

1161-30-65

**Dima Khavinson\*** (dkhavins@usf.edu). *Some Questions on  $L^1$ -approximation in Bergman Spaces.*

Suppose a continuous on the closed unit disk function  $\omega, \|\omega\|_{L^\infty} = 1$ , can be approximated by analytic functions in  $L^1(dA)$ -norm within  $\epsilon$ , here  $dA$  stands for the area measure.

**Question.** Can we approximate it (in  $L^1(dA)$ ) within  $C\epsilon$  by analytic functions with the  $L^\infty$  norm at most 1? (The constant  $C$  is , of course, independent of  $\omega$ .) The answer is NO, Moreover. the asymptotics, when  $\epsilon$ , tends to 0 can be arbitrarily bad (DK, 2020). **History.** The problem is the  $\epsilon$  - version of the celebrated Hoffman-Wermer Theorem for Uniform Algebras and was posed by J. Wermer in 1980. The answer of the analogous question in  $L^1(d\theta)$ , where  $d\theta$  is the Lebesgue measure on the unit circle, or, in most generality, in the hyperdirichlet algebras content, is also NO (DK-H.Shapiro-F. Perez-Gonzalez, 1998, DK-2019), and "Yes", if we replace  $O(\epsilon)$  by  $O(\epsilon) \log \frac{1}{\epsilon}$  for the disk , and  $O(\epsilon)^{1/2} \log \frac{1}{\epsilon}$  for the hypodirichlet case (DK, 2020). (Received August 08, 2020)