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Mrinal K Roychowdhury* (mrinal.roychowdhury@utrgv.edu), School of Mathematical and Statistical Science, University of Texas Rio Grande Valley, 1201 West University Drive, Edinburg, TX 78539. *Optimal Quantization.*

Let \mathbb{R}^d denote the d -dimensional Euclidean space, $\|\cdot\|$ denote the Euclidean norm on \mathbb{R}^d for any $d \geq 1$, and $n \in \mathbb{N}$. Then, the n th *quantization error* for a Borel probability measure P on \mathbb{R}^d is defined by

$$V_n := V_n(P) = \inf \left\{ \int \min_{a \in \alpha} \|x - a\|^2 dP(x) : \alpha \subset \mathbb{R}^d, \text{card}(\alpha) \leq n \right\},$$

where the infimum is taken over all subsets α of \mathbb{R}^d with $\text{card}(\alpha) \leq n$. If $\int \|x\|^2 dP(x) < \infty$ then there is some set α for which the infimum is achieved. Such a set α for which the infimum occurs and contains no more than n points is called an *optimal set of n -means*, or *optimal set of n -quantizers*. Recently, we have determined the optimal sets of n -means and n th quantization error for some singular and nonsingular continuous probability measures. I will talk about it. (Received January 26, 2017)