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**Casablanca.** *Wiener index and average eccentricity of the strong product of graphs.*

The Wiener index  $W(G)$  of a connected graph  $G$  is the sum of the distances between all unordered pairs of vertices. The average eccentricity of  $G$  is the arithmetic mean of the eccentricities of the vertices of  $G$ , where the eccentricity of a vertex  $v$  is the maximum of the distances from  $v$  to all other vertices of  $G$ .

A well-known result states that among all connected graphs of given order the path is the unique graph that maximises the Wiener index. Casablanca, Favaron and Kouider generalised this result: Consider for an arbitrary but fixed connected graph  $H$  the Wiener index of the strong product  $W(G \boxtimes H)$ , where  $G$  is chosen from a collection of graphs. If  $G$  is chosen from all connected graphs of order  $n$ , then  $W(G \boxtimes H)$  is maximised if  $G$  is a path.

We generalise this result by showing that if  $G$  is chosen from all connected graphs of given order and size, then  $W(G \boxtimes H)$  is maximised if  $G$  is a so-called path-complete graph. We further show that if  $G$  is chosen from all  $2r$ -connected graphs of given order, where  $r \in \mathbb{N}$ , then  $W(G \boxtimes H)$  is maximised if  $G$  is the  $r$ th power of a cycle.

We give similar results on the average eccentricity of strong products. (Received January 17, 2016)