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**Adela Vraciu\*** (vraciu@math.sc.edu). *Totally acyclic complexes over tensor products of algebras*. Preliminary report.

A doubly infinite complex of free modules over a Noetherian local ring is called totally acyclic if it is acyclic and its dual is also acyclic. A syzygy in such a complex is called a totally reflexive module. A ring is called G-regular if the only totally reflexive modules are free.

Let  $R, S$  be local Artinian algebras of finite type over a field  $k$  and let  $T = R \otimes_k S$ . We investigate the following questions:

1. If  $\mathcal{F}$  is a totally acyclic complex over  $T$ , does it follow that  $\overline{\mathcal{F}} = \mathcal{F} \otimes_T (k \otimes_k S)$  is a totally acyclic complex over  $S$ ?
2. If  $R$  and  $S$  are G-regular, does it follow that  $T$  is G-regular?

We prove that these questions have an affirmative answer if  $R$  belongs to a special class of G-regular rings which we call strictly G-regular.

An example of a strictly G-regular ring is  $R = k[y_1, \dots, y_n]/(y_1, \dots, y_n)^2$ , and as a consequence of our result we recover Tracy-Rangel's description of all the totally reflexive modules over the ring

$$\frac{k[x, y_1, \dots, y_n]}{(x^2, (y_1, \dots, y_n)^2)} = \frac{k[x]}{(x^2)} \otimes_k \frac{k[y_1, \dots, y_n]}{(y_1, \dots, y_n)^2}$$

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