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We consider solutions  $v > 0$  to certain nonlinear PDE of  $p$  Laplace type ( $1 < p < \infty$ ) in the cone,  $K(\alpha) = \{x = (x_1, \dots, x_n) : x_1 > \alpha|x|\} \subset \mathcal{R}^n$  with continuous boundary value zero on  $\partial K(\alpha)$  when  $\alpha \in [-1, 1)$ . It turns out that  $v$  is of the form,

$$v(x) = v(r, \theta) = r^\lambda f(\theta), \lambda > 0,$$

provided either  $\alpha \neq -1$  or  $\alpha = -1$  and  $p > n - 1$ . Here  $r, \theta$  are spherical coordinates :  $x_1 = r \cos \theta, r = |x|, 0 \leq \theta \leq \pi$ . During the first part of our talk we discuss what is known about the relationship between  $\alpha$  and  $\lambda$  for a fixed  $p > 1$  and our attempts to solve a related eigenvalue problem for a nonlinear first order differential equation when  $\alpha = -1$  and  $p > n - 1$ . During the second part of the talk we sketch a finesse type argument which shows for  $\alpha = -1$  and  $p > n - 1$  that  $\lambda = 1 - (n - 1)/p$ . Time permitting we discuss applications of this result. (Received February 05, 2018)