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**Ewain Gwynne** and **Jason Peter Miller\*** (jpmiller@mit.edu), Massachusetts Institute of Technology, Department of Mathematics, E18-470, 77 Massachusetts Avenue, Cambridge, MA 02139, and **Xin Sun**. *Almost sure multi-fractal spectrum of SLE.*

Suppose that  $\eta$  is a Schramm-Loewner evolution ( $\text{SLE}_\kappa$ ) in a smoothly bounded simply connected domain  $D \subset \mathbb{C}$  and that  $\phi$  is a conformal map from  $\mathbb{D}$  to a connected component of  $D \setminus \eta([0, t])$  for some  $t > 0$ . The multifractal spectrum of  $\eta$  is the function  $(-1, 1) \rightarrow [0, \infty)$  which, for each  $s \in (-1, 1)$ , gives the Hausdorff dimension of the set of points  $x \in \partial\mathbb{D}$  such that  $|\phi'((1 - \epsilon)x)| = \epsilon^{-s+o(1)}$  as  $\epsilon \rightarrow 0$ . We rigorously compute the a.s. multifractal spectrum of SLE, confirming a prediction due to Duplantier. As corollaries, we confirm a conjecture made by Beliaev and Smirnov for the a.s. bulk integral means spectrum of SLE and we obtain a new derivation of the a.s. Hausdorff dimension of the SLE curve for  $\kappa \leq 4$ . Our results also hold for the  $\text{SLE}_\kappa(\underline{\rho})$  processes with general vectors of weight  $\underline{\rho}$ . (Received January 19, 2015)