1117-11-387 Nathan Jones* (ncjones@uic.edu), University of Illinois at Chicago, MSCS Dept., 322 Science and Engineering Offices (M/C 249), 851 S. Morgan Street, Chicago, IL 60607, and Ken McMurdy (kmcmurdy@ramapo.edu). Elliptic curves with non-abelian entanglements.
Let $K$ be a number field. An elliptic curve $E / K$ is said to have a non-abelian entanglement if there are relatively prime positive integers, $m_{1}$ and $m_{2}$, such that $K\left(E\left[m_{1}\right]\right) \cap K\left(E\left[m_{2}\right]\right)$ is a non-abelian Galois extension of K . In this talk, we will discuss our ongoing efforts to classify, using explicit methods, all infinite families of elliptic curves $E / K$, for a fixed $K$, with non-abelian entanglements. This problem is closely related to that of determining when the image of $\rho_{E}$ in $G L_{2}(\hat{\mathbb{Z}})$ is maximal, and to the study of correction factors for various conjectural constants for elliptic curves over $\mathbb{Q}$. (Received January 18, 2016)

