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We show that every polynomial in $\mathbb{Z}[x]$ defines an endomorphism of the d -ary rooted tree induced by its action on the ring \mathbb{Z}_d of d -adic integers. The sections of this endomorphism also turn out to be induced by polynomials in $\mathbb{Z}[x]$ of the same degree. In the case of permutational polynomials acting on \mathbb{Z}_d by bijections the induced endomorphisms are automorphisms of the tree. In the case of \mathbb{Z}_2 such polynomials were completely characterized by Rivest. As our main application we utilize the result of Rivest to derive the condition on the coefficients of a permutational polynomial $f(x) \in \mathbb{Z}[x]$ that is necessary and sufficient for f to induce a level transitive automorphism of the binary tree, which is equivalent to the ergodicity of the action of $f(x)$ on \mathbb{Z}_2 with respect to the normalized Haar measure. (Received February 16, 2018)