

1126-05-90

Michael Ferrara* (michael.ferrara@ucdenver.edu). *Ore and Chvátal-type Degree Conditions for Fast Bootstrap Percolation.*

Bootstrap percolation is a deterministic cellular automaton in which vertices of a graph G begin in one of two states “dormant” or “active”. Given a fixed integer r , a dormant vertex becomes active if at any stage it has at least r active neighbors, and remains active for the duration of the process. Given an initial set of active vertices A , we say that G r -percolates (from A) if every vertex in G becomes active after some number of steps. Let $m(G, r)$ denote the minimum size of a set A such that G r -percolates from A .

Here, we provide degree-based density conditions that ensure $m(G, 2) = 2$. In particular, we give an Ore-type degree sum result that states if a graph G satisfies $\sigma_2(G) \geq n - 2$, then either $m(G, 2) = 2$ or G is in one of several exceptional classes. We also give a Chvátal-type degree condition: If G is a graph with degree sequence $d_1 \leq d_2 \leq \dots \leq d_n$ such that $d_i \geq i + 1$ or $d_{n-i} \geq n - i - 1$ for all $1 \leq i < \frac{n}{2}$, then $m(G, 2) = 2$. These results are inspired by, and extend [D. Freund, M. Poloczek, and D. Reichman, Contagious sets in dense graphs, to appear in *European J. Combin.*]/ Joint with Michael Dairyko, Bernard Lidicky, Ryan R. Martin, Florian Pfender and Andrew Uzzell. (Received January 05, 2017)