall University
Syracuse University
Texas Christian University
University of Miami
University of Santa Clara
Univ. of Southern California
University of Tulsa
Vanderbilt Uni versity
Wake Forest University
Washington Uni versity

Mathematics, Computer Science Statistics, Mathematics
Mathematics \& Computer Science
Computer Science, Mathematics
Statistics \& Comp. Inf. Systems, Mathematics, Operations Research Mathematics, Computer Science Mathematics, Electrical Eng. \& Computer Science, Mathematical Sciences
Computer Science
Mathematics
Ind. Eng. \& Management Sciences, Mathematics
Mathematics
Comp. \& Info. Sciences, Mathematics
Mathematics, Computer Science Mathematics \& Computer Science Mathematics
Mathematics
Mathematics \& Computer Science
Mathematics
Mathematics \& Computer Science Computer Science

## C. Public Four-Year Colleges

Alabama A \& M University
Bluefield State College
Boise State University
CUNY-Brooklyn College
CUNY-City College
CUNY-Hunter College
CUNY-Queens College
Cal Maritime Academy
Cal Polytech State University
Cal State College-Stanislaus
Cal State Polytech University
Cal State University-Chico
Cal State University-Long Beach
Cal State University-Northridge
Cameron University
Central Michigan University
Central State University
Chadron State College
Christopher Newport College
Cleveland State University
College of William \& Mary Delta State University
East Central Oklahoma St. Univ. Eastern Illinois University
Eastern Oregon State College
Florida International University
Francis Marion College
George Mason University
Georgia Institute of Technology
Harris-Stowe State College
Indiana-Purdue Univ.-Ft. Wayne
Indiana-Purdue Univ.-Indianapolis
Jacksonville State University
Lamar University
Longwood College
Mississippi Univ. for Women
Missouri Southern State College
New Mexico Inst. Mining/Tech.
North Carolina A \& T State Univ.
Northern Montana College
Northern State College
Northwestern Oklahoma State Univ.
Pan American University
Penn State Univ.-Capitol Campus
Plymouth State College
Ramapo College of New Jersey
Rutgers University-Newark

Mathematics
Nat. Sciences
Mathematics
Computer \& Info. Science,
Mathematics
Mathematics
Computer Science
Computer Science, Mathematics
Mathematics
Statistics, Computer Science
Mathematics
Mathematics
Mathematics
Mathematics
Mathematics \& Computer Science
Mathematics
Mathematics
Computer Science, Mathematics
Computer Science
Mathematics \& Science
Computer Science, Mathematics
Mathematics, Comp. \& Info Sci.
Computer Science, Mathematics
Mathematics
Computer Science, Mathematics
Mathematics
Mathematics \& Computer Science
Mathematical Sciences
Math. \& Computer Sciences
Mathematical Sciences, Systems
Engineering, Computer Science
Mathematics
Mathematics \& Science
Mathematical Sciences
Mathematical Sciences, Computer \&
Info. Sciences
Mathematics
Mathematics
Mathematical \& Computer Sciences
Science \& Mathematics
Computer Science, Mathematics
Mathematics, Computer Science
Mathematics \& Computer Science
Mathematics
Mathematics
Computer Science
Mathematics \& Computer Science
Mathematical Sciences
Mathematics, Computer Science
Mathematics
Mathematics

SUNY College at Buffalo
SUNY College at Cortland
SUNY College at Fredonia
SUNY College at Geneseo
SUNY College at Oswego
SUNY College at Tech
SUNY Maritime College
SUNY at Stony Brook

Saginaw Valley State College
San Diego State University
San Jose State University
Sangamon State University
South Dakota School Mines \& Tech.
Southeast Missouri State University
Southern Ill. Univ.-Edwardsville
St. Cloud State University
Stephen F. Austin State University
Texas Southern University
Troy State University-Ft. Rucker
Univ. of California-San Diego
Univ. of California-Santa Cruz University of D.C.
University of Illinois at Chicago
University of Minnesota-Duluth
University of Missouri-St. Louis
University of North Florida University of Puerto Rico-Humacao University of South Florida

University of Texas-Arlington University of Wisconsin-Eau Claire University of Wisconsin-Milwaukee University of Wisconsin-Platteville Valley City State College Washburn University of Topeka Western Carolina University Western Michigan University Western Washington University

