

1138-05-222

**He Guo\*** (he.guo@gatech.edu), Room 117, Skiles Building, 686 Cherry Street, Atlanta, GA 30332, and **Lutz Warnke**. *Packing nearly optimal Ramsey  $R(3, t)$  graphs.*

In 1995 Kim famously proved the Ramsey bound  $R(3, t) \geq ct^2/\log t$  by constructing an  $n$ -vertex graph that is triangle-free and has independence number at most  $C\sqrt{n\log n}$ . We extend this celebrated result, which is best possible up to the value of the constants, by approximately decomposing the complete graph  $K_n$  into a packing of such nearly optimal Ramsey  $R(3, t)$  graphs.

More precisely, for any  $\epsilon > 0$  we find an edge-disjoint collection  $(G_i)_i$  of  $n$ -vertex graphs  $G_i \subseteq K_n$  such that (a) each  $G_i$  is triangle-free and has independence number at most  $C_\epsilon\sqrt{n\log n}$ , and (b) the union of all the  $G_i$  contains at least  $(1 - \epsilon)\binom{n}{2}$  edges. Our algorithmic proof proceeds by sequentially choosing the graphs  $G_i$  via a semi-random (i.e., Rödl nibble type) variation of the triangle-free process.

As an application, we prove a conjecture in Ramsey theory by Fox, Grinshpun, Liebenau, Person, and Szabó (concerning a Ramsey-type parameter introduced by Burr, Erdős, Lovász in 1976). Namely, denoting by  $s_r(H)$  the smallest minimum degree of  $r$ -Ramsey minimal graphs for  $H$ , we close the existing logarithmic gap for  $H = K_3$  and establish that  $s_r(K_3) = \Theta(r^2 \log r)$ . (Received February 09, 2018)