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**A. Aleman, M. Hartz, John McCarthy and S. Richter\*** (srichter@utk.edu). *Weak products of complete Pick spaces.* Preliminary report.

Let  $\mathcal{H}$  be the Drury-Arveson or Dirichlet space of the unit ball of  $\mathbb{C}^d$ . The weak product  $\mathcal{H} \odot \mathcal{H}$  of  $\mathcal{H}$  is the collection of all functions  $h$  that can be written as  $h = \sum_{n=1}^{\infty} f_n g_n$ , where  $\sum_{n=1}^{\infty} \|f_n\| \|g_n\| < \infty$ . We show that  $\mathcal{H} \odot \mathcal{H}$  is contained in the Smirnov class of  $\mathcal{H}$ , i.e. every function in  $\mathcal{H} \odot \mathcal{H}$  is a quotient of two multipliers of  $\mathcal{H}$ , where the function in the denominator can be chosen to be cyclic in  $\mathcal{H}$ . Furthermore, the maps  $\eta : \mathcal{M} \rightarrow \mathcal{H} \cap \mathcal{M}$  and  $\tau : \mathcal{N} \rightarrow \text{Mult}(\mathcal{H}) \cap \mathcal{N}$  establish 1-1 and onto correspondences between the multiplier invariant subspaces of  $\mathcal{H} \odot \mathcal{H}$  and of  $\mathcal{H}$ , and the weak\*-closed ideals of the multipliers  $\text{Mult}(\mathcal{H})$ .

The results hold for many weighted Besov spaces  $\mathcal{H}$  in the unit ball of  $\mathbb{C}^d$  provided the reproducing kernel has the complete Pick property. (Received February 11, 2018)