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University Place, Burlington, VT 05405. *Efficient solution of Hartree–Fock equations in a periodic
external potential.*

Approximate yet fully quantum description of N impenetrable bosons in an external potential $V_{ext}(r)$ (e.g., helium atoms over a crystalline surface) leads to Hartree–Fock equations:

$$\left(-\nabla^2 + V_{ext}(r)\right)u_i(r) + \sum_{i \neq j} \langle u_j(r') | V_{bb}(r - r') | u_j(r') \rangle u_i(r) + \sum_{i \neq j} \langle u_j(r') | V_{bb}(r - r') | u_i(r') \rangle u_j(r) = \sum_j \mu_{ij} u_j(r), \quad (1)$$

where: u_i represents a one-particle wave function of boson i ; ∇^2 is the Laplacian; $V_{bb}(r - r')$ is the interaction potential between bosons at locations r and r' ; and μ_{ij} are Lagrange multipliers that make the solutions of (1) satisfy the orthonormality condition:

$$\langle u_i(r) | u_j(r) \rangle = \delta_{ij}. \quad (2)$$

Above, $\langle \dots | \dots \rangle$ denotes the standard inner product.

For an arbitrary V_{ext} , the cost of solving (1) increases as N^2 , due to the second group of V_{bb} -terms and the μ_{ij} -terms. However, when V_{ext} is periodic, as typical in a crystal, one expects to be able to reduce this to one equation with $O(N)$ terms. In this talk we show how this can be implemented efficiently and the resulting equation can be solved iteratively. (Received August 30, 2021)