1117-42-362 Leonid Slavin* (leonid.slavin@uc.edu) and Pavel Zatitskiy. Dimension-free estimates for harmonic BMO. Preliminary report.

We consider $BMO(\mathbb{R}^n)$ equipped with the Garsia norm,

$$\|\varphi\|_G = \sup_{z \in \mathbb{R}^{n+1}_+} \left(\varphi^2(z) - \varphi(z)^2\right)^{1/2},$$

where g(z) denotes the harmonic extension of a function g on \mathbb{R}^n into the upper half-space. We show how one can obtain estimates for expressions of the form

 $f(\varphi)(z)$

in terms of $\varphi(z)$, $\varphi^2(z)$ and $\|\varphi\|_G$. Here f is a fixed function on \mathbb{R} , a priori assumed locally bounded and uniformly bounded from below. For example, $f(t) = e^t$ gives the harmonic analog of the integral John–Nirenberg inequality.

It turns out that if f is such that the corresponding inequality holds for BMO((0,1)) equipped with the classical $(L^2$ -based) BMO norm, then we automatically have the same bound for the functional above; in particular, all such bounds are dimension-free. The proof uses Bellman functions for the classical formulation as locally concave majorants for those in the harmonic formulation. Analogous results hold for related function classes, such as A_p . (Received January 18, 2016)