Mathematics
Mathematics
Mathematics \& Computer Science
Mathematics
Mathematics
Math.-Art \& Sciences
Computer \& Info. Sciences
Mathematics
Computer Science, Applied
Mathematics \& Statistics, Mathematics
Science \& Engineering
Mathematical Sciences
Mathematics \& Computer Science
Mathematics
Mathematical Sciences
Mathematics, Computer Science
Mathematics-Stat.-Comp. Sci.
Mathematics \& Computer Science
Mathematics \& Statistics
Mathematics
Mathematics
Mathematics
Mathematics
Mathematics
Mathematics
Mathematical Sciences
Mathematical Sciences
Mathematical Sciences
Mathematics
Mathematics, Computer Science \&
Engineering
Mathematics
Computer Science, Mathematics
Mathematics
Mathematics, Computer Science
Mathematics
Math. \& Info. Sciences
Mathematics \& Computer Science
Computer Science, Mathematics
Computer Science

## D. Private Four-Year Colleges

Antillian College
Bellevue College
Bentley College
Berea College
Blue Mountain College
Brown University
Bryant College

California Lutheran College
Cardinal Stritch College
Carleton College
Central College
Chatham College
Coe College
College of Idaho
Colorado Technical College
DePauw University
Edgewood College
Fairleigh Dickinson Univ.-Teaneck
Florida Institute of Technology
Florida Memorial College
Gordon College
Hamilton College
Heidelberg College
Hood College
Illinois College
Iona College
Jarvis Christian College
Keuka College
La Salle University
Lakeland College
Manchester College
Marion College
Midland Lutheran College
Millikin University
New Hampshire College
Oberlin College
Oklahoma Christian College
Oral Roberts University
Our Lady of Holy Cross College
Pace University
Rider College
Rochester Institute of Technology
Samford University
Siena College
Southern College
St. John's University
St. Joseph's University
St. Leo College
St. Mary's College
Sterling College
Talladega College
Trinity Christian
University of Bridgeport
University of Dayton
University of San Francisco
University of Steubenville
Virginia Wesleyan College
West Coast Univ.-Orange City Ctr.
Westbrook College
York College of Pennsylvania

Mathematics-Physics-Comp. Sci. Mathematics \& Computer Science Mathematics
Mathematics \& Computer Science Mathematics, Info. Science
Mathematics \& Computer Science
Mathematics
Mathematics
Mathematics \& Computer Science
Mathematics \& Computer Science
Mathematics \& Computer Science
Mathematics \& Computer Science
Science \& Mathematics
Mathematics \& Computer Science
Mathematics \& Computer Science
Mathematics
Mathematics
Computer Science
Mathematics, Comp. Info. Science
Mathematics
Mathematics
Mathematical Sciences
Mathematics \& Computer Science
Mathematical Sciences
Mathematics, Computer Science
Mathematics
Mathematics \& Computer Science
Mathematics
Mathematics
Mathematics
Mathematics \& Science
Natural Sciences
Mathematics
Mathematics \& Physics
Mathematics
Math-Engr-Computer Science
Mathematics
Mathematics
Computer Science
Mathematics \& Computer Science
Science \& Mathematics
Computer Science
Applied Mathematics
Mathematics
Mathematics
Mathematics
Computer Science
Mathematics
Mathematics-Computer Science
Mathematics \& Computer Science
Computer Science, Arts \& Sciences
Mathematics
Mathematics-Physical Sci.

## E. Two-Year Colleges

Alexander City State Jr. College
Alpena Community College
Amarillo College
American River College
Austin Community College
Bakersfield College
Bergen Community College
Brevard Community College
Broward Community College
Burlington County College
Butte Community College
CUNY-New York City Tech. College
Central Texas College
Cerritos College
Chabot College
Cloud County Community College
Coastline Community College
College of the Albemarle
Community College of Beaver County
Contra Costa College
Cuyahoga Community College
Cypress College
Davenport College of Business
DeKalb Community College
El Camino College
El Paso Community College
Erie Community College
Everett Community College
Fresno City College
Gainesville Jr. College
Galveston College
Harrisburg Area Community College
Haywood Technical College
Henry Ford Community College
Imperial Valley College
Inter American Univ.-Aquadilla, PR
Jacksonville College
Johnston Technical College
Joliet Junior College
Kellogg Community College
Kirtland Community College
Lackawanna Jr. College
Lake City Community College
Lake Region Community College
Lake-Sumter Community College
Lakeland Community College
Lane Community College
Lansing Community College
Laredo Jr. College
Lincoln College

Mathematics
Mathematics \& Engineering
Mathematics \& Engineering Mathematics \& Phys. Science Mathematics
Natural Sci. \& Mathematics
Mathematics
Math. -Cen. Campus
Sci.-Math.-Technology
Mathematics
Mathematics
Mathematics
Mathematics
Science \& Mathematics

