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An odd hole is an induced odd cycle of length at least 5. Scott and Seymour confirmed a conjecture of Gyárfás and proved that if a graph G has no odd holes then $\chi(G) \leq 2^{2^{\omega(G)+2}}$. Chudnovsky, Robertson, Seymour and Thomas showed that if G has neither K_4 nor odd holes then $\chi(G) \leq 4$. In this note, we show that if a graph G has neither triangles nor quadrilaterals, and has no odd holes of length at least 7, then $\chi(G) \leq 4$ and $\chi(G) \leq 3$ if G has radius at most 3. We also show that, for each vertex u of G , the set of vertices of the same distance to u induces a bipartite subgraph. This answers some questions by Plummer and Zha. (Received January 15, 2016)