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**Thomas M. Fiore\*** (tmfiore@umich.edu). *Approximation in  $K$ -theory for Waldhausen Quasicategories.*

Waldhausen's Approximation Theorem from 1985 gives a sufficient criteria for an exact functor to induce a level-wise equivalence of Waldhausen  $K$ -theory spectra. This talk is about an analogous version in the setting of quasicategories: if an exact functor  $F$  satisfies Waldhausen's App 1 and App 2, and the domain admits certain colimits, then  $F$  induces a level-wise equivalence in Waldhausen  $K$ -theory. As a corollary, if  $F$  is an exact functor of Waldhausen quasicategories and induces an equivalence of homotopy categories, and all morphisms of the domain are cofibrations, then  $F$  induces a level-wise equivalence in Waldhausen  $K$ -theory. The main technical result to prove this is a Pre-Approximation Theorem that does not require Waldhausen structures. Namely, if  $F$  is a functor between quasicategories that reflects equivalences, every morphism  $Fa \rightarrow b$  factors as  $(equiv) \circ Ff$ , the functor of homotopy categories  $hoF$  is essentially surjective and full on isos, and the domain of  $F$  admits certain colimits preserved by  $F$ , then  $F$  induces an equivalence of maximal Kan subcomplexes. (Received January 04, 2017)