

1105-22-274

Uladzimir Shtukar* (ushtukar@ncsu.edu), 1801 Fayetteville Street, MTSB, r. 3253, Durham, NC 27707. *Invariant Reductive Triplets in Lie Algebras.*

Let \mathfrak{g} be a Lie algebra, and \mathfrak{h} be a subalgebra Lie at \mathfrak{g} . Suppose that the pair $\mathfrak{g}, \mathfrak{h}$ is reductive, that means there exists a subspace \mathfrak{m} such that $\mathfrak{g} = \mathfrak{h} + \mathfrak{m}$ and $[\mathfrak{h}, \mathfrak{m}] = \mathfrak{m}$. We will say also that the triplet $\mathfrak{g}, \mathfrak{h}, \mathfrak{m}$ is reductive. A homogeneous space G/H with a reductive triplet $\mathfrak{g}, \mathfrak{h}, \mathfrak{m}$ is called reductive; this space has some excellent geometry properties including an effective description of all invariant affine connections on the homogeneous space G/H in terms of the bilinear forms on \mathfrak{m} , that was received by K.Nomizu in Invariant affine connections on homogeneous spaces, Amer. J. Math., 76, 33-65, 1954. If S is an automorphism of Lie algebra \mathfrak{g} that saves \mathfrak{h} and \mathfrak{m} , $S(\mathfrak{h}) = \mathfrak{h}$ and $S(\mathfrak{m}) = \mathfrak{m}$, then we call the reductive triplet $\mathfrak{g}, \mathfrak{h}, \mathfrak{m}$ to be invariant with respect to S . At this case, the automorphism S generates a local affine transformation of the homogeneous space as it was proved by the author in the article Invariant connections and metrics on homogeneous spaces generated by global triplets, Math. Zametki, 26, #3, 449-463, 1979. According to the last basic fact, it is interesting to determine all automorphisms of \mathfrak{g} that save a given reductive triplet. If \mathfrak{g} is a compact Lie algebra, then all possible reductive triplets can be formed using a unique direct sum presentation. (Received September 22, 2014)