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Mikel Viana* (mviana3@gatech.edu) and **Rafael de la Llave**. *Almost-Reducibility for fibered holomorphic dynamics.*

We consider fibered holomorphic dynamics generated by the skew product

$$\begin{aligned} F : \mathbb{C}^n \times \mathbb{T}^d &\longrightarrow \mathbb{C}^n \times \mathbb{T}^d \\ F(z, \theta) &= (f(z, \theta), \theta + \omega) \end{aligned}$$

which has as base the irrational translation T_ω on the torus \mathbb{T}^d .

F has no fixed point nor a periodic orbit: The invariant object that organizes the dynamics is an invariant torus $K : \mathbb{T}^d \rightarrow \mathbb{C}^n$. A Nash-Moser iteration has been developed to efficiently construct such tori, given an approximately invariant torus K_0 . It is necessary to add parameters to the system if we want to preserve the frequency.

The asymptotic properties of the derivative cocycle

$$A_{K_0}(\theta) := Df(K_0(\theta), \theta),$$

play a crucial role. We allow central directions E^c for the action of A_{K_0} , and use the notion of approximate reducibility to perform a KAM step. Here some Diophantine conditions (called Melnikov conditions) appear, but it turns out that these conditions are not strictly necessary for the construction of K : We will see that one can still construct non-reducible invariant tori K near K_0 . (Received January 17, 2016)