

1139-05-635

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Star-triangle diagrams are a useful but poorly understood tool in the theory of association schemes. Similar ideas have been used to rule out distance-regular graphs using different language. Meanwhile the same object is encoded in the partition function of link diagrams in the development of spin models.

Let  $X$  be a nonempty finite set and let  $\mathbb{A}$  be a vector subspace of  $\text{Mat}_X(\mathbb{C})$ . Consider a digraph  $G = (V(G), E(G))$  with edge weight function  $w : E(G) \rightarrow \mathbb{A}$  and a set  $R \subseteq V(G)$  of distinguished nodes. For  $|R| = m$ , the *scaffold*  $\mathcal{S}(G; w, R)$  is then defined as the  $m^{\text{th}}$  order tensor

$$\mathcal{S}(G; R, w) = \sum_{\varphi: V(G) \rightarrow X} \left( \prod_{\substack{e \in E(G) \\ e=(a,b)}} w(e)_{\varphi(a), \varphi(b)} \right) \bigotimes_{r \in R} \widehat{\varphi(r)}$$

where  $\hat{x}$  is the standard basis vector in  $\mathbb{C}^X$  indexed by  $x \in X$ .

The aim of this talk is to outline a basic theory of scaffolds in the case where  $\mathbb{A}$  is the Bose-Mesner algebra of some association scheme. Topics to be discussed include spin models for link invariants, triple intersection numbers for distance-regular graphs and structure theorems for  $Q$ -polynomial association schemes. (Received February 20, 2018)