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**David Galvin\*** (dgalvin1@nd.edu). *Long-range influence in colorings of the cube.*

Choose an independent set uniformly in the  $d$ -dimensional hypercube. The probability that a particular vertex, say  $v_1 = (1, \dots, 1)$ , is in the independent set is roughly  $1/4$  (though this is far from obvious). We also know that there is long-range influence: if we condition on  $(0, \dots, 0)$  being in the independent set, then the probability of  $v_1$  being in the set changes dramatically, dropping to nearly 0 if  $d$  is odd and jumping to nearly  $1/2$  if  $d$  is even.

Similar long-range influence results can be established if “independent set” is replaced by “proper  $q$ -colouring”. I’ll discuss these results, and highlight a question relating to mixing time of Glauber dynamics for sampling proper  $q$ -colourings of the cube, which we can resolve for  $q = 3$  but remains open for  $q > 3$ . Partly joint work with John Engbers. (Received February 12, 2016)