

1138-60-391

**Máté Wierdl\*** (wierdlmate@gmail.com), Department of Mathematical Sciences, The University of Memphis, memphis, TN 38152. *Simultaneous recurrence of stationary random walks*. Preliminary report.

The talk is about a problem raised by M. Boshernitzan: Does a stationary random walk simultaneously revisit the origin infinitely often along two different step sizes?

Let us be precise: Let  $(\Omega, \Sigma, P)$  be a probability space;  $T : \Omega \rightarrow \Omega$  an invertible, ergodic m.p.t.;  $F : \Omega \rightarrow \mathbb{Z}$  measurable. Define the random walk  $F^n$  defined by

$$F^n(\omega) = \begin{cases} \sum_{0 \leq k < n} F(T^k \omega), & \text{for } n > 0; \\ 0, & \text{for } n = 0; \\ \sum_{n \leq k < 0} F(T^k \omega), & \text{for } n < 0. \end{cases}$$

It is well known that if  $\int F = 0$  then almost surely  $F^n = 0$  for infinitely many  $n$ .

Boshernitzan's question is if the random walks  $(F^n)$  and  $(F^{2n})$  almost surely return to the origin *simultaneously*, that is almost surely, are there infinitely many  $n$  so that  $F^n = F^{2n} = 0$ ?

Presently, we cannot answer the question, but we will examine some special cases, and present evidence that the answer to Boshernitzan's question is, in general, no.

We also show that simultaneous *triple* return to the origin is, in general, doesn't happen. The counterexample is provided in case  $(T^n F)$  is an iid sequence. (Received February 13, 2018)