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**Nathan Pennington\*** (nathanpennington@creighton.edu), NE 68102. *Low regularity global solutions to a generalized Leray-alpha equation.*

It has recently become common to study many different approximating equations of the Navier-Stokes equation. One of these is the Leray- $\alpha$  equation, which regularizes the Navier-Stokes equation by replacing (in most locations) the solution  $u$  with  $(1 - \alpha^2 \Delta)u$ . Another is the generalized Navier-Stokes equation, which replaces the Laplacian with a Fourier multiplier with symbol of the form  $-|\xi|^\gamma$  ( $\gamma = 2$  is the standard Navier-Stokes equation), and recently in [?] Tao also considered multipliers of the form  $-|\xi|^\gamma/g(|\xi|)$ , where  $g$  is (essentially) a logarithm. The generalized Leray- $\alpha$  equation combines these two modifications by incorporating the regularizing term and replacing the Laplacians with more general Fourier multipliers, including allowing for  $g$  terms similar to those used in [?]. Here we prove the existence of unique, low regularity solutions to the generalized Leray-alpha equation with non- $L^2$  initial data. (Received January 17, 2015)