

1127-11-261

**Mojtaba Moniri\*** (m-moniri@wiu.edu). *Approximate closed formulas for (the g-inverse of) binary lengths of a Wolfram sequence.*

For a sequence  $c$  of approximate multiplication by  $\frac{3}{2}$ , namely  $x_{n+1} = \lfloor \frac{3}{2}x_n \rfloor$ , with  $x_1 = 2$ , the binary lengths  $s$  of the terms of  $c$  and the generalized inverse  $r(m) = \min\{k | s(k) \geq m\}$  of  $s$  are considered. We prove that if  $c$  is never a power of 2 beyond the third position, then  $r$  is Sturmian there  $\lfloor \frac{m}{\log_2(\frac{3}{2})} + \gamma \rfloor - 1$  with its inhomogeneity  $\gamma$  expressible via an Odlyzko-Wilf constant. In any case we show that on a set of  $n$ 's with density between 0.9027 to 0.9028,  $r_m = \lfloor \frac{m}{\log_2(\frac{3}{2})} \rfloor - 1$  and on an exception set of density between 0.0972 to 0.0973,  $r_m = \lfloor \frac{m}{\log_2(\frac{3}{2})} \rfloor$ . For the sequence  $s$  itself, we show that on a set of  $n$ 's with density between 0.8869 to 0.8870,  $s_n = \lfloor n \log_2(\frac{3}{2}) \rfloor + 1$  and on an exception set of density between 0.1130 to 0.1131,  $s_n = \lfloor n \log_2(\frac{3}{2}) \rfloor + 2$ . A similar conditional closed formula is obtained for  $s$  in the style of the one for the sequence  $r$ . (Received February 05, 2017)