Mathematics
Science Engr. \& Mathematics
Math. Eng. \& Computer Science
Science \& Mathematics
Mathematics and Science Div.
Mathematics
Mathematics
Mathematics \& Science
Mathematics
Mathematics \& Natural Science
Math. Eng. \& Technology
Mathematics
Math. Eng. \& Science
Mathematics
Mathematics

Science \& Mathematics
Mathematics
Mathematics
Mathematics
Math-Sci-All'd Health
Mathematics
Mathematics
Mathematics
Mathematics
Mathematics

Long Beach City College
Los Angeles City College
Los Angeles Pierce College
Los Angeles Southwest College
Los Angeles Trade Tech. College
Los Angeles Valley College
Louisiana State Univ.-Alexandria
Macomb Community College
Merced College
Montgomery College-Takoma Pk.
Moorpark College
Morristown College
Mt. San Antonio College
Muskegon Community College
North Harris City College
Northeast Alabama St. Jr. College
Ocean County College
Odessa College
Ohio State Univ.- Agri. Tech. Inst.
Olympic College
Orange Coast College
Oxnard College
Pima Community College
Portland Community College
Prince George's City Community College
Rancho Santiago College
Rapphannock Community College
Richard Bland College
Ricks College
Rock Valley College
Rockingham Community College
San Antonio College
San Diego City College
San Jacinto College
Santa Monica College
Santa Rosa Jr. College
Scottsdale Community College
Southwestern Michigan College
Spartanburg Tech. College
Surry Community College
Tallahassee Comm. College
Tarrant County Jr. College
Temple Jr. College
Texas State Tech. Inst.-Amarillo
Tidewater Community College
Tri-Cities State Tech. Inst.
Tulsa Jr. College
Vernon Regional Jr. College
Villa Julie College
Vista College
Wayne Community College
Wayne County Community College

Mathematics \& Engineering
Mathematics
Mathematics
Mathematics
Mathematics \& Science
Mathematics
Mathematics
Mathematics \& Science
Mathematics
Mathematics
Mathematics
Mathematics \& Astronomy
Mathematics \& Science
Mathematics
Mathematics
Mathematics
Mathematics
Mathematics
Mathematics \& Phys. Scienc Mathematics \& Science

Mathematics
Mathematics \& Engineering
Mathematics
Mathematics \& Statistics
Mathematics
Mathematics \& Humanities
Mathematics \& Science
Mathematics
Mathematics \& Engineering
Mathematics
Mathematics
Mathematics \& Science
Mathematical Sciences
Mathematics \& Science
Mathematics \& Science
Mathematics
Mathematics
Mathematics
Mathematics
Mathematics
Mathematics \& Science
Mathematics \& Science Mathematics

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Wenatchee Valley College
West Los Angeles College
Western Piedmont Community College
Wilkes Community College
William R. Harper College
York Technical College
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Mathematics
Mathematics \& Science

Tech-Mathematics-Phys. Science Mathematics

This survey is an essential reference for any one concerned with trends in enrollments or staffing in the mathematical sciences. Every five years, since 1965, the Conference Board of the Mathematical Sciences (CBMS) has sponsored these national surveys. This report is based on that entire record, and it presents a coherent view of the mathematical teaching resources of post secondary schools and of the numbers of students enrolled in various courses across the mathematical sciences curriculum.

This is the book for you if you are interested in any of the following: the supply of mathematically trained students, the growth of computer science, the various roles of two-year and four-year institutions and universities, or the staffing of mathematical sciences departments. The fine details of the survey give information about specific courses and types of institutions. The overall trends are also noteworthy. In mathematics itself undergraduate enrollments are up by $34 \%$ since 1970 ,while staffing is up by less than $6 \%$ over the same period. Such broad general movements are charted here, and they form the background necessary to understand the present and plan for the future.

Survey Sponsor

## The Conference Board of the Mathematical Sciences

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[^6]
[^0]:    * and ** See footnotes on next page.

[^1]:    * Total from original data

[^2]:    * These two numbers are estimates and are probably slightly too low and too high respectively.

[^3]:    (1)

    The percentages shown are of all sections taught by the departments indicated. They include a small number of sections in mathematics or in the other of the two fields.

[^4]:    *Arthur M. Cohen and Florence B. Brawer, The American Community College, Jossey Bass, San Francisco, 1982.

[^5]:    * L denotes some but less than 500 and NA denotes not available.

[^6]:    Member Organizations
    American Mathematical Association of Two-Year Colleges
    American Mathematical Society
    American Statistical Association
    Association for Symbolic Logic
    Association for Women in Mathematics
    Association of State Supervisors of Mathematics
    Institute of Mathematical Statistics
    Mathematical Association of America
    National Council of State Supervisors of Mathematics
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