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**Carl C. Cowen\*** (ccowen@iupui.edu), IUPUI Dept of Mathematical Sciences, 402 N Blackford St, Indianapolis, IN 46202-3216. *Continuous Semigroups of Composition Operators on Function Spaces on the Disk*. Preliminary report.

An analytic map  $\phi$  of the unit disk into itself defines a composition operator by  $C_\phi f = f \circ \phi$ . Writing  $\phi_n$  for the  $n$ -fold composition of  $\phi$  gives a discrete semigroup of operators  $C_{\phi_j} C_{\phi_k} = C_{\phi_{j+k}}$ . We consider the possibility of extending this to a continuous semigroup,  $C_{\phi_t}$  for  $t \geq 0$ .

An old theorem says that if  $\phi$  is an analytic map of the disk into itself with attractive fixed point  $a$  in the closed disk and  $\phi'(a) \neq 0$ , for each  $z$  in the disk, there is  $\tau(z) \geq 0$  so that  $\phi_t(z)$  can be defined for  $t > \tau(z)$ , so that

$$\{\phi_n(z) : n \geq 0\} \cup \{\phi_t(z) : t > \tau(z)\}$$

is a semigroup. If  $\phi$  maps the disk into itself,  $\phi(1) = \phi'(1) = 1$ , and the power series for  $\phi$  centered at 0 has only positive coefficients, there is a continuous semigroup  $\phi_t(r)$  for  $0 \leq r \leq 1$ ; that is,  $\tau(r) = 0$  for  $0 \leq r \leq 1$ .

We discuss the question of extension to the disk: “If  $\phi$  is a univalent, analytic map of the disk into itself with  $\phi(1) = \phi'(1) = 1$ , and the power series for  $\phi$  centered at 0 has only positive coefficients, when does there exist a continuous semigroup,  $\{C_{\phi_t} : 0 \leq t < \infty\}$ ?” (Received February 03, 2018)