

1126-13-250

**Warren Wm. McGovern\*** (warren.mcGovern@fau.edu), Jupiter, FL 33458. *Applications of Ultrafilters to Commutative Rings with Identity*. Preliminary report.

Let  $R$  be a commutative ring with identity. Furthermore, we impose the condition that  $R$  is Jacobson semi-simple, that is, the intersection of the maximal ideals of  $R$  is 0. Denote the set of maximal ideals of  $R$  by  $\text{Max}(R)$ . Given an ideal  $I \subseteq R$ , define

$$V(I) = \{M \in \text{Max}(R) : I \subseteq M\}.$$

The collection  $Z = \{V(I) : I \text{ is a f.g. ideal}\}$  is closed under finite unions and finite intersections. Thus, it is a bounded distributive lattice of sets. Moreover,  $Z$  is a Wallman lattice. Therefore, the collection of  $Z$ -ultrafilters,  $\text{Ult}(Z)$ , is a compact  $T_1$ -space when equipped with the Wallman topology. There is a one-to-one correspondence between the collection of  $z$ -ideals of  $R$  and the collection of  $Z$ -filters. In particular,  $\text{Max}(R)$  and  $\text{Ult}(Z)$  are homeomorphic.

Our goal is to generalize this to the lattice  $Z^\# = \{cl \ int V(I) : I \text{ is f.g. ideal}\}$ . The goal is to describe  $\text{Ult}(Z^\#)$  as well as the corresponding maximal  $Z^\#$ -ideals. (Received January 15, 2017)