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**Caleb McKinley Shor\*** ([cshor@wne.edu](mailto:cshor@wne.edu)), Department of Mathematics, Western New England University, 1215 Wilbraham Rd, Springfield, MA 01119. *Ordinary and higher-order Weierstrass points on superelliptic curves.*

Given an algebraic curve  $C$  of genus  $g$  defined over  $\mathbb{C}$ , we say a point  $P$  is a Weierstrass point if  $\dim(\mathcal{L}(gP)) > 1$ , where  $\mathcal{L}(D)$  is the Riemann-Roch space associated to a divisor  $D$ . One can generalize this to define a higher-order Weierstrass point (which we call a  $q$ -Weierstrass point, for  $q \geq 1$ ), and one can also talk about the weight of a Weierstrass point. For any curve of genus  $g > 1$  and any  $q \geq 1$ , there are a finite number of  $q$ -Weierstrass points with bounded weights.

The subject of Weierstrass points is an interesting one with immediate applications. In particular, the set of Weierstrass points is an invariant of a curve which is useful in studying the automorphism group of a curve.

In this talk, we will consider Weierstrass points on superelliptic curves, which are curves of the form  $y^n = f(x)$  for  $f(x)$  a separable polynomial of degree  $d$ . Under a mild hypothesis, it is well known that the branch points of such curves are Weierstrass points. We will investigate the weights of these branch points for given values of  $n$  and  $d$  and use them to obtain some asymptotic results. We will also discuss arithmetic properties of these points. (Received January 20, 2015)