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Jason S Williford* (jwillif1@uwyo.edu), University of Wyoming, Dept 3036, 1000 E. University Ave., Laramie, WY 82071. *Graphs With Schur-Closed Adjacency Algebras.*

Given a labeled graph G with adjacency matrix A , we define the adjacency algebra of G to be the matrix algebra \mathcal{A} generated by A . Since A is diagonalizable, the dimension of \mathcal{A} is simply the number of distinct eigenvalues of A . If G is connected and this algebra is also closed under the Schur (entrywise) product of matrices, we will call the graph G an S -graph.

Distance-regular graphs are examples of S -graphs, however many other interesting graphs which are not distance-regular fall into this class as well. This talk will begin with a combinatorial characterization of S -graphs followed by examples. We will then discuss the ongoing search for examples of certain types of S -graphs, including those with the so-called Q -polynomial property. These are S -graphs whose idempotents E_0, E_1, \dots, E_d in the spectral decomposition of A can be ordered so that E_i is a degree i polynomial of E_1 , where multiplication is the Schur product. (Received August 25, 2015)