Kasso A. Okoudjou and Shujie Kang*, 4176 Campus Drive - William E. Kirwan Hall, College Park, MD 20742. Grassmannian Frames and Minimizers of the p-Frame Potentials. Preliminary report.
The $p$-frame potential of a frame $\left\{v_{i}\right\}_{i=1}^{N} \subset \mathbb{R}^{d}$ is defined as $F P_{p, N, d}=\left(\sum_{i<j}\left|\left\langle v_{i}, v_{j}\right\rangle\right|^{p}\right)^{1 / p}$. Grassmannian frames are minimizers of the frame potential when $p=\infty$. More generally, one can ask if Grassmannian frames also minimize the $p$ frame potentials for $2 \leq p<\infty$. We report on recent progress made in solving this question in $\mathbb{R}^{2}$. There have been results showing this is true when $p$ is even, and we conjecture that the statement also holds when p is odd. We shall motivate our approach by focusing on the case $p=3$ and $N=5$. Our preliminary results rely on certain techniques developed by Cohn and Kumar involving absolute continuous function and ultraspherical polynomials. (Received February 05, 2018)

