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Eva A. Gallardo-Gutierrez*, Department of Mathematics, Rawles Hall, 831 East Third St., Indiana University, Bloomington, IN 47405-7106. *C₀-semigroups of 2-isometries and Dirichlet spaces.*

A bounded linear operator T on a separable, infinite dimensional complex Hilbert space \mathcal{H} is called a *2-isometry* if it satisfies

$$T^{*2}T^2 - 2T^*T + I = 0,$$

where I is the identity operator. In addition, such operators are called *analytic* if no nonzero vector is in the range of every power of T . It turns out that M_z , i.e. the multiplication operator by z , acting on the classical Dirichlet space, is a cyclic analytic 2-isometry. But, moreover, Richter proved that any cyclic analytic 2-isometry is unitarily equivalent to M_z acting on a generalized Dirichlet space $D(\mu)$.

In the context of Richter's theorem, we will establish a similarity between C_0 -semigroups of analytic 2-isometries acting on \mathcal{H} and the multiplication operator semigroup $\{M_{\phi_t}\}_{t \geq 0}$ induced by $\phi_t(s) = \exp(-st)$ for s in the right-half plane \mathbb{C}_+ acting boundedly on weighted Dirichlet spaces on \mathbb{C}_+ . As a consequence, we derive a connection with the right shift semigroup acting on a weighted Lebesgue space on the half line \mathbb{R}_+ and address some applications regarding the study of the invariant subspaces of C_0 -semigroups of analytic 2-isometries.

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