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**Marcelo Aguiar** (maguiar@math.cornell.edu) and **Aaron Lauve\*** (lauve@math.luc.edu),  
Department of Mathematics and Statistics, Loyola University Chicago, 1032 W Sheridan Road,  
Chicago, IL 60660. *The characteristic polynomial of the antipode for combinatorial Hopf algebras.*

The Adams operators  $\Psi_n$  on a Hopf algebra  $H$  are the convolution powers of the identity of  $H$ . The antipode of  $H$  is the special case  $n = -1$ . We study the Adams operators when  $H$  is graded connected. The main result is a complete description of the characteristic polynomial—both eigenvalues and their multiplicities—for the action of the operator  $\Psi_n$  on each homogeneous component of  $H$ . The eigenvalues are powers of  $n$ . The multiplicities are independent of  $n$ , and in fact only depend on the dimension sequence of  $H$ . We look at some combinatorial consequences of this result, and, time permitting, indicate extensions to Hopf monoids in species,  $q$ -Hopf algebras, and cofree graded connected Hopf algebras. (Received January 19, 2015)