1105-65-1Susanne C Brenner* (brenner@math.lsu.edu), Department of Mathematics, Center for
Computation & Technology, Louisiana State University, Baton Rouge, LA 70803. Novel Finite
Element Methods for Optimal Control Problems with PDE Constraints.

Let Ω be a bounded convex polygonal domain in \mathbb{R}^2 . A model elliptic optimal control problem with pointwise state constraints is to find the minimizer of the functional

$$J(y,u) = \int_{\Omega} (y - y_d)^2 \, dx + \beta \int_{\Omega} u^2 \, dx,$$

where $(y, u) \in H_0^1(\Omega) \times L_2(\Omega)$ are subjected to the constraints

$$\int_{\Omega} \nabla y \cdot \nabla v \, dx = \int_{\Omega} uv \, dx \qquad \forall v \in H_0^1(\Omega),$$
$$\psi_1 \le y \le \psi_2 \qquad \text{a.e. in } \Omega.$$

We will present finite element methods for this optimal control problem that are based on the reformulation of the problem as a fourth order elliptic variational inequality for y, discuss their *a priori* and *a posteriori* error analyses, and introduce post-processing procedures that generate approximations of the optimal control u from the approximations of the optimal state y.

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