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**Linyuan Lu\*** (lu@math.sc.edu), Department of Mathematics, University of South Carolina, 1523 Greene Street, Columbia, SC 29208, and **Zhiyu Wang**, School of Mathematics, Georgia Institute of Technology, Atlanta, GA 30332. *On the size of planar graphs with positive Lin-Lu-Yau Ricci curvature.*

Let  $G$  be a planar graph embedded into a sphere. The combinatorial curvature  $\phi(v)$  at a vertex  $v$  is defined by  $\phi(v) = 1 - \frac{\deg(v)}{2} + \sum_{\sigma \in F(v)} \frac{1}{|\sigma|}$ , where  $F(v)$  is the set of faces touching  $v$  and  $|\sigma|$  is the number of edges bounding a face  $\sigma$ .  $G$  is said to be positively curved if  $\phi(v) > 0$  for every  $v \in V(G)$ . Higuchi [*J. Graph Theory, 2001*] conjectured that if  $G$  is a simple connected positively curved graph embedded into a 2-sphere and with minimum degree at least 3, then  $G$  is finite. DeVos and Mohar [*Trans. Amer. Math. Soc., 2007*] showed that if  $G$  is not a prism, and an antiprism, then  $|V(G)| \leq 3444$ , resolving Higuchi's conjecture. In this talk, we show an analogue of Higuchi's conjecture in the context of the Lin-Lu-Yau Ricci curvature. In particular, we show that if a planar graph  $G$  with minimum degree at least 3 has positive Lin-Lu-Yau Ricci curvature on every edge, then  $G$  is finite. (Received August 16, 2020)