Y M He\* (he@ou.edu), 601 Elm Ave, Norman, OK 73019. Non-realizability of some big mapping class groups.

For any surface S, there is a natural projection map  $p: Homeo^+(S) \to MCG(S)$  from the group of orientation-preserving homeomorphisms of S to the mapping class group of S. The Nielsen realization problem studies if there is a map  $s: MCG(S) \to Homeo^+(S)$  such that the composition  $s \circ p$  is the identity map on MCG(S).

In this talk, we will discuss the Nielsen realization problem for some big mapping class groups. In particular, we show that the mapping class group of the plane minus a Cantor set or the sphere minus a Cantor set has no realization as a subgroup of the homeomorphism group. (Received January 19, 2022)