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**Louiza Fouli** and **Bruce Olberding\*** (olberdin@nmsu.edu), Department of Mathematical Sciences, New Mexico State University, Las Cruces, NM 88003-8001. *Reductions in Noetherian local rings with finite residue field*. Preliminary report.

A reduction of an ideal  $I$  of a commutative ring  $R$  is a subideal  $J$  of  $I$  such that  $I^{n+1} = JI^n$  for some  $n > 0$ . Reductions play an important role in the study of Noetherian local rings by allowing a given ideal to be replaced by a “simpler” one in the form of a well-chosen reduction. However, much of the theory of reductions depends on the local ring having an infinite residue field. For example, if  $R$  is a Noetherian local ring with infinite residue field and Krull dimension  $d > 0$ , then every ideal of  $R$  has a reduction that can be generated by  $d$  elements, an assertion that need not be true if  $R$  has a finite residue field. We examine the number of generators needed for reductions of ideals in Noetherian local rings with finite residue field. (Received January 15, 2017)