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Charles Tomlinson* (ctomlinson2@math.unl.edu) and **Philip DeOrsey**. *Fast percolation on the hexagonal lattice*. Preliminary report.

In r neighbor bootstrap percolation one considers the evolution of a cellular automaton consisting of cells where new cells become infected if at least r of their neighbors are already infected. Classical interest was in the model where cells were selected for inclusion in the initially infected set, seed, independently at random with probability p . The effects of p on expected percolation time and the probability of percolation have been studied extensively.

We approach the model from an extremal perspective, asking how fast a convex region in a hexagonal lattice can be percolated by a minimum size seed 3-neighbor percolation. The fastest time is known for squares in a square lattice with 2 neighbor percolation. In a regular hexagon whose sides contain n sites, the n -hex, we show that the fastest percolation can occur is in $2n + 1$ steps. Unlike the extremal examples for the square grid, the seed does not reside in n -hex. When the seed is entirely contained in the n -hex we show that the fastest percolation time, t satisfies $2n + 1 \leq t \leq \frac{7}{3}(n - 2) + 3$. The upper bound comes via construction which we conjecture, and are working to show, is optimal. (Received February 23, 2016)