

1108-53-119

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This talk is based on joint work with Bang-Yen Chen, Franki Dillen and Luc Vrancken on curvature inequalities for Lagrangian submanifolds of complex space forms. In particular, if  $M^n$  is an  $n$ -dimensional Lagrangian submanifold of a complex space form  $\tilde{M}^n(c)$  of constant holomorphic sectional curvature  $c$ , then one can prove pointwise inequalities of the following type:

$$\delta(n_1, \dots, n_k) \leq a(n, k, n_1, \dots, n_k) \|H\|^2 + b(n, k, n_1, \dots, n_k) c.$$

Here,  $H$  is the mean curvature vector and  $\delta(n_1, \dots, n_k)$  is any delta-curvature of  $M^n$ . Recall that on an  $n$ -dimensional Riemannian manifold, one can define a delta-curvature for any  $k$ -tuple  $(n_1, \dots, n_k)$  of integers, satisfying  $2 \leq n_1 \leq \dots \leq n_k \leq n - 1$  and  $n_1 + \dots + n_k \leq n$ . The strength of the inequalities lies in the fact that they give information about intrinsic invariants (the delta-curvatures) by knowing an extrinsic invariant (the mean curvature) and vice versa.

In this talk, I will give an overview of the search for the optimal constants  $a$  and  $b$  in the above inequality. Franki Dillen was involved in all major steps, from the first proposal in 1994 until our final solution in 2013. (Received January 06, 2015)