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**Ricardo Burity, Aron Simis and Stefan O Tohaneanu\*** (tohaneanu@uidaho.edu). *On the Jacobian ideal of an almost generic hyperplane arrangement.*

Let  $\mathcal{A}$  denote a rank  $n$  central hyperplane arrangement in  $\mathbb{K}^n$ , where  $\text{char}(\mathbb{K}) = 0$ . Suppose  $\ell_1, \dots, \ell_m \in R := \mathbb{K}[x_1, \dots, x_n]$ ,  $m \geq n$  are the defining linear forms, and let  $f = \ell_1 \cdots \ell_m$  denote the defining polynomial of  $\mathcal{A}$ .

We investigate the relationship between two ideals associated to  $\mathcal{A}$ : the Jacobian ideal  $J_f$  (which is the ideal generated by the first partial derivatives of  $f$ ), and the ideal  $\mathbb{I}$  generated by all  $(m - 1)$ -fold products of the distinct defining linear forms (i.e., these generators are  $f/\ell_1, \dots, f/\ell_m$ ).

In the main result we prove that if  $\mathcal{A}$  is almost generic (i.e., any  $n - 1$  of the  $m$  defining linear forms are linearly independent), then  $J_f$  is a minimal reduction of  $\mathbb{I}$ . If  $n = 3$ , then any hyperplane arrangement is almost generic since any two distinct defining linear forms are linearly independent; this determine us to conjecture that the result is true regardless of the almost generic condition.

When  $\mathcal{A}$  is generic, we show that  $(J_f)^{\text{sat}} = \mathbb{I}$ . This provides a simpler proof of a conjecture due to Yuzvinsky (and proven first by Rose and Terao) that  $\text{depth}(\mathbb{R}/J_f) = 0$ . (Received August 16, 2021)