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Aamena Rasim Al-Qabani* (rn030601@reading.ac.uk), University of Reading/
Whiteknights, PO Box 2, Reading, RG6 6AX, United Kingdom, **Titus Willem Hilberdink**
(t.w.hilberdink@reading.ac.uk), University of Reading/ Whiteknights, PO Box 2, Reading,
RG6 6AX, United Kingdom, and **Jani A. Virtanen** (j.a.virtanen@reading.ac.uk), University
of Reading/ Whiteknights, PO Box 2, Reading, RG6 6AX, United Kingdom. *Fredholm properties
of block Toeplitz operators on vector valued Fock spaces $(F_\alpha^p)_N$.*

Let F^2 be the standard Fock space. The vector valued space $(F_\alpha^p)_N$, is defined by

$$(F_\alpha^p)_N = \{ \mathcal{F} = (f_1, f_2, \dots, f_n) : f_k \in F_\alpha^p \text{ for all } 1 \leq k \leq n \},$$

it is a subspace of L_N^p . Let $\mathcal{A} \in L_{N \times N}^\infty(\mathbb{C})$ is a matrix valued function and let $M_{\mathcal{A}} : L_N^p \rightarrow L_N^p$ is the multiplication operator

The block Toeplitz operator $T_{\mathcal{A}}$ on $(F_\alpha^p)_N$ defined by

$$T_{\mathcal{A}}(f) = \left(\sum_{i=1}^N T(a_{ki}) f_i \right)_{k=1}^N = \left(\sum_{i=1}^N P(a_{ki} f_i) \right)_{k=1}^N,$$

where, P is the orthogonal projection from $L^p(\mathbb{C}, d\lambda_\alpha)$ onto F_α^p , and $f \in (F_\alpha^p)_N$.

We study the boundedness, compactness and the Fredholm properties of $T_{\mathcal{A}}$ on $(F_\alpha^p)_N$ with \mathcal{A} in $(L^\infty(\mathcal{C}) \cap VO)_{N \times N}$ and $(L^\infty(\mathcal{C}) \cap VMO)_{N \times N}$. The main result establishes a criterion for the Fredholmness and the index of $T_{\mathcal{A}}$ on $(F_\alpha^p)_N$. (Received February 11, 2016)