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Franklin H. J. Kenter* (franklin.h.kenter@rice.edu). *Spectral Results for Adaptations of Graph Coloring.*

Hoffman proved that for a simple graph G , the chromatic number, $\chi(G)$, obeys $\chi(G) \leq 1 - \lambda_{\max}/\lambda_{\min}$ where λ_{\max} and λ_{\min} are the maximal and minimal eigenvalues of the adjacency matrix of G respectively.

We give a short probabilistic proof of Hoffman's theorem. Then, we extend the technique to variations of graph coloring with additional restrictions and/or relaxations. Our results include necessary spectral conditions for coloring 3-, 4-, and 5-uniform hypergraphs; for coloring graphs limiting the use of colorings with a neighborhood (i.e., frugal coloring); and coloring directed graphs where no color class is a strongly connected component. (Received August 16, 2015)