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Barry Monson* (bmonson@unb.ca) and **Egon Schulte**. *Symmetries of Universal Alternating Semiregular Polytopes*. Preliminary report.

Any abstract regular n -polytope R has a free extension U_R , a regular $(n + 1)$ -polytope whose n -faces are all isomorphic to R [Schulte, 1983]. Think of such R 's as building blocks which we glue together face-to-face in the 'freest possible way'. The automorphism group of U_R is about as complicated as that of its building block R .

Recently we extended this construction by allowing two kinds of compatible building blocks P and Q . Since the facets of these regular n -polytopes are all isomorphic, we can fit copies of P and Q in alternating fashion around $(n - 2)$ -faces. Again doing this in the freest possible way we get the universal alternating semiregular $(n + 1)$ -polytope $U_{P,Q}$. We know a lot about its structure: for example, $U_{P,Q}$ covers any $(n + 1)$ -polytope (of arbitrary symmetry) whose facets alternate between any selection of quotients of P and Q . But when $P \not\cong Q$ and we want to understand the regular covers of $U_{P,Q}$ itself, we run into confounding and unexpected difficulties. I will complain about this as time permits. (Received December 30, 2017)