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**Wei-Hsuan Yu\*** (u690604@gmail.com), 619 Red Cedar Rd, east lansing, MI 48862, and **Alexey Glazyrin**. *New bounds for equiangular lines and spherical two-distance sets.*

The set of points in a metric space is called an  $s$ -distance set if pairwise distances between these points admit only  $s$  distinct values. Two-distance spherical sets with the set of scalar products  $\{\alpha, -\alpha\}$ ,  $\alpha \in [0, 1)$ , are called equiangular. The problem of determining the maximal size of  $s$ -distance sets in various spaces has a long history in mathematics. We determine a new method of bounding the size of an  $s$ -distance set in two-point homogeneous spaces via zonal spherical functions. This method allows us to prove that the maximum size of a spherical two-distance set in  $\mathbb{R}^n$  is  $\frac{n(n+1)}{2}$  with possible exceptions for some  $n = (2k + 1)^2 - 3$ ,  $k \in \mathbb{N}$ . We also prove the universal upper bound  $\sim \frac{2}{3}na^2$  for equiangular sets with  $\alpha = \frac{1}{a}$  and, employing this bound, prove a new upper bound on the size of equiangular sets in an arbitrary dimension. Finally, we classify all equiangular sets reaching this new bound. (Received January 17, 2017)