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**Tin-Yau Tam\*** ([tamtiny@auburn.edu](mailto:tamtiny@auburn.edu)), Department of Mathematics and Statistics, 221 Parker Hall, Auburn University, Auburn, AL 36830. *Hyperbolic geometry of positive definite matrices associated with geometric mean.*

In this talk we will discuss the geometry and inequalities associated with the geometric mean of positive definite matrices. The space  $P_n$  of  $n \times n$  positive definite matrices of determinant 1 is a Riemannian manifold. It turns out that the geometry associated with the Riemannian structure is hyperbolic. We show that geodesic convexity emerges when a natural pre-order called log majorization is introduced to  $P_n$ . We also derive several inequalities for the geometric mean. Some inequalities reflect the hyperbolic geometry. (Received January 12, 2016)