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Richard M Aron* (aron@math.kent.edu), Richard M. Aron, Department of Mathematics, Kent State University, Kent, OH 44242, Javier Falco Benavent (franjfal@gmail.com), Javier Falco Benavent, Department of Mathematics, Kent State University, Kent, OH 44242, Domingo Garcia, Departamento de Analisis Matematico, Universidad de Valencia, Dr. Moliner, 50, 46100 Burjassot, Spain, and Manuel Maestre, Departamento de Analisis Matematico, Universidad de Valencia, Dr. Moliner, 50, 46100 Burjassot, Spain. Analytic structure in Fibers. Preliminary report.

Let B_X be the open unit ball of a complex Banach space X. Denote by $\mathcal{H}^{\infty}(B_X)$ the Banach algebra of bounded analytic functions $f: B_X \to \mathbb{C}$, endowed with the sup-norm. Our interest is in the maximal ideal space $\mathcal{M}(\mathcal{H}^{\infty}(B_X)) :\equiv$

 $\{\varphi: \mathcal{H}^{\infty}(B_X) \to \mathbb{C} \mid \varphi \text{ is a (non - trivial, continuous) homomorphism}\}.$

After reviewing the classical situation (when $X = \mathbb{C}$ so that $\mathcal{H}^{\infty}(B_{\mathbb{C}})$ is just the standard \mathcal{H}^{∞}), we will discuss properties of the natural fibering $\pi : \mathcal{M}(\mathcal{H}^{\infty}(B_X)) \to \overline{B_{X^{**}}}$. We will examine fibers $\pi^{-1}(z)$ for points $z \in \overline{B_{X^{**}}}$, and we will specialize to two cases: $X = c_0$ and $X = \mathbb{C}^2$, where some intriguing basic questions have arisen.

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