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Chantal David* (chantal.david@concordia.ca), **Antoine Comeau-Lapointe**, **Matilde Lalin** and **Wanlin Li**. *On the vanishing of twisted L -functions of elliptic curves over function fields.*

Let E be an elliptic curve over Q , and χ be a Dirichlet character of order ℓ . Heuristics based on the distribution of modular symbols and random matrix theory have led to strong (and somewhat surprising) conjectures on the vanishing of the twisted L -functions $L(E, \chi, s)$ at $s = 1$ (David-Fearnley-Kisilevsky and Mazur-Rubin). In particular, it is conjectured that there are only finitely many characters of order $\ell > 5$ such that $L(E, \chi, 1) = 0$. We investigate in this talk the case of elliptic curves over function fields. For Dirichlet L -functions over function fields, Li and Donepudi-Li have shown how to produce infinitely many characters of order ℓ such that $L(\chi, 1/2) = 0$. We show that their work can be generalized to isotrivial curves $E/F_q(t)$, and we show that if there is one Dirichlet character χ of order ℓ such that $L(E, \chi, 1) = 0$, then there are infinitely many, leading to some specific examples contradicting (the function field analogue of) the number field conjectures. Such a dichotomy does not seem to exist for general (non-isotrivial) curves over $F_q(t)$, and we produce empirical evidence which suggests that the conjectures over number fields also hold over function fields for non-isotrivial $E/F_q(t)$. (Received January 25, 2022)