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**Andrew Treglown.** *Tiling directed graphs with tournaments.* Preliminary report.

The Hajnal–Szemerédi theorem is a celebrated theorem in extremal graph theory. It states that for any integer  $r \geq 1$  and any multiple  $n$  of  $r$ , if  $G$  is a graph on  $n$  vertices and  $\delta(G) \geq (1 - 1/r)n$ , then  $G$  can be partitioned into  $n/r$  vertex-disjoint copies of the complete graph on  $r$  vertices. We will discuss a very general analogue of this result for directed graphs: for any integer  $r \geq 4$  and any sufficiently large multiple  $n$  of  $r$ , if  $G$  is a directed graph on  $n$  vertices and every vertex is incident to at least  $2(1 - 1/r)n - 1$  directed edges, then  $G$  can be partitioned into  $n/r$  vertex-disjoint subgraphs of size  $r$  each of which contain every tournament on  $r$  vertices. (Received February 22, 2016)