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Throughout R is a commutative Noetherian local ring and R -modules are assumed to be finitely generated.

Recall a reflexive R -module M is called totally reflexive if $\text{Ext}_R^i(M, R) = 0 = \text{Ext}_R^i(M^*, R)$ for all $i \geq 1$, where $M^* = \text{Hom}_R(M, R)$. The totally reflexive modules are precisely the nonzero modules of Gorenstein dimension zero. In 2006 Jorgensen and Şega proved the conditions defining total reflexivity are independent: they constructed a ring R , and a reflexive R -module M such that $\text{Ext}_R^i(M, R) = 0 \neq \text{Ext}_R^i(M^*, R)$ for all $i \geq 1$.

I will report on an ongoing joint work with Tokuji Araya. In view of the aforementioned result, we consider the problem of determining new conditions, under which the vanishing of $\text{Ext}_R^i(M, R)$ forces M to be totally reflexive. Motivated by the definition of reducible complexity, a notion studied by Bergh, we introduce the reducing versions of standard homological dimensions.

In this talk we will raise some questions and discuss one of our results in this direction: if a module M has finite reducing Gorenstein dimension and $\text{Ext}_R^i(M, R) = 0$ for all $i \geq 1$, then M is totally reflexive. (Received February 19, 2018)