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**Steven Lindell\*** ([slindell@haverford.edu](mailto:slindell@haverford.edu)), 370 Lancaster Ave., Department of computer science, Haverford College, Haverford, PA 19041, and **Scott Weinstein** ([weinstein@cis.upenn.edu](mailto:weinstein@cis.upenn.edu)). *Traversal-invariant elementary definability for logarithmic-space computation*. Preliminary report.

First-order logic is often portrayed as being insufficient to capture complexity classes of importance in theoretical computer science. Typically, inductive definitions such as transitive-closure are added as fixed-point operators, and the resulting logics characterize logarithmic-space computation over finite structures. We remedy this by insisting that all structures are input in some traversal order – one in which individual elements are related to previous elements. For example, a traversal of a connected undirected graph is a linear ordering of its vertices in which every initial segment is connected. First-order formulas invariant of the underlying traversal order are called traversal-invariant. Our results show that the traversal-invariant definitions capture logarithmic-space computability. If moreover the traversal corresponds to a breadth-first order, the breadth-first invariant elementary definitions capture nondeterministic logarithmic-space computability. To prove these results we rely heavily on some of the most important theorems in computational complexity: the existence of universal traversal sequences; as well as the celebrated closure of nondeterministic space under complementation. Time permitting, we will discuss extensions into the transfinite. (Received February 03, 2017)