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Jordan Almeter, Samet Demircan, Andrew Kallmeyer, Kevin G Milans*
(milans@math.wvu.edu) and **Robert Winslow**. *Graph 2-rankings*.

A *2-ranking* of a graph G is a proper coloring $f : V(G) \rightarrow [t]$ such that for each path uvw in G , either u and w have distinct colors or $f(v) > f(u) = f(w)$. A 2-ranking is intermediate in strength between a star coloring and a distance-2 coloring. The *2-ranking number of G* , denoted $\chi_2(G)$, is the minimum number of colors needed for a 2-ranking. A classical error-correcting code argument gives an optimal distance-2 coloring of the d -dimensional cube Q_d when d is one less than a power of two. We extend the argument to obtain $\chi'_2(Q_d) = d + 1$ for all d .

The *edge 2-ranking number* of a graph G , denoted $\chi'_2(G)$, is the 2-ranking number of the line graph of G . It is also the least integer t such that the edges of G can be partitioned into matchings M_1, \dots, M_t such that M_k is an induced matching in the subgraph of G with edge set $\bigcup_{j \in [k]} M_j$. What is the edge 2-ranking number of $K_{m,n}$? We obtain an asymptotic result when m is fixed and $n \rightarrow \infty$. For the diagonal case, we show only that $\Omega(n \log n) \leq \chi'_2(K_{n,n}) \leq O(n^{\log_2 3})$. (Received February 07, 2017)