We show that for any finite coloring of the Gaussian integers, there exist distinct nonzero elements x and y of the same color such that $x^{2}-y^{2}=n^{2}$ for some Gaussian integer $n$. We will also explain the connection between this problem with a structure theorem for multiplicative functions on the Gaussian integers. (Received January 11, 2015)

