

1120-05-138

**Noga Alon, Alexandr Kostochka, Benjamin Reiniger\*** (reiniger@ryerson.ca), **Douglas West** and **Xuding Zhu**. *Coloring, sparseness, and girth via augmented trees.*

An  $r$ -augmented tree is a rooted tree plus  $r$  edges added from each leaf to ancestors. For  $d, g, r \in \mathbb{N}$ , we construct a bipartite  $r$ -augmented complete  $d$ -ary tree having girth at least  $g$ . The height of such trees must grow extremely rapidly in terms of the girth.

Using the resulting graphs, we construct sparse non- $k$ -choosable bipartite graphs, showing that maximum average degree at most  $2(k - 1)$  is a sharp sufficient condition for  $k$ -choosability in bipartite graphs, even when requiring large girth. We also give a new simple construction of non- $k$ -colorable graphs and hypergraphs with any girth  $g$ . (Received February 19, 2016)